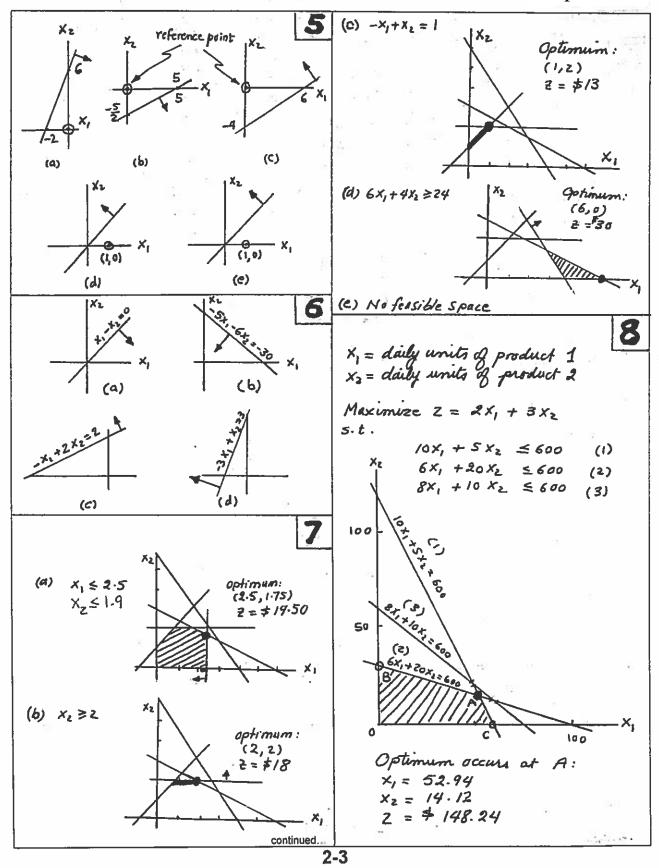
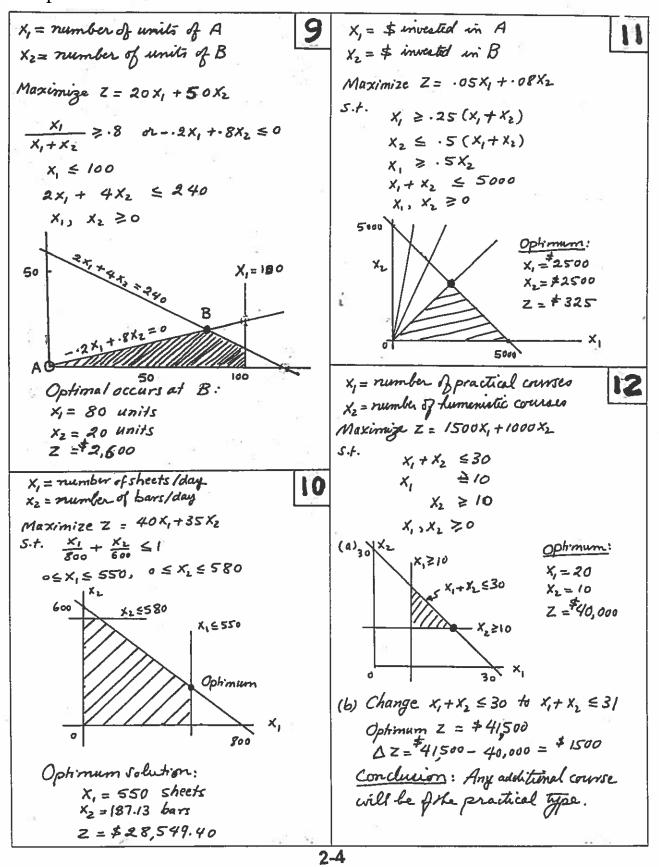
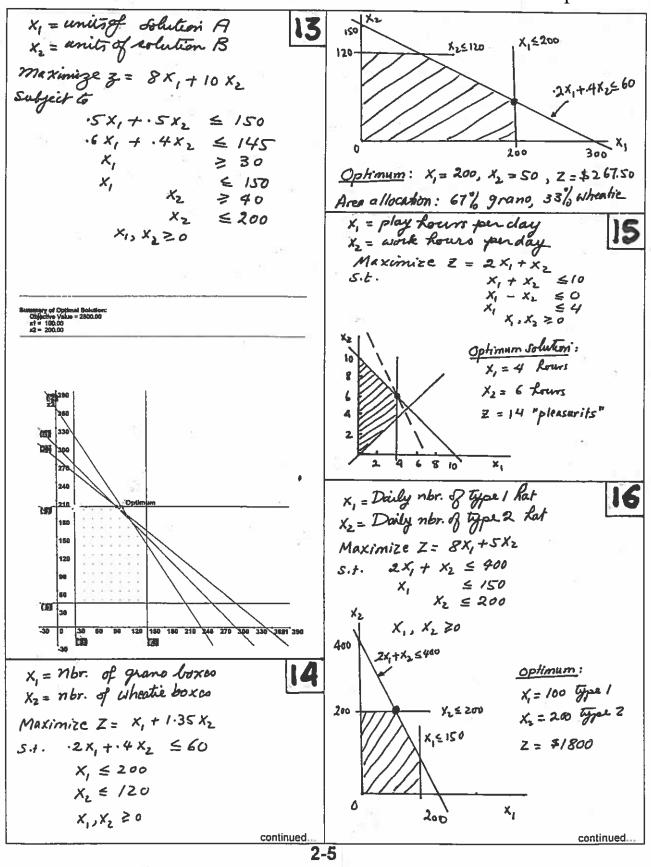
CHAPTER 2

Modeling with Linear Programming

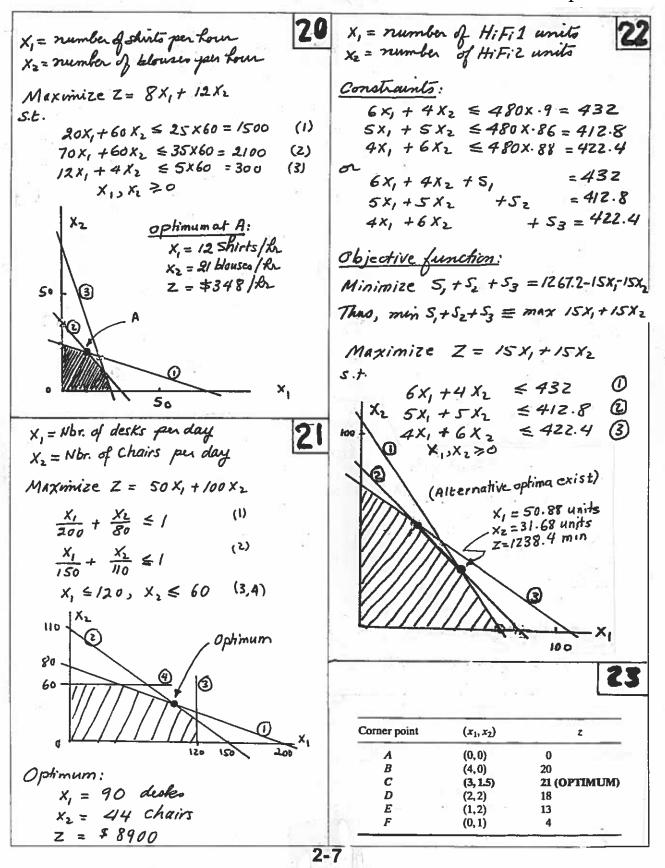
(a) $X_2 - X_1 \ge 1$ or $-X_1 + X_2 \ge 1$ Quantity discount results in the 4. (b) $X_1 + 2X_2 \ge 3$ and $X_1 + 2X_2 \le 6$ (c) $X_2 \ge X_1$ or $X_1 - X_2 \le 0$ (d) $X_1 + X_2 \ge 3$ $Z = \begin{cases} 5X_1 + 4X_2, & 0 \le x_1 \le 2\\ 4 \cdot 5X_1 + 4X_2, & X_1 > 2 \end{cases}$ (a) $x_1 + x_2 \ge 5$ (c) $\frac{x_2}{x_1 + x_2} \le .5 \text{ or } .5x_1 - .5x_2 \ge 0$ 2 (a) $(X_{13}X_{3}) = (1, 4)$ $(X_1, X_2) \geq 0$ $(X, X_1) = (2, 2)$ $(X, X_1) = (2, 2)$ (X,6x1+4x4 = 22 < 24 $1x1+2x4 = 9 \pm 6$ infeasible (b) $(x, x_1) = (2, 2)$ Z = 5x2 + 4x2 = \$18(c) $(X_1, X_2) = (3, 1.5)$ X13X2 30 $6 \times 3 + 4 \times 1.5 = 24 = 24$ $1 \times 3 + 2 \times 1.5 = 6 = 6$ $-1 \times 3 + 1 \times 1.5 = -1.5 < 1$ $1 \times 1.5 = 1.5 < 2$ $Z = 5_{X3+} 4_{XI-5} = 21 $(d)(X_{1,1}X_{2}) = (2,1)$ $x_1, x_2 \ge 0$ $6 \times 2 + 4 \times 1 = 16 < 24$ feasible $1 \times 2 + 2 \times 1 = 4 < 6$ $-1 \times 2 + 1 \times 1 = -1 < 1$ 1×1 =1 $Z = 5x_2 + 4x_1 = 14 (e) $(X_1, X_2) = (29 - 1)$ $X_1 \ge 0, X_2 < 0$, infeasible Conclusion: (c) gives the best feasible Solution $(X_1, X_2) = (2, 2)$ det 5, and 52 be the unused daily 3 amounts of Mi and M2. For M1: 5, = 24 - (6x, + 4x) = 4 tons/day For M2: $S_2 = 6 - (x_1 + 2x_2)$ = 6-(2+2X2) = 0 tons / day 2-2

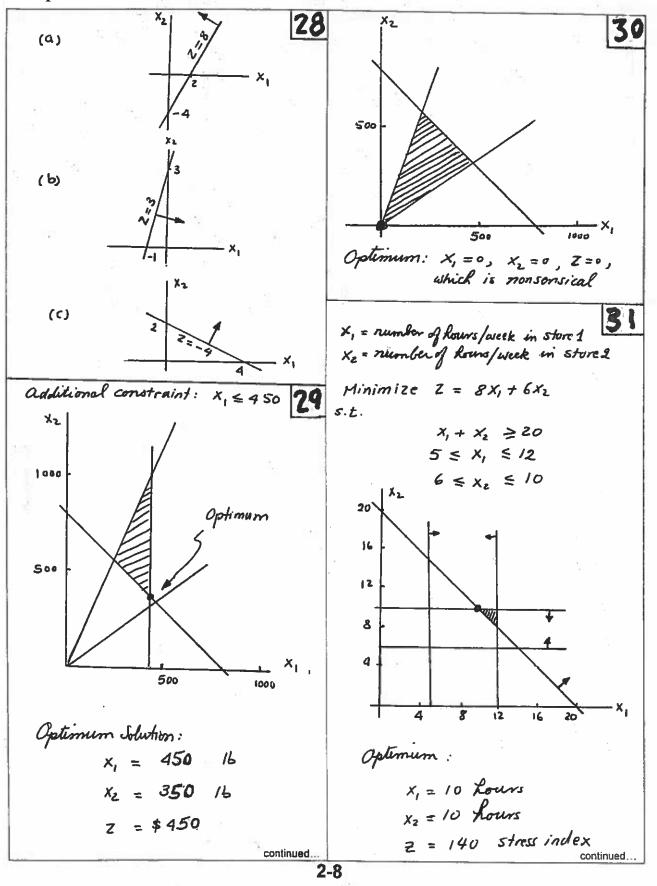




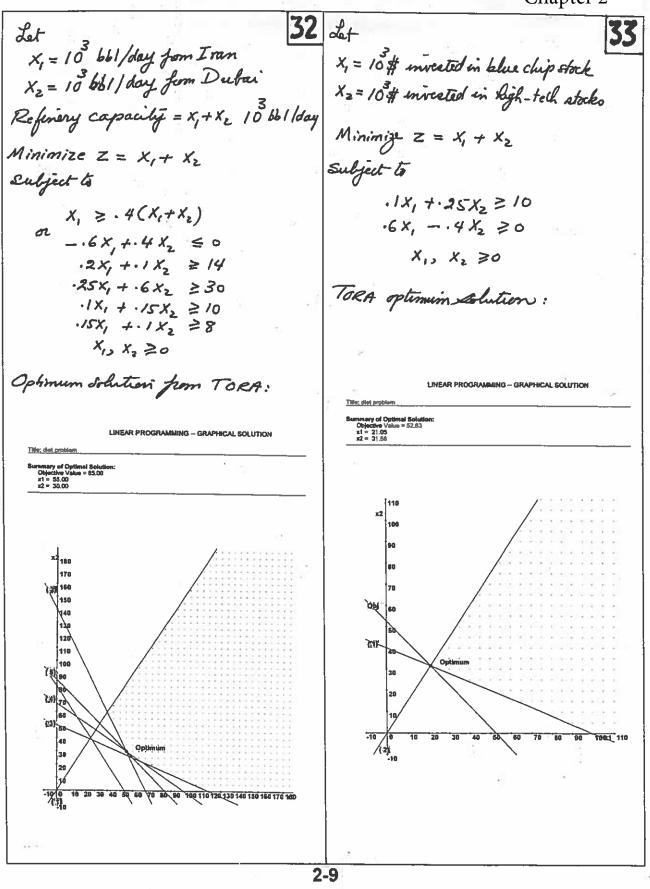


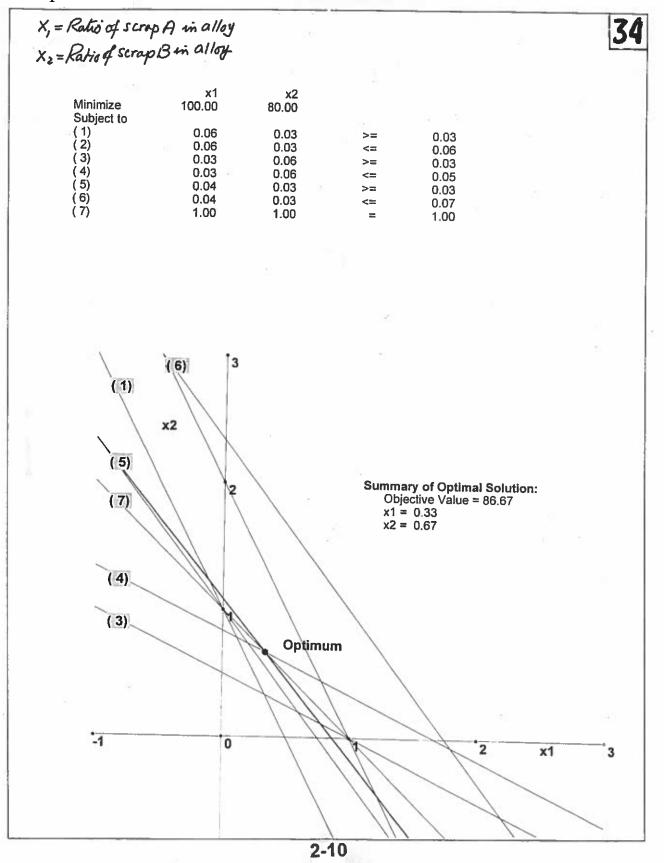
X1 = radio minutes X2 = TV minutes (a) Optimum occurs at A: X,= 5.128 tons per hour X2 = 10.256 tons per how Maximize $Z = X_1 + 25X_2$ Z = 153,846 16 of Steam S.t. 15×, + 300×2 ≤ 10,000 Optimal ratio = 5.128 = .5 $\frac{X_1}{X_2} \ge z \quad \text{or} \quad -X_1 + 2X_2 \le 0$ (b) $2.1x_1 + .9x_2 \le (20+1) = 21$ $X_1 \leq 400, X_1, X_2 \geq 0$ Optimum Z = 161538 16 of steam Az = 161538-153846 = 7692 16 200 X. X, = Nbr. of radio commercials 19 beyond the first X2 = Nbr. of TV ads beyond the first x,\$400 Maximize Z = 2000 X, + 300 0X2 + 5000 + 2000 100 5.t. 300(X,+1) +2000(X,+1) ≤ 20,000 5X, + 300 X2 = 10000 300 (X+1) 5 .8x 20,000 2000 (X2+1) < . 8× 20,000 X., X. >0 or Maximize Z = 2000x, +3000x2+7000 Optimum occurs at A: X, = 60.61 minutes 300 X, + 2000 X2 ≤ 17700 \bigcirc S.F. X = 30.3 minutes (2) 300×1 ≤ 15700 Z = 8/8.18 2000x2 ≤ 14000 (3) x, = tons of C, consumed per hour 18 X2 = tons of C2 consumed per Rour Maximize Z = 12000 X, + 9000 X2 X1, X2 20 Xa S.t. 1800 ×, + 2100 ×2 ≤ 2000 (×,+×2) s - 200 X1 + 100 X2 50 (1) 2.1 x, + .9 x, = 20 ×, X, , X, 30 X٤ 52.33 Optimum colation : 20 Radio commercials = 52.33+1 = 53.33 TV ads = 1+1 = 2 10 Z = 107666.67+7000 = 114666.67 continued. 2-6





÷.,





(a) X:= Undertaken portion of project i 40 (d) The elack S: in period i is treated as an unrestricted variable. Maximize TORA optimum solution : 2= \$131.30 Z = 32.4X, +35.8X2+17.75X3 + 14.8X4+18.2X5 $S_1 = 2.3, S_2 = .4, S_3 = -5, S_4 = -6.1$ + 12-35 Xc This means that additional funds are Subject to 10.5x,+8.3x2+10.2x3+7.2x4+12.3x5+9.2x2 ≤60 needed in years 3 and 4. 14.4×1+12.6×2+14.2×3+10.5×4+10.1×5+7.8×6 ≤70 Increase in return = 131.30 - 116.06 2.2x, + 9.5x, +5.6x, +7.5X, + 8.3x, + 6.9x, ≤35 = \$ 15.24 2.4 x, +3.1x +4.2x + 5.0x + 6.3x + 5.1 x = 20 Ignoring the time value of money, 0 5 x, 1 = 1, j= 13, ..., 6 The amount borrowed 5-+6.1- (2.3+.4) TORA optimum Solution: =\$8.4. Thus, $X_1 = X_2 = X_3 = X_4 = 1, Y_5 = .84, X_6 = 0, Z = 116.06$ rate of return = 15.24-8.4 ~ 81% (b) Add the constraint X, < X6 8.4 TORA optimum Solution: 41 $X_{1} = X_{2} = X_{3} = X_{4} = X_{6} = 1, X_{5} = 0.03, Z = 113.68$ Xi= dollar investment in project i, i=1,2,3,4 (C) Let 5. be the unused funds at the end of year i and change the right-hand Y = dollar investment in bank in year j, j=1,2,3,4,5 Sides of constraints 2, 3, and 4 to 70+5, 35+52, and 20+53, respectively. Maximize Z = 75 TORA optimum solution : Subject to $X_1 = X_2 = X_3 = X_4 = X_5 = 1, X_6 = .71$ $X_1 + X_2$ + ×4 + J, Z = 127.72 (thousand) ≤ 10,000 · 5x, + · 6x2 - ×3 + · 4×4 + 1.065 +, - y = 0 The solution is interpreted as follows: $\cdot 3X_1 + \cdot 2X_2 + \cdot 8X_3 + \cdot 6X_4 + 1.065 + - y_2 = 0$ L Si. Si-Si-I Decision 1.8×1+1.5×2+1.9×3+1.8×4+1.065+3-44=0 1 4.96 1.2x,+1.3x2+.8X3+.95X4+1.0654,-45== 7.62 +2.66 Don't borrow from yr 1 Z all variables 20 3 4.62 -3.00 Borrow \$3 from year 2 TORA optimal solution : 4 Borrow \$4.62 from yr 2 -4.62 0 $X_1 = 0, X_2 = {}^{\$} | 0,000, X_2 = {}^{\$} 6000, X_4 = 0$ The effect of availing excess money H= 0, H=0, H3 = \$6800, H4=\$33,642 for use in later years is that the first five projected are completed Z = \$53,628.73 at the start of year 5 and TI of of project 6 is undertaken. The total revenue increases from \$ 116,060 to 127,720. continued. 2-11

Pi = fraction undertaken of project 42 4. Assume that the investment レ, レニリノン Bi= million dollars borrowsed in program ends at the start of year 11. quarter j, j=1, 2, 3, 4 This, The 6-year bond option can be S; - Surplus million dollars at the start exercised in years 1, 2, 3, 4, and 5 of quarter j, j = 1, 2, 3, 4, 5 only Similarly, the 9-year bond can be need in years 1 and 2 only. Hence, i+β_i, {+B2 1+ B₂ 1+84 from year 6 on, the only option available is moured savings at 7.5%. 1.0255 Let Hozs B2 1.025 B2 1.025 8 1-025B I. = insured savings modelments on year i, i=1,2, ..., 10 19+38 3.19+2.58 1.59-1.582 -1.69-1.882 -58-2.882 Gi = 6-year bond investment in year i, i=1,2,..., 5 (a) Maximize $Z = S_5$ Mi = 9-year bond investment in Subject to year i, i=1,2 $P_{1}^{+}+3P_{2}^{+}+S_{1}^{-}-B_{1}^{+}$ The objective is to maximize total 3.1P+2.5B-1.025, +52+1.025B1-B2=1 accumulation at the end of year 10; 1.5 P-1.5P,-1.02 5,+5,+1.025 B2-B3=1 that is , -1.8 p-1.8 p-1.02 53 + 54+1.025 B3 - B4 = 1 maximize Z = 1.075 I, +1.079 Gs+1.085M -5 P1-2.8 P2-1.02 S4 + 55 +1.025 B4 =1 The constraints represent the balance $o \leq P_1 \leq I, o \leq P_2 \leq I$ equation for each year's cash flow. $o \leq B_{i'} \leq 1, j = 1, 2, 3, 4$ Optimim Solution : I, +.98G, +1.02M, =2 $P_1 = .7113$ $P_2 = 0$ I2+ .98G2+1.02M2 Z = 5.8366 million dollars = 2+1.075 I, +.079 G, +.085 M $I_3 + .98G_3$ B, = 0, B2 = .9104 million dollars $= 2.5 + 1.075 I_2 + .079(G_1 + G_2)$ B3 = 1 million dollars, B4=0 $+ .085(M_1 + M_2)$ (b) B,=0, S,=.2887 million\$ $I_{4} + .98G_{q} = 2.5 + 1.075I_{3} +$ $B_{2} = .9/04, S_{2} = 0$ ·079 (G1+G2+G3) + $B_3 = 1, S_3 = 0$.085 (M, + M2) By=0, Sy = 1.2553 Is + .98 Gs = 3+1.075 I4 + The solution shows that Bi S; = 0 , ·079 (G1+G2+G3+G4)+ meaning that you can't forrow and also -085(M, + M2) end up with surplus in any quarter. I6=3.5+1.075 I5 The result makes sense because the $+ \cdot 079(G_1 + G_2 + G_3 + G_4 + G_5)$ cost of borrowing (2.5%) is higher then +.085 (M,+M2) the return on surplus funds (2%) continued. 2-12

XiA = amount invested in yari, 44 plan A (1000\$) $I_7 = 3.5 + 1.075 I_6 + 1.079 G_1$ $+.079 (G_2 + G_3 + G_4 + G_5)$ +.085 (M,+M2) XiB = amount invested in year i, plan B (1000\$) $I_{g} = 4 + 1.075 I_{7} + 1.079 G_{2}$ $+ \cdot 079 (G_3 + G_4 + G_5)$ +.085 (M, + M2) Maximize Z = 3 X2B + 1.7 X3A Ig = 4 + 1.075 Ig + 1.079 G3 + .079 (G4+G5) Subject to + .085 (M, + Me) XIA + XIR I10 = 5+1.075 Ig + 1.079 Gy *≤ 100* -1.7 X_{IA} + X2A+ X2B +.079 G5 +1.085 M, +.085 M, all variables 20 $-3 \times_{1B} - 1.7 \times_{2A} + \times_{3A} = 0$ *** OPTIMUS SOLUTION SUPPLY *** XiA, XiB =0 for i=1, 2,3 Title: Problem 26m-14 Final iteration No: 14 Objective value (max) = 46.8500 PTIMUM SOLUTION SUPPLAY *** Value Obj Coeff Obj Val Contrib Title: Problem 2.6e-15 Final iteration Re: 6 Objective value (mm.) = 510.000 => ALTERNATIVE solution detected 0.0000 0.0000 0.0000 at 11 0.0000 0.0000 0.0000 0.0000 \$10,0000 13 13 0.0000 0.0000 0.0000 0.0000 4.6331 9.6137 15.4678 Variable Value 0.0000 Obj Coeff Obj Val Contrib 86 16 87 17 a1 a14 100.0000 0.0000 0.0000 A2 x19 x3 x2A x4 x29 x5 x3A 0.0000 0.0000 0.0000 0.0000 x9 19 x9 19 x10 110 x11 51 5.0000 0000 0.0000 17.520 170.000 3.0000 510,000 3141 0000 1.7000 ±12 0.0000 x13 G3 x14 G4 x15 G5 Constraint 9053 0.0000 RHS Slack(-)/Surplus(+) 3.1399 1 (4) 2 (4) 3 (4) 3.9028 1.9608 2.1242 100.0000 0.0000 0.0000 .0790 2111 0.0000 ±16 H1 0.0000 x17 H2 1.0850 Constraint ENS Slack(+)/Surplus(+) Optimum solution: Invest \$100,000 in A in yr I and 2.0000 2.0000 2.5000 1 (=) 0.0000 \$170,000 in B in yr 2. 0.0000 Alternative optimum: Invest \$100,000 in B in yr 1 and 2.5000 5 (=) 5 (=) 6 (=) 7 (=) 8 (=) 9 (=) 10 (=) 3 0000 0.0000 \$300,000 in A in yr 3. X1 = dollars allocated to choice i, 45 $\dot{\mathcal{L}} = 1, 2, 3, 4$ Jear. Recommendation Y = minimum return Invest all in 9-yr bond 1 -3X1+4X2-7X3+15X4 Investall in 9-yr. bond 2 Investall in 6-yr bond Maximize Z = min { 5x1 - 3x2 + 9x3 + 4X4 3 Investall in Gyr bond subject to (3x1 - 9x2 + 10x3 - 8x4 4 5 Investall in 6-yr bond $X_{1} + X_{2} + X_{3} + X_{4} \leq 500$ Invest all in insured savings 7 Invest all in incured savings X1, X2, X3, XY ≥0 8 The problem can be converted to Invest all in insured sarings 9 Survest all in moured savings 10 a linear program as continued 2-13

$$\begin{array}{rcl} & \text{Maximize } \mathbb{Z} = \# \\ & \text{subject } \text{fs} \\ & \text{subject } \text{fs} \\ & -3x_1 + 4x_2 - 7x_3 + 1/5 & x_4 \geq \# \\ & \text{subject } \text{fs} \\ & -3x_1 + 4x_2 - 7x_3 + 1/5 & x_4 \geq \# \\ & 5x_1 - 3x_2 + 9x_3 + 4 & x_4 \geq \# \\ & 5x_1 - 3x_2 + 9x_3 + 4 & x_4 \geq \# \\ & 3x_1 - 9x_2 + 10x_3 - 8x_4 \geq \# \\ & 3x_1 - 9x_2 + 10x_3 - 8x_4 \geq \# \\ & x_1 + x_2 + x_3 + x_4 \leq \text{SDO} \\ & x_1 + x_2 + x_3 + x_4 = x_4 + x_4 = x_4 + x_4$$

Y,

X:36

0

0

0

0 0

0

0

Xw1 = # wrenches / wk using regular time 47 46 X = number of units -produced of XW2 = # wrenches / wk using overtime XW2 = # wrenches / wk using subcontracting product j, j=1,2,3,4 Xc1 = # Chisilo/WK using regular time Profit per unit: X_{C2} = # chiels/wk using overtime K_{C3} = # chiels/wk using subcontracting Product 1= 75-2×10-3×5-7×4 = \$12 Minimize Z = 2 X + 2.8 X + 3 X + 2.1 X CI Product 2 = 70 - 3x10 - 2x5-3x4 = \$ 18 Product 3 = 55-4×10-1×5-2×4= \$2 + 3.2× C2 + 4.2× C3 Subject to Product 4 = 45 - 2×10 - 2×5-1×4 = \$ 11 $X_{\omega_1} \leq 550$, $X_{\omega_2} \leq 250$ MaxImize Z = 12×1+18×2+2×3+11×4 $X_{c_1} \leq 620, X_{c_2} \leq 280$ S.t. Xc1 + Xc2 + Xc3 > 2 $2x_1 + 3x_2 + 4x_3 + 2x_4 \le 500$ XWI + XWZ + XW3 $\begin{array}{r} 3x_1 + 2X_2 + & X_3 + 2X_4 \leq 380 \\ 7X_1 + 3X_2 + 2X_3 + & X_4 \leq 450 \\ X_1 , X_2 , & X_3 , & X_4 \geq 0 \end{array}$ $2X_{W_1} + 2X_{W_2} + 2X_{W_3} - X_{C_1} - X_{C_2} - X_{C_3} \le 0$ TORA Solution: Xw1 + Xw2 + Xw3 = 1500 $X_1 = 0, X_2 = 133.33, X_3 = 0, X_4 = 50$ $X_{c_1} + X_{c_2} + X_{c_3} \ge 1200$ Z = \$2950 all variables >0 (a) Optimum from TORA: X' = number of units of model j 49 XWI = 550, XW2 = 250, XW3 = 700 Maximize Z = 30×1+20×2+50×3 Xc, = 620, Xc2 = 280, Xc3 = 2100 Subject to Z = #14,918 $2X_1 + 3X_2 + 5X_3 \le 4000$ 0 4×, + 2×2 +7×3 ≤6000 (b) Increasing marginal cost ensures 3 $X_1 + .5 X_2 + \frac{1}{2} X_3 \le 1500$ that regular time capacity is used (4) $\frac{X_1}{3} = \frac{X_2}{3} or 2X_1 - 3X_2 = 0$ before that of overtime, and that overtime capacity is used before that of subcontracting. If the \bigcirc $\frac{X_{2}}{2} = \frac{X_{3}}{2}, \sigma_{1} \leq X_{2} - 2X_{3} = 0$ marginal cost function is not $X_1 \ge 200, X_2 \ge 200, X_3 \ge 150$ monotonically increasing, additional constraints are needed to ensure *** OPTIMUM SOLUTION SUMMARY that the capacity restriction is Title: Problem 2.6e-12 Final iteration No: 6 Objective value (max) =41081.0820 satified. Variable Value Obj Coeff Obj Val Contrib x1 12 12 324.3243 216.2162 30.0000 9729.7305 20,0000 4324.3242 \$40.5405 27027.0273 Constraint RAS Slack(+)/Surplus(+) 4000.0000 6000.0000 1500.0000 0.0000 0.0000 RE7.3875 U-1 390.5405 continued. 2 - 15

X; = Units of peroduct j, j=1, 2 54 y== Unused hours of machine i 7 i=1,2 y= Overtime hours of machine i) i=1,2 Maximize Z = 110 X, +118X2-100 (y+ y+) S.t. $\frac{X_1}{5} + \frac{X_2}{5} + y_1^- - y_1^+ = 8$ $\frac{X_1}{8} + \frac{X_2}{4} + \frac{y^2}{6_2} - \frac{y^4}{6_2} = 8$ $\mathcal{Y}_1^+ \leq 4, \ \mathcal{Y}_2^+ \leq 4$ X,,X2, y, , y, , y-, y+ 20 Solution: Revenue = 6,232 $X_1 = 56$, $y_1^+ = 4$ hrs $X_2 = 4$, $y_2^+ = 0$ 7,7=0 2-17

Let $x_i = Nbr$, starting on day i and lasting for 7 days

 y_{ij} = Nbr. starting shift on day i and starting their 2 days off on day j, $i \neq j$

Thus, of the x_1 workers who start on Monday, y_{12} will take T and W off, y_{13} will take W and Th off, and so on, as the following table shows.

	x _l	<i>x</i> ₂	<i>x</i> ₃	<i>x</i> ₄	xs	<i>x</i> ₆	<i>x</i> ₇
1	(start on Mon	<i>y</i> 12	<i>y</i> 12 ⁺ <i>y</i> 13	y13 ⁺ y14	y14+y15	<i>y</i> 15+ <i>y</i> 16	Y 16
2	y27	Tue	y23	y23+y24	y24+y25	y25+y26	y26+y27
3	y31+y37	y31	Wed	y34	y34+y35	y35+y36	y36+y37
4	y41+y47	y41+y42	y42	Th	y45	y45+y46	y46+y47
5	y51+y57	y51+y52	y 5 2+y53	y53	Fri 🚀	y:56	y:56+y:57
6	y61+y67	y61+y62	y62+y63	y63+y64	y64	Sat 着 👌	y67
7	y71	y71+y72	y72+y73	y73+y74	y74+y75	y75	Su the

Minimize $z = x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7$

Each employee has 2 days off: $x_i = sum{j in 1...7,j\neq i}y_y$ Mon (1) constraint: s -(y27 + y31 + y37 + y41 + y47 + y51 + y57 + y61 + y67 + y71) >= 12Tue (2) constraint: s -(y12 + y31 + y41 + y42 + y51 + y52 + y61 + y62 + y71 + y72) == 18Wed (3) constraint: s -(y12 + y13 + y23 + y42 + y52 + y53 + y62 + y63 + y72 + y73) == 20Th (4) constraint: s -(y13 + y14 + y23 + y24 + y24 + y53 + y63 + y64 + y73 + y74) == 28Fri (5) constraint: s -(y14 + y15 + y24 + y25 + y34 + y35 + y45 + y64 + y74 + y75) == 32Sat(6) constraint: s -(y15 + y16 + y25 + y26 + y35 + y36 + y45 + y46 + y56 + y75) == 40Sun(7) constraint: s -(y16 + y26 + y27 + y36 + y37 + y46 + y47 + y56 + y57 + y67) >= 40

continued

Starting		Nbr off							
On 🕅	Nbr	М	Tu	Wed	Th	Fri	Sat	Sun	
М	16		16	16			in s		
Tu	8	12			8	8			
Wed	8	8	8	1					
Th	0								
Fri	6	23405 V		6	6				
Sat	2	2	54 55	10				2	
Sun	2				_	, 2	2		
Nbr off		10	24	22	14	10	2	2	
Nbr at w	ork	32	18	20	28	32	40	40	
Surplus a minimun	above n	20	0	0	0	0	0	0	
		•							
				,					
				1	i.				

123.5.0

25×5 ≥ 1.3×, +1.2×m+.5×4+1.4×p New land use constraint: 66 $2X_1 + 3X_2 + 4X_3 + X_4 \le .85(800 + 100)$ Optimum: Z = 8290.30 thousand \$ X1 = 100, Xm = 125, Xu = 227.04 New Ophinum Solution: $x_p = 300, x_s = 32.54, x_n = 25$ z=\$3815461.35 $X_c = 0$ X, = 381.54 homes 65 X = Nor. of single - family homes $X_2 = X_3 = 0$ X2= Nbr. of double-family homes X1, = 1.91 areas X3 = Nbr. of triple-family home. X4 = Nbr. of recreation areas DZ = 3,815,461.35-3,391,521.20 = \$423,940.35 Maximize Z = 10,000 X, + 12000 X2 + 15000 X3 DZ < 450,000, the purchasing S.F cost of 100 acres. Hence, the $2x_{1} + 3x_{2} + 4x_{2} + x_{4} \leq \cdot 85 \times 800$ purchase of the new acreage is not recommended. $\frac{X_1}{X_1 + X_2 + X_2} \ge .5 \quad \text{or} \quad .5X_1 - .5X_2 - .5X_3 \ge 0$ $X_4 \ge \frac{X_1 + 2X_3 + 3X_3}{2\pi 0}$ or $200X_9 - X_1 - 2X_2 - 3X_3 \ge 0$ 1800X, +1200X,+1400X,+800X4 ≥ 100,000 400 X, + 600 X2 + 840 X3 + 450 X4 5 200,000 $X_1, X_2, X_7, X_4 \ge 0$ Optimum solution : X = 339.15 homes $X_{1} = 0$ $x_{3} = 0$ Xu = 1.69 areas z = \$3391521.20 2-22

$$\begin{array}{c|c} x_{3} = tons & f & grapes / day, \\ x_{3} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{4} = tons & f & grapes / day, \\ x_{5} = 16 & g & donik & B / day, \\ x_{5} = 16 & g & strauberg, used in donik & B / day, \\ x_{5} = 16 & g & strauberg, used in donik & B / day, \\ x_{5} = 16 & g & strauberg, used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = 16 & g & strause used in donik & B / day, \\ x_{6} = x_{6} + x$$

5.1. Y = 5x2000 = 10,000 $X_{AI} = X_{AI}, X_{AI} = SX_{AI}, X_{AI} = SX_{DI}$ Y2 = 2x2000 = 4,000 Y = 1x2000 = 2,000 $X_{A2} = X_{B2}, X_{A2} = 2X_{C2}, X_{A2} = \frac{2}{3}X_{D2}$ Y < 1 × 2000 = 2,000 YA = 1000, YB = 1200, Y = 900, Y = 1500 $X_{OA} = \frac{50}{5} X_{FA}, X_{OA} = \frac{50}{2} X_{AA}$ F. 2 200, F. 2 400 Optimum delution : Z = \$ 495, 416.67 $X_{0B} = \frac{60}{2} X_{CB}, X_{B} = \frac{60}{3} X_{B}$ YA = 958.33 bb1/day $X_{0C} = \frac{60}{3} X_{C}, X_{0C} = \frac{60}{4} X_{C}, X_{0C} = \frac{60}{2} X_{C}$ Y = 958.33 661 / day all variables are nonnegative. Y = 516.67 661/day Optimum Solution: Z = \$ 5384.84 / day Yn = 1500 bbl / day Wa = 2500 lb or 500 boxes/day F1 = 200 161/day Wa = 3000 lb or 600 boxes F. = 3733.33 661/day W = 5793.4516 or ~ 1158 boxes X = 10,000 16 or 5 tons / day A = bbl of crude A / day X = 471.1916 or 236 ton B = 661 of crude B / day X = 428.16 16 or · 214 ton R= 661 of regular gasoline / day Xa = 394.11 16 or .197 ton P- bbl of premum gasoline / day $X_{ai} = bb1 \quad \text{J} \text{ gasdine A in fuel i} \qquad 71$ $X_{Bi} = bb1 \quad \text{G} \text{ gasoline B in fuel i} \qquad i = 1, 2$ $X_{ai} = bb1 \quad \text{G} \text{ gasoline C in fuel i} \qquad i = 1, 2$ $Ci \qquad 1 \quad \text{Or } 1 \quad \text{Or } 1$ 70 J = bbl of jet gasoline / day Maximize $Z = 50(R - R^{\dagger}) + 70(P - P^{\dagger})$ + 120(J-J+)-(10R+15P+20J) $-(2R^{+}+3P^{+}+4T^{+})-(30A+40B)$ X = 661 of gasoline D in fuel i 5.E. A < 2500, B < 3000 R=. 2A+. 25B, R+R-R= 500 $Y_{o} = X_{AI} + X_{AZ}$ $P_{\pm} \cdot |A + \cdot 3B, P + p^{-} - p^{+} = 700$ $J_{\pm} \cdot 2SA + \cdot 1B, J + J^{-} J^{+} = 400$ YR = XRI + XBZ $Y_c = X_{c1} + X_{c2}$ All variables = 0 $Y_{D} = X_{DI} + X_{DZ}$ Optimum dolution : $F_{i} = X_{Ai} + X_{Bi} + X_{ci} + X_{Di}$ Z = \$21,852.94 A=1176.47 661/day $F_{3} = X_{A2} + X_{B2} + X_{C2} + X_{D2}$ B= 1058.82 661/day Maximize Z= 200 F1 + 250 F2 R=500 661/day P=435.29 661/day - (120 / +90 / +100 / +150 /) T = 400 661/day continued.

S= tons of steel scrap / day 75 76 A = tono J. alum. scrap / day Xij = tons of one i allocated to alloy & Whe = tons of alloy & produced C = tons of Cast iron scrap / day Ab = tono of alum. briquettes / day MAXIMIZE Z = 200 WA + 300 WB Sb = tono silicon briguettes / day - 30 (XIA+ XIB) a = tons of alum. I day g = tone of graphite / day $-40(X_{2A}+X_{2B})$ $-50(X_{2D}+X_{3P})$ I = tone of Eilicon / day aI = tons of alum in ingot I / day Subject to a II = tons falum. in ingot I / day Specification constraints: gI - tons of graphite in mgot I / day · 2 X1A + · 1 X2A + · 05 X3A ≤ · 8 WA () gII = tone of graphite in mast II /day SI = tone of Silion in ingst I /day SII = tone of Silion in ingst I /day · 1 X1A + · 2 X2A + · 05 X3A ≤ ·3 WA (2) · 3 X1A + 3 X2A + 2 X3A = 5 WA 3 I, = tons of night I / day $\cdot 1 \times_{1B} + \cdot 2 \times_{2R} + \cdot 05 \times_{3B} \ge \cdot 4 W_{B} (4)$ Iz= tons of ingot II / day. ·1×1B + · 2 ×2B + · 05 ×3B ≤ .6 WBG Minimize Z = 100 S+150 A+75 C+900 A6+380 S6 ·3 X18 + · 3 X18 + · 7 X38 = · 3 WR 6 S.J. SE 1000, AE 500, CE2500 $\cdot 3 \times_{18} + \cdot 3 \times_{28} + \cdot 2 \times_{38} \leq \cdot 7 W_{R}(7)$ a = .1S + .95A + AbOhe constraints. 9 = .05 S +. 01 A +. 15 C 3 = . 14 S +. 02 A +. 08 C + SL XIA + XIR = 1000 I,= 9I+JI+&I Iz=9II+JI+&I X2A + X28 5 2000 91 + 97 5× , SI+81 ≤ 8, gI+gI ≤ g X3A + K3B 5 3000 $\begin{array}{l} \cdot 0 & \mathcal{B} & \mathcal{I} \\ \cdot & \mathcal{O} & \mathcal{B} & \mathcal{I} \\ \cdot & \mathcal{O} & \mathcal{I} & \mathcal{I} \\ \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{I} \\ \cdot & \mathcal{O} & \mathcal{I} \\ \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{I} \\ \cdot & \mathcal{O} & \mathcal{I} \\ \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{I} \\ \cdot & \mathcal{O} & \mathcal{I} \\ \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \end{array} \begin{array}{l} \cdot & \mathcal{O} & \mathcal{O} \\ \end{array} \end{array}$ UTION SIMILARY +--Title: Problem 26a Final Iteration No: ·0251, ≤ 81 < 00 Objective value (#81) =40 $\cdot \sigma f_2 I_2 \leq a I \leq \cdot \sigma g g I_2$ fer i sbl e Value Obj Val Contrib $\cdot \circ 4/I_2 \leq gII \leq a$ $\cdot \circ 28I_2 \leq gII \leq \cdot \circ 4/I_2$ 200.0000 1000.0001 x3 x1/ 00000.0312 1000.0000 30000.0000 30.000 x5 x2A x6 x28 I,≥130, I2≥250 40.0000 60.000 27 234 10.10 0.0000 Optimum solution : Constraint Elack(-)/Surp 1 (4) 7 = \$ 117.435.65 S=0, A=38.2, C= 1489.41 DODO 9 («) 10 («) Ab = Sb = 0I,= 130, I2=250 Solution: a = 36.29, g = 223.79, d= 119.92 Produce 1800 tons of alloy A and 1000 tons of alloy B.

Xi = Nbr. of ads for issue i, i= 1,2,3,4 78 Minimize $Z = S_{1}^{-} + S_{1}^{-} + S_{3}^{-} + S_{4}^{-}$ S.F. (-30,000+6,0000+30,000)X1+5,-5,=.51×400,000 (10,000+30,000-45,000)X2+5-5t=.51×400,000 (40,000+10,000)X3+5-5t=.51×400,000 (90,000 - 25,000) ×4 + 54 - 54 = .51 × 400,000 $1500(X_1 + X_2 + X_2 + X_4) \le 100,000$ $X_1, X_2, X_3, X_4 \ge 0$ Solution ; $X_1 = 3.4$, $X_2 = 3.14$, $X_3 = 4.08$, $X_9 = 3.14$ X = Units of part i produced by is department i, i=1,2 j=1,2,3 $Maximize Z = \min \{ X_{11} + X_{21}, X_{12} + X_{22}, X_{13} + X_{23} \}$ or Maximize Z = 7 S.t. $\gamma \leq \chi_1 + \chi_2$ 7 = X12 + X22 A ≤ X13 + X23 $\frac{\chi_{11}}{x} + \frac{\chi_{12}}{z} + \frac{\chi_{13}}{10} \le 100$ $\frac{X_{21}}{6} + \frac{X_{12}}{12} + \frac{X_{23}}{4} \le 80$ all XIII 20 Solution: Nbr. of assembly units = y = 556.2 ~ 557 X:= Space (in2) allocated to cereal c $x_{11} = 354.78$, $x_{21} = 2.01.79$ 77 $x_{12} = 0$, $x_{21} = 556.52$ $x_{13} = 556.52$, $x_{23} = 0$ MaxImize z=1.1x,+1.3x,+1.08x3+1.25x+1.2x5 s.t. . 16×,+24×2+18×3+22×4+20×5 ≤ 5000 Xi= tons of coal is i= 1,2,3 80 $X_1 \leq 10^{0}, X_2 \leq 85, X_3 \leq 140, X_y \leq 80, X_5 \leq 90$ $Minimize \ z = 30X_1 + 35X_2 + 33X_2$ S.F. 2500 X1 + 1500 X2 + 1600 X3 ≤ 2000 (X1 + X2 + X3) X1 ≤ 30, X2 ≤ 30, X3 ≤ 30 X; 20 for all i= 1,2, ..., 5 <u>Solution</u>: Z = \$ 314 / day $X_1 + X_2 + X_3 \geq 50$ Solution: Z= \$1361.11 $X_{3} = 100, X_{3} = 140, X_{5} = 44$ X, = 27.22 tono, X2 = 0, X3 = 27.78 tons. $X_{2} = X_{2} = 0$ 2-27

