SOLUTIONS MANUAL

POWER SYSTEMS ANALYSIS

ARTHUR R. BERGEN VIJAY VITTAL

PART I. SOLUTIONS TO PROBLEM SETS
PART II. DISCUSSION OF SOLUTIONS TO
DESIGN EXERCISES

PRENTICE HALL, Upper Saddle River, New Jersey 07458

Associate Editor: Alice Dworkin

Special Projects Manager: Barbara A. Murray

Production Editor: Meaghan Forbes

Supplement Cover Manager: Paul Gourhan Supplement Cover Designer: Liz Nemeth

Manufacturing Buyer: Pat Brown

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PART I. SOLUTIONS TO PROBLEM SETS

$$\frac{2.1}{i} = \sqrt{2} \times 120 \ co(\omega t + 30^{\circ}) \Rightarrow \sqrt{= 120 (30^{\circ})}$$

$$i = \sqrt{2} \times 10 \ co(\omega t - 30^{\circ}) \Rightarrow T = 10 (-30^{\circ})$$

(b)
$$Z = V/I = 12 (60° = 6+310.39 = R+3 × $\Rightarrow R=6$, $X=10.39$$$

2.2 (a) Using (2.3) we find $P_{max} = 1707 = |V|/II/(cosf+1)$ and $P_{min} = -293 = |V|/II/(cosf-1)$. Then, since |V| = 100, we get |II = 10 and $|Cosf| = \pm 45^\circ$. Dich $|G| = 45^\circ \Rightarrow |Z| = 10/45^\circ = 7.07 + <math>g$ 7.07 = g7.07 = g9.07 = g9.09 = g9

(c) For simplicity assume $i(t) = \sqrt{2} |I| \cos \omega t$. Then $P_L(t) = \sqrt{2} (t) i(t) = L \frac{di}{dt} i = -2\omega L |I|^2 \cos \omega I \sin \omega t = -\omega L |I|^2 \sin 2\omega t$ $P_L max = \omega L |I|^2 = 707 = Q$. Thus $P_L max = Q$. The same!

2.3 0.7 PF laying $\Rightarrow g = 45.57^{\circ}$, Q = 5.10 MVAr 0.9 PF laying $\Rightarrow g = 25.34^{\circ}$, Q = 2.42 MVAr. Capacita must Dupply 5.10 - 2.42 = 2.68 MVAr.

2.4 0.707 PF lagging $\Rightarrow S_{34} = 200 + j 200 \pm VA$. Cap supplies $50 \pm VA$. Resultant $S_{34} = 200 + j 150 \pm VA \Rightarrow PF = 0.80$. $|S| = \frac{|S_{34}|}{3} = \frac{250 \times 10^3}{3} = |Y||I| = \frac{440}{\sqrt{3}}|I| \Rightarrow |II| = 328 A$

(a) S = 10 + j 4.84 hVA

(b) 10 ×103 = 416 × |I| × 0.9 ⇒ |I| = 26.71 A

(c) Using (2.3), (or first principles) we get $P(t) = 10 \times 10^{3} + 11.11 \times 10^{3} \cos(2\omega t + 25.84^{\circ})$ Note: The average value of p(t) is 10 kW

2.6 Because explem is balanced $V_{ab} = 208 / 120^{\circ}$, $V_{bc} = 208 / 0^{\circ}$. Using (2.17) or Fig 2.11, $V_{an} = 120 / 90^{\circ} \Rightarrow V_{bn} = 120 / -30^{\circ}$, $V_{cn} = 120 / -150^{\circ}$. Using per phase analysis, $T_{a} = 12 / 105^{\circ} \Rightarrow T_{b} = 12 / -15^{\circ}$, $T_{c} = 12 / -135^{\circ}$.

 $\frac{2.7}{2.7} \quad S = VI^* = V(YV)^* = Y^*NI^2 = Y_c^* + Y_L^* + Y_R^*$ = -35 + 310 + 0.1 = 0.1 + 35

 $\frac{2.8}{10}$ (a) Wing loop a nodel analysis we find, after much work, $I_a = 0.9123 / -90.351^{\circ}$, $I_b = 0.9123 / -209.65^{\circ}$, $I_c = 0.9929 / 30^{\circ}$. (b) Using per phase analysis $I_a = 1/0^{\circ}/j 1.1 = 0.9091 / -90^{\circ}$, then, $I_b = 0.9091 / -210^{\circ}$, $I_c = 0.9091 / 30^{\circ}$.

2.9 Proceeding by analogy with 3\$\phi\$, we note $E_{ab} = E_{an} - E_{bn} = E_{an} \left(1 - e^{-j\pi/2}\right) = \sqrt{2} E_{an} e^{j\pi/4}.$ Thus $E_{an} = \frac{1}{\sqrt{2}} E_{ab} e^{-j\pi/4}$, and $E_{an}, E_{bn}, E_{cn}, E_{dn}$ from a pos. seq. set of 4\$\phi\$ voltages. Doing per phase (phase) analysis we have

 $\frac{1}{12} (45^{\circ})^{\frac{1}{2}} - j0.5 \Rightarrow I_{a} = \frac{1}{12} (-45^{\circ}) = \sqrt{2} \cdot (-135^{\circ})$

Then I6 = J2 /-225°, Ic = J2 /-315°, IJ = J2 /-405°

2.10 Using per phase circuit we find $I_a = 103.8 / 41.5^{\circ}$.

240 $\sqrt{3}$ $T_{A} = \frac{1}{3} \frac{1}{100} c = -\frac{1}{3} \cdot 0.884$

Vain = Z, Ia = 91.76 (-48.5° > |Vaibi | = 53.91.76= 158.9 V

 $S_{lose} = V_{ain} T_a^* = 9524 / -90^\circ$

Send = 3 Spood = 28574 (-90° W

Assume pos. seg. operation. Vo"b" = Vo"n - Vo"n = J3 Vaine at/6 > Vain = 方 Vaibi e-3 11/6 = 方 130° Per Phase Cht 100 + 0 10.1 = 10.1 0+ ± 1-300 Voltage divider law we get

Vain = 0.899 (-10.89° > Vyn = 0.899 (-130.89° Vun = 0.899 /-250.89°. Then Vaib! = 1.557 /19.11°

2.12 Assume pos. seq. Per Phase Cht In al 10° 5 31 310 3 1 - j 10

Combining parellel elements we have Z1 = - 15. Ta = 0.25 /10° Vain = - 15. jo.25 = 1.25 60° Va'b' = 2.165 (30° > Iap-.2165/120° | Ib= 1.20 /90°, Ic= 1.20 /-150° Stord = 3 Vain Ia = 0.3125 /-900

(a) Vbc = 208/-120°, Yea=208/120° $V_{an} = \frac{208}{\sqrt{3}} \left(-30^{\circ} \right) = 1.20 \left(-90^{\circ} \right)$ Then Tb= 1.20 (-210°, Ic= 1.20 (-330°

(b) Vbc = 208/120°, Vca = 208/-120° $V_{an} = \frac{208}{\sqrt{3}} \left(\frac{30}{30} \right) \Rightarrow \Gamma_a = 1.20 \left(\frac{-30}{30} \right)$

Per Phase cht. Problem reduces to picking Z so that Vain > I van 1. It helps to draw some phase digrams.

I. Z=jwL	I Z=R	皿 2=-ま立
disp disp in 31 in 1st I	Vain drop in 31	Fr. example $Z=-j2$ $I = \frac{1}{\sqrt{2}} \text{ (45°)}$ $V_{0'n} = \sqrt{2} \text{ (-45°)}$
clearly Vain / Van	clearly Wa'n K I Van)	Vain > Vain This is o.k.

2.15 Since $E_a + E_b + E_c = 0$, neutrols are at same potential. $Z = E_a / I_a = \sqrt{2} (55^\circ)$. For each Z, $S = V I'' = |V|^2 / Z''$. Thus $S^{3\phi} = \frac{(\sqrt{2})^2 + 1^2 + 1^2}{\sqrt{2} (-55^\circ)} = 2\sqrt{2} (55^\circ).$

$$\frac{3.1}{2\pi} = 2 \times 10^{-7}, |T_a| = 100$$

(Upward) flux luikages of telephone wies

$$\lambda = 2 \times 10^{-7} \left[i_a ln \frac{26}{25} - i_a ln \frac{21}{20} \right] = -.00957 \times 2 \times 10^{-7} i_a$$

V+el = d/d => Vtel = JWx (-0.00957x2x10-7) x 100 V/melen

Since 1 mile = 1.609 km, |V+el | = 0.116 V/mile

3.2
$$\lambda = 2 \times 10^{-7} i_{a} \left[ln \frac{\sqrt{25^{3}+11^{2}}}{\sqrt{25^{3}+10^{3}}} - ln \frac{\sqrt{20^{3}+11^{2}}}{\sqrt{20^{3}+10^{3}}} \right]$$

$$= -0.066 294 \times 2 \times 10^{-7} i_{a}$$

$$\Rightarrow |V_{+el}| = 0.076 V/mile$$

 $\lambda = 2 \times 10^{-7} \left[i_a \ln \frac{31}{30} + i_b \ln \frac{20}{25} + i_c \ln \frac{21}{20} \right]$ $= 2 \times 10^{-7} \left[0.0328 i_a + 0.0392 i_b + 0.0488 i_c \right]$

 $V_{\text{tel}} = 3 \times 2 \times 10^{-7} \left[0.0328 \, \text{Ja} + 0.0392 \, \text{Jb} + 0.0488 \, \text{Je} \right]$ $|V_{\text{tel}}| = 377 \times 2 \times 10^{-7} \times 100 \times \left| 0.0328 + 0.0392 \, \frac{\left| -120^{\circ} + 0.0488 \right| 120^{\circ}}{120^{\circ}} \right|$ $= 1048 \times 10^{-7} \, \text{V/meler} = 0.1692 \, \text{V/mile}$

34 The telephone wies are trampsed every 1000 ft. Cancellation occurs in all but 720' of line \$ 0.0158 V.

The flux linkages due to the current in the left enductor is $\approx \lambda_1 = \frac{\mu_0}{2\pi} i \left[\frac{\mu_r}{4} + \ln \frac{D}{r} \right] = i \frac{\mu_0}{2\pi} \ln \frac{D}{r'}$

Here we are neglecting partial flux linkages of the far (right) conductor. The current in the right conductor containbutes an equal number of flux lunkages. Thus (at least appears in slely),

l = 2 1/i = 10 ln D = 4 × 10-7 ln D H /melu

3.6 If each conductor is hollow then the are no partial flux lunkage, and in (3.13) the term involving Mr is absent. Then r'= r and

$$l = \frac{\mu_0}{2\pi} \ln \frac{D}{r}$$
 H/m

3.7 The hint is misleading. A better hint for combining the 7 (unequal) inductances l_1, l_2, \dots, l_7 would be to use the average inductance i.e. let $l_a = \frac{l_{av}}{7} = \frac{l_1 + l_2 + \dots + l_7}{7^2}$ Returning to the problem, paralleling the steps which lead to (3.27) we have

$$\lambda_{1} = \frac{u_{0}}{2\pi} \left[\frac{i_{0}}{7} \left(\ln \frac{1}{d_{11}} + \ln \frac{1}{d_{12}} + \dots + \ln \frac{1}{d_{17}} \right) + \frac{i_{0}}{7} \left(\ln \frac{1}{d_{18}} + \ln \frac{1}{d_{19}} + \dots + \ln \frac{1}{d_{1,21}} \right) + \frac{i_{0}}{7} \left(\ln \frac{1}{d_{1,15}} + \ln \frac{1}{d_{1,16}} + \dots + \ln \frac{1}{d_{1,21}} \right) \right]$$

$$\approx \frac{\mu_{0}}{2\pi} i_{0} \ln \frac{D}{(d_{11} \cdots d_{17})^{1/7}} \Rightarrow l_{1} = 7 \times \frac{u_{0}}{2\pi} \ln \frac{D}{(d_{11} \cdots d_{17})^{1/7}}$$

$$l_{a} = \frac{l_{av}}{7} = \frac{l_{1} + \cdots + l_{7}}{7^{2}} = \frac{\mu_{0}}{2\pi} \ln \frac{D}{R_{S}}$$
where $R_{S} \triangleq \left[(d_{11} \cdots d_{17})^{l_{7}} - \cdots + (d_{71} \cdots d_{77})^{l_{77}} \right]^{l_{7}}$

Six of the product terms are the same; the relevant distances are shown on the left. The different germetay is for the center wire to

the outside wires. Let d = 0.0876 in be the wine diameter. Noting that die = 0.7788. & we have Rs=[((0.7788 \frac{d}{2}).d3.2d.(\sqrt{3d})2)6(0.7788 \frac{d}{2}.d6)] 1/72

= 1.088 d = 0.0943 in. = 0.00786 ft.. che!

 $D_{m} = (45' \times 45' \times 90')'3 = 56.70 \text{ ft}$ R = (0,0479 x 1.5 x 52 x 1.5) 4 = .69151

$$L = 2 \times 10^{-7} lm \frac{D_m}{R_b} = 8.81 \times 10^{-7} H/m$$

3.10 Using $r' = 0.7788 \times \frac{1.424}{2} \times \frac{1}{12} = 0.0462'$ (instead of GMR = 0.0479) we get Rb = 0.6853!

 $l = 2 \times 10^{-7} \text{ en } \frac{D_m}{R_1} = 8.83 \text{ H/m} . \approx 0.23\% \text{ eno.}$

$$\frac{3.11}{L} = 9.47 \times 10^{-7} \, H/m$$

$$X_{L} = 1609 \times 377 \times 9.47 \times 10^{-7} = 0.574 \, 2s/m \, 1e$$

$$\frac{3.12}{L} = D_{m} = (26' \times 26' \times 52')^{1/3}, R_{b} = (0.0386' \times 15)^{1/2} = 0.2406'$$

$$L = 2 \times 10^{-7} \ln \frac{D_{m}}{R_{b}} = 9.83 \times 10^{-7} H/m$$

3.13 Using
$$r' = 0.7788 \times \frac{1.165}{2} \times \frac{1}{12} = 0.0378'$$
 we get $12_b = 0.2381'$

$$1 = 2 \times 10^{-7} \ln \frac{D_m}{P_b} = 9.85 \text{ H/m}. \approx 0.20\% \text{ even}.$$

$$\frac{3.15}{r} = \frac{D_{m} = (45' \times 45' \times 90')^{1/3} = 56.70'}{r = \frac{1.424''}{2} \times \frac{1}{12} = 0.0593', R_{b}^{c} = (0.0593 \times 1.5^{2} \times 5^{2} \times 1.5^{2} \times 1.5^{2}$$

$$\begin{array}{rcl}
\frac{3.17}{D_{m}} & D_{m} = \left(2C^{1} \times 2C^{1} \times 52^{1}\right)^{1/3} = 32.7C^{1} \\
Y & = \frac{1.165^{"}}{2} \times \frac{1}{12} = 0.0485^{1} \\
R_{b}^{c} & = \left(0.0485^{1} \times 1.5^{1}\right)^{1/2} = 0.26981 \\
C & = 11.59 \times 10^{-12} = 1.59 \times 10^{-12} = 1.59 \times 10^{-12}
\end{array}$$

3.18
$$B_c = 1609 \times 377 \times 11.59 \times 10^{-12} = 7.03 \times 10^6 \text{ZT/mi},$$
 $|X_c| = 1/B_c = 0.142 \text{ M.S.} / \text{mile}$

$$2c = 8.81 \times 10^{-7} \times 12.78 \times 10^{-12} = 11.259 \times 10^{-18}$$

$$4.660 = 4 \times 10^{-7} \times 8.854 \times 10^{-12} = 11.126 \times 10^{-18}$$

3.20
$$l c = 9.83 \times 10^{-7} \times 11.59 \times 10^{-12} = 11.393 \times 10^{-18}$$
 $M_0 \epsilon_0 = 11.12 C \times 10^{-18}$

Note: $\mu_0 \epsilon_0$ is a universal constant.

Velocity of light in vacuum "c" = $\frac{1}{\sqrt{\mu_0 \epsilon_0}} \approx 2.998 \times 10^8$
 m/sec .

3.21

 $r_a = r_b = r_c = 0.145 \, \Omega/\text{mi}$, from Table A8.1, for Grosbeak, at 25°C.

 $GMR_a = GMR_b = GMR_c = 0.0355$ ft. (From Table A8.1).

Assume $\rho = 100 \Omega$ -m (as in Example 3.6), f = 60 Hz, then

$$D_e = 2160 \sqrt{\frac{\rho}{f}} = 2160 \sqrt{\frac{100}{60}} = 2790 \text{ ft.}$$

At 60 Hz, $r_d = 9.869 \times 10^{-7} \times f$ Ω/m

Using the conversion factor: 1 mile = 1.609 km we get

 $r_d = 0.09528 \ \Omega / \text{mi}$

Then
$$z_{aa} = z_{bb} = z_{cc} = r_a + r_d + j\omega \times 2 \times 10^{-7} \ln \frac{D_e}{GMR_i} \Omega/m$$

=
$$(0.145 + 0.09528) + j(377 \times 2 \times 10^{-7}) (n \frac{2790}{0.0355} \times 1.609 \times 10^{3}) = 0.2403 + j1.3675 \Omega/mi$$

$$d_{ab} = \sqrt{4^2 + 5.5^2} = 6.807 \text{ ft}, \ d_{ca} = 4 \text{ ft}, \ d_{bc} = 5.5 \text{ ft}.$$

$$z_{ab} = r_d + j\omega \times 2 \times 10^{-7} \ln \frac{D_e}{d_{ab}} \Omega/m$$

=
$$0.09528 + j(377 \times 2 \times 10^{-7}) \ln \frac{2790}{6.8007} \times 1.609 \times 10^3 = 0.09528 + j \cdot 0.7299 \Omega/mi$$

Similarly using $d_{bc} = 5.5$ ft. and $d_{ca} = 4$ ft., we get

$$z_{bc} = 0.09528 + j \cdot 0.7557 \Omega / \text{mi}, \ z_{ca} = 0.09528 + j \cdot 0.7943 \Omega / \text{mi}$$

For 30 miles of line we multiply the above values by 30 to write, in matrix notation

$$Z_{abc} = \begin{bmatrix} (7.209 + j41.025) & (2.858 + j21.8970) & (2.858 + j23.8290) \\ (2.858 + j21.8970) & (7.209 + j41.025) & (2.858 + j22.6710) \\ (2.858 + j23.8290) & (2.858 + j22.6710) & (7.209 + j41.025) \end{bmatrix} \Omega$$

3.22

 $r_a = r_b = r_c = 0.306 \text{ }\Omega/\text{mi}$ (From Table A8.1, for Ostrich, at 25°).

 $GMR_a = GMR_b = GMR_c = 0.0230 \text{ ft.}$ (From Table A8.1).

Assume $\rho = 100 \ \Omega$ -m as in Example 3.6, $f = 60 \ Hz$, then

$$D_e = 2160 \sqrt{\frac{\rho}{f}} \text{ ft } = 2160 \sqrt{\frac{100}{60}} = 2790 \text{ ft.}$$

At 60 Hz,
$$r_d = 9.869 \times 10^{-7} \times f \Omega / m$$

Using the conversion factor: 1 mile = 1.609 km we get $r_d = 0.09528 \ \Omega / mi$

Then
$$z_{aa} = z_{bb} = z_{cc} = r_a + r_d + j\omega \times 2 \times 10^{-7} \ln \frac{D_e}{GMR_i} \Omega / \text{m}$$

$$= (0.306 + 0.09528) + j(377 \times 2 \times 10^{-7}) \ln \frac{2790}{0.0230} \times 1.609 \times 10^3 \Omega / \text{mi}$$

$$d_{ab} = d_{bc} = \sqrt{4^2 + 1.5^2} = 4.2720 \text{ ft}, d_{ca} = 8.0 \text{ ft}.$$

$$z_{ab} = r_d + j\omega \times 2 \times 10^{-7} \ln \frac{D_e}{d_{ab}} \Omega / \text{m}$$

$$= 0.09528 + j(377 \times 2 \times 10^{-7}) \ln \frac{2790}{4.2720} \times 1.609 \times 10^3 = 0.09528 + j0.7864 \Omega / \text{mi}$$

$$z_{bc} = z_{ab} = 0.09528 + j0.7864 \Omega / \text{mi}.$$

Similarly using
$$d_{ca} = 8.0$$
 ft. we get $z_{ca} = 0.09528 + j \cdot 0.7102 \Omega/\text{mi}$.

For 40 miles of line we multiply the above values by 40 to write, in matrix notation

$$Z_{abc} = \begin{bmatrix} (16.0512 + j \, 56.804) & (3.8112 + j \, 31.456) & (3.8112 + j \, 28.408) \\ (3.8112 + j \, 31.456) & (16.0512 + j \, 56.804) & (3.8112 + j \, 31.456) \\ (3.8112 + j \, 28.408) & (3.8112 + j \, 31.456) & (16.0512 + j \, 56.804) \end{bmatrix} \Omega$$

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