Mechanics of Materials SI 9th Edition Hibbeler Solutions Manual Full Download: https://www.initenter.com/initenter

2-1 The center portion of the rubber balloon has a diameter of d = 100 mm. If the air pressure within it causes the balloon's diameter to become d = 125 mm, determine the average normal strain in the rubber.

Given: $d_0 := 100$ mm d := 125mm

mm

Solution:

$$\varepsilon := \frac{\pi d - \pi d_0}{\pi d_0}$$
$$\varepsilon = 0.2500 \frac{mm}{mm}$$

Ans



Ans: $\epsilon_{CE} = 0.00250 \text{ mm/mm}, \epsilon_{BD} = 0.00107 \text{ mm/mm}$

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2–2. A thin strip of rubber has an unstretched length of 375 mm. If it is stretched around a pipe having an outer diameter of 125 mm, determine the average normal strain in the strip.

 $L_0 = 375 \text{ mm}$

 $L = \pi(125 \text{ mm})$

 $\varepsilon = \frac{L - L_0}{L_0} = \frac{125\pi - 375}{375} = 0.0472 \text{ mm/mm}$

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2-3. The rigid beam is supported by a pin at A and wires BD and CE. If the load **P** on the beam causes the end C to be displaced 10 mm downward, determine the normal strain developed in wires CE and BD.



$$\frac{\Delta L_{BD}}{3} = \frac{\Delta L_{CE}}{7}$$
$$\Delta L_{BD} = \frac{3 (10)}{7} = 4.286 \text{ mm}$$
$$\epsilon_{CE} = \frac{\Delta L_{CE}}{L} = \frac{10}{4000} = 0.00250 \text{ mm/mm}$$
$$\epsilon_{BD} = \frac{\Delta L_{BD}}{L} = \frac{4.286}{4000} = 0.00107 \text{ mm/mm}$$

Ans: $\epsilon_{CE} = 0.00250 \text{ mm/mm}, \epsilon_{BD} = 0.00107 \text{ mm/mm}$

Ans.

*2-4. The force applied at the handle of the rigid lever causes the lever to rotate clockwise about the pin *B* through an angle of 2° . Determine the average normal strain developed in each wire. The wires are unstretched when the lever is in the horizontal position.



Geometry: The lever arm rotates through an angle of $\theta = \left(\frac{2^{\circ}}{180}\right)\pi$ rad = 0.03491 rad. Since θ is small, the displacements of points *A*, *C*, and *D* can be approximated by

> $\delta_A = 200(0.03491) = 6.9813 \text{ mm}$ $\delta_C = 300(0.03491) = 10.4720 \text{ mm}$

 $\delta_D = 500(0.03491) = 17.4533 \text{ mm}$

Average Normal Strain: The unstretched length of wires AH, CG, and DF are

$$L_{AH} = 200 \text{ mm}, L_{CG} = 300 \text{ mm}, \text{ and } L_{DF} = 300 \text{ mm}.$$
 We obtain

$$(\epsilon_{avg})_{AH} = \frac{\delta_A}{L_{AH}} = \frac{6.9813}{200} = 0.0349 \text{ mm/mm}$$
 Ans.
 $(\epsilon_{avg})_{CG} = \frac{\delta_C}{L_{CG}} = \frac{10.4720}{300} = 0.0349 \text{ mm/mm}$ Ans.

$$(\epsilon_{\text{avg}})_{DF} = \frac{\delta_D}{L_{DF}} = \frac{17.4533}{300} = 0.0582 \text{ mm/mm}$$
 Ans.



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2–5. The two wires are connected together at A. If the force **P** causes point A to be displaced horizontally 2 mm, determine the normal strain developed in each wire.



$$L'_{AC} = \sqrt{300^2 + 2^2 - 2(300)(2)\cos 150^\circ} = 301.734 \text{ mm}$$

 $\epsilon_{AC} = \epsilon_{AB} = \frac{L'_{AC} - L_{AC}}{L_{AC}} = \frac{301.734 - 300}{300} = 0.00578 \text{ mm/mm}$

Ans.

300mm ISDO

Ans: $\epsilon_{AC} = \epsilon_{AB} = 0.00578 \text{ mm/mm}$ **2–6.** The rubber band of unstretched length $2r_0$ is forced down the frustum of the cone. Determine the average normal strain in the band as a function of z.

Geometry: Using similar triangles shown in Fig. *a*,

$$\frac{h'}{r_0} = \frac{h'+h}{2r_0}; \quad h'=h$$

Subsequently, using the result of h'

$$\frac{r}{z+h} = \frac{r_0}{h}; \qquad r = \frac{r_0}{h} (z+h)$$

Average Normal Strain: The length of the rubber band as a function of z is $L = 2\pi r = \frac{2\pi r_0}{h} (z+h)$. With $L_0 = 2r_0$, we have

$$\epsilon_{\text{avg}} = \frac{L - L_0}{L_0} = \frac{\frac{2\pi r_0}{h}(z+h) - 2r_0}{2r_0} = \frac{\pi}{h}(z+h) - 1$$
 Ans.





Ans:

$$\epsilon_{\rm avg} = \frac{\pi}{h} \left(z + h \right) - 1$$

2-7. The pin-connected rigid rods *AB* and *BC* are inclined at $\theta = 30^{\circ}$ when they are unloaded. When the force **P** is applied θ becomes 30.2°. Determine the average normal strain developed in wire *AC*.

Geometry: Referring to Fig. *a*, the unstretched and stretched lengths of wire *AD* are

 $L_{AC} = 2(600 \sin 30^\circ) = 600 \text{ mm}$

 $L_{AC'} = 2(600 \sin 30.2^\circ) = 603.6239 \,\mathrm{mm}$

Average Normal Strain:

$$(\epsilon_{\text{avg}})_{AC} = \frac{L_{AC'} - L_{AC}}{L_{AC}} = \frac{603.6239 - 600}{600} = 6.04(10^{-3}) \,\text{mm/mm}$$
 Ans.



(a)



*2-8. Part of a control linkage for an airplane consists of a rigid member *CBD* and a flexible cable *AB*. If a force is applied to the end *D* of the member and causes it to rotate by $\theta = 0.3^{\circ}$, determine the normal strain in the cable. Originally the cable is unstretched.



$$AB = \sqrt{400^2 + 300^2} = 500 \text{ mm}$$

$$AB' = \sqrt{400^2 + 300^2 - 2(400)(300) \cos 90.3^\circ}$$

$$= 501.255 \text{ mm}$$

$$\epsilon_{AB} = \frac{AB' - AB}{AB} = \frac{501.255 - 500}{500}$$

$$= 0.00251 \text{ mm/mm}$$



2-9. Part of a control linkage for an airplane consists of a rigid member *CBD* and a flexible cable *AB*. If a force is applied to the end *D* of the member and causes a normal strain in the cable of 0.0035 mm/mm, determine the displacement of point *D*. Originally the cable is unstretched.



$$AB = \sqrt{300^2 + 400^2} = 500 \text{ mm}$$

$$AB' = AB + \varepsilon_{AB}AB$$

$$= 500 + 0.0035(500) = 501.75 \text{ mm}$$

$$501.75^2 = 300^2 + 400^2 - 2(300)(400) \cos \alpha$$

$$\alpha = 90.4185^{\circ}$$

$$\theta = 90.4185^{\circ} - 90^{\circ} = 0.4185^{\circ} = \frac{\pi}{180^{\circ}} (0.4185) \text{ rad}$$

$$\Delta_D = 600(\theta) = 600(\frac{\pi}{180^\circ})(0.4185) = 4.38 \text{ mm}$$



v 2-10. The corners of the square plate are given the displacements indicated. Determine the shear strain along the edges of the plate at A and B. 16 mm В 3 mm 3 mm |16 mm С 16 mm 16 mm At A: $\frac{\theta'}{2} = \tan^{-1}\left(\frac{9.7}{10.2}\right) = 43.561^{\circ}$ $\theta' = 1.52056 \text{ rad}$ ní 10,210. $(\gamma_A)_{nt} = \frac{\pi}{2} - 1.52056$ 3.7 in. = 0.0502 rad Ans. At *B*: $\frac{\phi'}{2} = \tan^{-1}\left(\frac{10.2}{9.7}\right) = 46.439^{\circ}$ $\phi' = 1.62104 \text{ rad}$ $(\gamma_B)_{nt} = \frac{\pi}{2} - 1.62104$ 10.210 = -0.0502 rad Ans. 4.710 Ans: $(\gamma_A)_{nt} = 0.0502 \text{ rad}, (\gamma_B)_{nt} = -0.0502 \text{ rad}$

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Ans: $\epsilon_{DB} = \epsilon_{AB} \cos^2 \theta + \epsilon_{CB} \sin^2 \theta$ **2–14.** The force **P** applied at joint D of the square frame causes the frame to sway and form the dashed rhombus. Determine the average normal strain developed in wire AC. Assume the three rods are rigid.



Geometry: Referring to Fig. *a*, the stretched length of $L_{AC'}$ of wire AC' can be determined using the cosine law.

$$L_{AC'} = \sqrt{400^2 + 400^2 - 2(400)(400)\cos 93^\circ} = 580.30 \text{ mm}$$

The unstretched length of wire AC is

$$L_{AC} = \sqrt{400^2 + 400^2} = 565.69 \,\mathrm{mm}$$

Average Normal Strain:

$$(\epsilon_{\text{avg}})_{AC} = \frac{L_{AC'} - L_{AC}}{L_{AC}} = \frac{580.30 - 565.69}{565.69} = 0.0258 \text{ mm/mm}$$
 Ans.





2-15. The force **P** applied at joint D of the square frame causes the frame to sway and form the dashed rhombus. Determine the average normal strain developed in wire AE. Assume the three rods are rigid.



Geometry: Referring to Fig. *a*, the stretched length of $L_{AE'}$ of wire AE can be determined using the cosine law.

$$L_{AE'} = \sqrt{400^2 + 200^2 - 2(400)(200)} \cos 93^\circ = 456.48 \text{ mm}$$

The unstretched length of wire AE is

$$L_{AE} = \sqrt{400^2 + 200^2} = 447.21 \text{ mm}$$

Average Normal Strain:

$$(\epsilon_{\text{avg}})_{AE} = \frac{L_{AE'} - L_{AE}}{L_{AE}} = \frac{456.48 - 447.21}{447.21} = 0.0207 \text{ mm/mm}$$
 Ans.



*2-16. The triangular plate *ABC* is deformed into the shape shown by the dashed lines. If at *A*, $\varepsilon_{AB} = 0.0075$, $\epsilon_{AC} = 0.01$ and $\gamma_{xy} = 0.005$ rad, determine the average normal strain along edge *BC*.



Average Normal Strain: The stretched length of sides AB and AC are

$$L_{AC'} = (1 + \varepsilon_y)L_{AC} = (1 + 0.01)(300) = 303 \text{ mm}$$
$$L_{AB'} = (1 + \varepsilon_x)L_{AB} = (1 + 0.0075)(400) = 403 \text{ mm}$$

Also,

$$\theta = \frac{\pi}{2} - 0.005 = 1.5658 \operatorname{rad}\left(\frac{180^{\circ}}{\pi \operatorname{rad}}\right) = 89.7135^{\circ}$$

The unstretched length of edge BC is

$$L_{BC} = \sqrt{300^2 + 400^2} = 500 \,\mathrm{mm}$$

and the stretched length of this edge is

$$L_{B'C'} = \sqrt{303^2 + 403^2 - 2(303)(403)\cos 89.7135^\circ}$$

= 502.9880 mm

We obtain,

$$\epsilon_{BC} = \frac{L_{B'C'} - L_{BC}}{L_{BC}} = \frac{502.9880 - 500}{500} = 5.98(10^{-3}) \text{ mm/mm}$$
 Ans.



2–17. The plate is deformed uniformly into the shape shown by the dashed lines. If at A, $\gamma_{xy} = 0.0075$ rad., while $\epsilon_{AB} = \epsilon_{AF} = 0$, determine the average shear strain at point *G* with respect to the x' and y' axes.



Geometry: Here, $\gamma_{xy} = 0.0075 \operatorname{rad}\left(\frac{180^{\circ}}{\pi \operatorname{rad}}\right) = 0.4297^{\circ}$. Thus, $\psi = 90^{\circ} - 0.4297^{\circ} = 89.5703^{\circ}$ $\beta = 90^{\circ} + 0.4297^{\circ} = 90.4297^{\circ}$

Subsequently, applying the cosine law to triangles AGF' and GBC', Fig. a,

$$L_{GF'} = \sqrt{600^2 + 300^2 - 2(600)(300)} \cos 89.5703^\circ = 668.8049 \text{ mm}$$

$$L_{GC'} = \sqrt{600^2 + 300^2 - 2(600)(300)} \cos 90.4297^\circ = 672.8298 \text{ mm}$$

Then, applying the sine law to the same triangles,

$$\frac{\sin \phi}{600} = \frac{\sin 89.5703^{\circ}}{668.8049}; \qquad \phi = 63.7791^{\circ}$$
$$\frac{\sin \alpha}{300} = \frac{\sin 90.4297^{\circ}}{672.8298}; \qquad \alpha = 26.4787^{\circ}$$

Thus,

$$\theta = 180^{\circ} - \phi - \alpha = 180^{\circ} - 63.7791^{\circ} - 26.4787^{\circ}$$
$$= 89.7422^{\circ} \left(\frac{\pi \operatorname{rad}}{180^{\circ}}\right) = 1.5663 \operatorname{rad}$$

Shear Strain:

$$(\gamma_G)_{x'y'} = \frac{\pi}{2} - \theta = \frac{\pi}{2} - 1.5663 = 4.50(10^{-3}) \text{ rad}$$
 Ans.



Ans: $(\gamma_G)_{x'y'} = 4.50(10^{-3})$ rad **2–18.** The piece of plastic is originally rectangular. Determine the shear strain γ_{xy} at corners A and B if the plastic distorts as shown by the dashed lines.

v 5 mm 2 mm 4 mm B 2 mm 0 300 mm 2 mm DΑ 400 mm 3 mm 300 400 mm

> Ans: $(\gamma_B)_{xy} = 11.6(10^{-3})$ rad, $(\gamma_A)_{xy} = 11.6(10^{-3})$ rad

Geometry: For small angles,

$$\alpha = \psi = \frac{2}{302} = 0.00662252 \text{ rad}$$

 $\beta = \theta = \frac{2}{403} = 0.00496278 \text{ rad}$

Shear Strain:

$$(\gamma_B)_{xy} = \alpha + \beta$$

= 0.0116 rad = 11.6(10⁻³) rad
 $(\gamma_A)_{xy} = \theta + \psi$
= 0.0116 rad = 11.6(10⁻³) rad

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Ans.

2-19. The piece of plastic is originally rectangular. Determine the shear strain γ_{xy} at corners D and C if the 5 mm plastic distorts as shown by the dashed lines. 2 mm 2 mm (300 mm DA 400 mm 3 mm Geometry: For small angles, $\alpha = \psi = \frac{2}{403} = 0.00496278$ rad $\beta = \theta = \frac{2}{302} = 0.00662252$ rad **Shear Strain:** $(\gamma_C)_{xy} = \alpha + \beta$ $= 0.0116 \text{ rad} = 11.6(10^{-3}) \text{ rad}$ Ans. $(\gamma_D)_{xy} = \theta + \psi$ $= 0.0116 \text{ rad} = 11.6(10^{-3}) \text{ rad}$ Ans.

> Ans: $(\gamma_C)_{xy} = 11.6(10^{-3}) \text{ rad},$ $(\gamma_D)_{xy} = 11.6(10^{-3}) \text{ rad}$

4 mm

‡2 mm

В

*2–20. The piece of plastic is originally rectangular. Determine the average normal strain that occurs along the diagonals AC and DB.



Geometry:

 $AC = DB = \sqrt{400^2 + 300^2} = 500 \text{ mm}$ $DB' = \sqrt{405^2 + 304^2} = 506.4 \text{ mm}$ $A'C' = \sqrt{401^2 + 300^2} = 500.8 \text{ mm}$

Average Normal Strain:

$$\epsilon_{AC} = \frac{A'C' - AC}{AC} = \frac{500.8 - 500}{500}$$

= 0.00160 mm/mm = 1.60(10⁻³) mm/mm
$$\epsilon_{DB} = \frac{DB' - DB}{DB} = \frac{506.4 - 500}{500}$$

= 0.0128 mm/mm = 12.8(10⁻³) mm/mm

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Ans.

,5 mm

400 mm

5 mm

В

300 mm

Α

2–21. The rectangular plate is deformed into the shape of a parallelogram shown by the dashed lines. Determine the average shear strain γ_{xy} at corners *A* and *B*.

Geometry: Referring to Fig. a and using small angle analysis,

$$\theta = \frac{5}{300} = 0.01667 \text{ rad}$$

 $\phi = \frac{5}{400} = 0.0125 \text{ rad}$

Shear Strain: Referring to Fig. a,

$$(\gamma_A)_{xy} = \theta + \phi = 0.01667 + 0.0125 = 0.0292 \text{ rad}$$
 Ans.
 $(\gamma_B)_{xy} = \theta + \phi = 0.01667 + 0.0125 = 0.0292 \text{ rad}$ Ans.



Ans: $(\gamma_A)_{xy} = 0.0292 \text{ rad}, (\gamma_B)_{xy} = 0.0292 \text{ rad}$

2-22. The triangular plate is fixed at its base, and its apex *A* is given a horizontal displacement of 5 mm. Determine the shear strain, γ_{xy} , at *A*.



 $L = \sqrt{800^2 + 5^2 - 2(800)(5)\cos 135^\circ} = 803.54 \text{ mm}$

 $\frac{\sin 135^{\circ}}{803.54} = \frac{\sin \theta}{800}; \qquad \theta = 44.75^{\circ} = 0.7810 \text{ rad}$

$$\gamma_{xy} = \frac{\pi}{2} - 2\theta = \frac{\pi}{2} - 2(0.7810)$$

= 0.00880 rad

Ans.

Ans: $\gamma_{xy} = 0.00880$ rad **2–23.** The triangular plate is fixed at its base, and its apex A is given a horizontal displacement of 5 mm. Determine the average normal strain ϵ_x along the x axis.



 $L = \sqrt{800^2 + 5^2 - 2(800)(5) \cos 135^\circ} = 803.54 \text{ mm}$ $\epsilon_x = \frac{803.54 - 800}{800} = 0.00443 \text{ mm/mm}$

Ans.

Ans: $\epsilon_x = 0.00443 \text{ mm/mm}$ *2–24. The triangular plate is fixed at its base, and its apex A is given a horizontal displacement of 5 mm. Determine the average normal strain $\epsilon_{x'}$ along the x' axis.



$$\epsilon_{x'} = \frac{5}{565.69} = 0.00884 \text{ mm/mm}$$

Ans.

800 mm

A′ ≂5 mm

45°

45

800 mm

45

x'

2-25. The square rubber block is subjected to a shear strain of $\gamma_{xy} = 40(10^{-6})x + 20(10^{-6})y$, where x and y are in mm. This deformation is in the shape shown by the dashed lines, where all the lines parallel to the y axis remain vertical after the deformation. Determine the normal strain along edge *BC*.

Shear Strain: Along edge *DC*, y = 400 mm. Thus, $(\gamma_{xy})_{DC} = 40(10^{-6})x + 0.008$. Here, $\frac{dy}{dx} = \tan(\gamma_{xy})_{DC} = \tan[40(10^{-6})x + 0.008]$. Then,

$$\int_{0}^{\delta_{c}} dy = \int_{0}^{300 \text{ mm}} \tan[40(10^{-6})x + 0.008] dx$$
$$\delta_{c} = -\frac{1}{40(10^{-6})} \left\{ \ln \cos \left[40(10^{-6})x + 0.008 \right] \right\} \Big|_{0}^{300 \text{ mm}}$$
$$= 4.2003 \text{ mm}$$

Along edge *AB*, y = 0. Thus, $(\gamma_{xy})_{AB} = 40(10^{-6})x$. Here, $\frac{dy}{dx} = \tan(\gamma_{xy})_{AB} = \tan[40(10^{-6})x]$. Then,

$$\int_{0}^{\delta_{B}} dy = \int_{0}^{300 \text{ mm}} \tan\left[40(10^{-6})x\right] dx$$
$$\delta_{B} = -\frac{1}{40(10^{-6})} \left\{\ln\cos\left[40(10^{-6})x\right]\right\} \Big|_{0}^{300 \text{ mm}}$$
$$= 1.8000 \text{ mm}$$

Average Normal Strain: The stretched length of edge BC is

$$L_{B'C'} = 400 + 4.2003 - 1.8000 = 402.4003 \,\mathrm{mm}$$

We obtain,

$$(\epsilon_{\text{avg}})_{BC} = \frac{L_{B'C'} - L_{BC}}{L_{BC}} = \frac{402.4003 - 400}{400} = 6.00(10^{-3}) \text{ mm/mm}$$
 Ans.





Ans: $(\epsilon_{\text{avg}})_{BC} = 6.00(10^{-3}) \text{ mm/mm}$

2-26. The Polysulfone block is glued at its top and bottom to the rigid plates. If a tangential force, applied to the top plate, causes the material to deform so that its sides are described by the equation $y = 3.56x^{1/4}$, determine the shear strain in the material at its corners A and B.



Prob. 2-33

$$y = 3.56 x^{1/4}$$
$$\frac{dy}{dx} = 0.890 x^{-3/4}$$
$$\frac{dx}{dy} = 1.123 x^{3/4}$$

AtA, x=0

$$\gamma_A = \frac{dx}{dy} = 0$$
 Ans

At B,

 $2 = 3.56 x^{1/4}$ x = 0.0996 mm

$$\gamma_B = \frac{dx}{dy} = 1.123(0.0996)^{3/4} = 0.199 \text{ rad}$$
 Ans

Ans: $(\epsilon_{avg})_{CA} = -5.59(10^{-3}) \text{ mm/mm}$ **2-27.** The square plate *ABCD* is deformed into the shape shown by the dashed lines. If *DC* has a normal strain $\epsilon_x = 0.004$, *DA* has a normal strain $\epsilon_y = 0.005$ and at *D*, $\gamma_{xy} = 0.02$ rad, determine the shear strain at point *E* with respect to the x' and y' axes.

Average Normal Strain: The stretched length of sides DC and BC are

$$L_{DC'} = (1 + \epsilon_x)L_{DC} = (1 + 0.004)(600) = 602.4 \text{ mm}$$
$$L_{B'C'} = (1 + \epsilon_y)L_{BC} = (1 + 0.005)(600) = 603 \text{ mm}$$

Also,

$$\alpha = \frac{\pi}{2} - 0.02 = 1.5508 \operatorname{rad}\left(\frac{180^{\circ}}{\pi \operatorname{rad}}\right) = 88.854^{\circ}$$
$$\phi = \frac{\pi}{2} + 0.02 = 1.5908 \operatorname{rad}\left(\frac{180^{\circ}}{\pi \operatorname{rad}}\right) = 91.146^{\circ}$$

Thus, the length of C'A' and DB' can be determined using the cosine law with reference to Fig. *a*.

$$L_{C'A'} = \sqrt{602.4^2 + 603^2 - 2(602.4)(603)\cos 88.854^\circ} = 843.7807 \text{ mm}$$

$$L_{DB'} = \sqrt{602.4^2 + 603^2 - 2(602.4)(603)\cos 91.146^\circ} = 860.8273 \text{ mm}$$

Thus,

$$L_{E'A'} = \frac{L_{C'A'}}{2} = 421.8903 \text{ mm}$$
 $L_{E'B'} = \frac{L_{DB'}}{2} = 430.4137 \text{ mm}$

Using this result and applying the cosine law to the triangle A'E'B', Fig. a,

$$602.4^{2} = 421.8903^{2} + 430.4137^{2} - 2(421.8903)(430.4137)\cos^{2}\theta = 89.9429^{\circ}\left(\frac{\pi \operatorname{rad}}{180^{\circ}}\right) = 1.5698 \operatorname{rad}$$

Shear Strain:

$$(\gamma_E)_{x'y'} = \frac{\pi}{2} - \theta = \frac{\pi}{2} - 1.5698 = 0.996(10^{-3}) \text{ rad}$$
 Ans.





Ans: $(\gamma_E)_{x'y'} = 0.996(10^{-3})$ rad

 $\boldsymbol{\theta}$

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*2-28. The wire is subjected to a normal strain that is defined by $\epsilon = (x/L)e^{-(x/L)^2}$. If the wire has an initial length *L*, determine the increase in its length.

1	$\epsilon = (x/L)e^{-(x/L)^2}$
x	x
· ا	L

$$\Delta L = \frac{1}{L} \int_0^L x e^{-(x/L)^2} dx$$
$$= -L \left[\frac{e^{-(x/L)^2}}{2} \right]_0^L = \frac{L}{2} [1 - (1/e)]$$
$$= \frac{L}{2e} [e - 1]$$





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2–29.

Ans:

 $(\epsilon_{\text{avg}})_{AC} = 0.0168 \text{ mm/mm},$ $(\gamma_A)_{xy} = 0.0116 \text{ rad}$ **2-30.** The rectangular plate is deformed into the shape shown by the dashed lines. Determine the average normal strain along diagonal BD, and the average shear strain at corner B.



Geometry: The unstretched length of diagonal *BD* is

$$L_{BD} = \sqrt{300^2 + 400^2} = 500 \,\mathrm{mm}$$

Referring to Fig. a, the stretched length of diagonal BD is

$$L_{B'D'} = \sqrt{(300 + 2 - 2)^2 + (400 + 3 - 2)^2} = 500.8004 \text{ mm}$$

Referring to Fig. a and using small angle analysis,

$$\phi = \frac{2}{403} = 0.004963 \text{ rad}$$
$$\alpha = \frac{3}{300 + 6 - 2} = 0.009868 \text{ rad}$$

Average Normal Strain: Applying Eq. 2,

$$(\epsilon_{\text{avg}})_{BD} = \frac{L_{B'D'} - L_{BD}}{L_{BD}} = \frac{500.8004 - 500}{500} = 1.60(10^{-3}) \text{ mm/mm}$$
 Ans.

Shear Strain: Referring to Fig. a,

$$(\gamma_B)_{xy} = \phi + \alpha = 0.004963 + 0.009868 = 0.0148$$
 rad Ans.



Ans: $(\epsilon_{avg})_{BD} = 1.60(10^{-3}) \text{ mm/mm},$ $(\gamma_B)_{xy} = 0.0148 \text{ rad}$

2–31. The nonuniform loading causes a normal strain in the shaft that can be expressed as $\epsilon_x = kx^2$, where <i>k</i> is a constant. Determine the displacement of the end <i>B</i> . Also, what is the average normal strain in the rod?	A	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$
$\frac{d(\Delta x)}{dx} = \epsilon_x = kx^2$ $(\Delta x)_B = \int_0^L kx^2 = \frac{kL^3}{3}$ $(\epsilon_x)_{avg} = \frac{(\Delta x)_B}{L} = \frac{\frac{kL^3}{3}}{L} = \frac{kL^2}{3}$	Ans. Ans.	
		Ans: $(\Delta x)_B = \frac{kL^3}{3}, (\epsilon_x)_{avg} = \frac{kL^2}{3}$

*2-32 The rubber block is fixed along edge *AB*, and edge *CD* is moved so that the vertical displacement of any point in the block is given by $v(x) = (v_0/b^3)x^3$. Determine the shear strain γ_{xy} at points (b/2, a/2) and (b, a).

Shear Strain: From Fig. a,

$$\frac{dv}{dx} = \tan \gamma_{xy}$$
$$\frac{3v_0}{b^3}x^2 = \tan \gamma_{xy}$$
$$\gamma_{xy} = \tan^{-1}\left(\frac{3v_0}{b^3}x^2\right)$$

Thus, at point (b/2, a/2),

$$\gamma_{xy} = \tan^{-1} \left[\frac{3v_0}{b^3} \left(\frac{b}{2} \right)^2 \right]$$
$$= \tan^{-1} \left[\frac{3}{4} \left(\frac{v_0}{b} \right) \right]$$

and at point (b, a),

$$\gamma_{xy} = \tan^{-1} \left[\frac{3v_0}{b^3} (b^2) \right]$$
$$= \tan^{-1} \left[3 \left(\frac{v_0}{b} \right) \right]$$



Ans.

2-33. The fiber AB has a length L and orientation θ . If its ends A and B undergo very small displacements u_A and v_B , respectively, determine the normal strain in the fiber when it is in position A'B'.



Geometry:

$$L_{A'B'} = \sqrt{(L\cos\theta - u_A)^2 + (L\sin\theta + v_B)^2}$$
$$= \sqrt{L^2 + u_A^2 + v_B^2 + 2L(v_B\sin\theta - u_A\cos\theta)}$$

Average Normal Strain:

$$\epsilon_{AB} = \frac{L_{A'B'} - L}{L}$$
$$= \sqrt{1 + \frac{u_A^2 + v_B^2}{L^2} + \frac{2(v_B \sin \theta - u_A \cos \theta)}{L} - 1}$$

Neglecting higher terms u_A^2 and v_B^2

$$\epsilon_{AB} = \left[1 + \frac{2(v_B \sin \theta - u_A \cos \theta)}{L}\right]^{\frac{1}{2}} - 1$$

Using the binomial theorem:

$$\epsilon_{AB} = 1 + \frac{1}{2} \left(\frac{2v_B \sin \theta}{L} - \frac{2u_A \cos \theta}{L} \right) + \dots - 1$$
$$= \frac{v_B \sin \theta}{L} - \frac{u_A \cos \theta}{L}$$

Ans.

Ans. $\epsilon_{AB} = \frac{v_B \sin \theta}{L} - \frac{u_A \cos \theta}{L}$

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2–34. If the normal strain is defined in reference to the final length, that is,

$$\boldsymbol{\epsilon}_n' = \lim_{p \to p'} \left(\frac{\Delta s' - \Delta s}{\Delta s'} \right)$$

instead of in reference to the original length, Eq. 2–2, show that the difference in these strains is represented as a second-order term, namely, $\epsilon_n - \epsilon'_n = \epsilon_n \epsilon'_n$.

$$\epsilon_{B} = \frac{\Delta S' - \Delta S}{\Delta S}$$

$$\epsilon_{B} - \epsilon'_{A} = \frac{\Delta S' - \Delta S}{\Delta S} - \frac{\Delta S' - \Delta S}{\Delta S'}$$

$$= \frac{\Delta S'^{2} - \Delta S \Delta S' - \Delta S' \Delta S + \Delta S^{2}}{\Delta S \Delta S'}$$

$$= \frac{\Delta S'^{2} + \Delta S^{2} - 2\Delta S' \Delta S}{\Delta S \Delta S'}$$

$$= \frac{(\Delta S' - \Delta S)^{2}}{\Delta S \Delta S'} = \left(\frac{\Delta S' - \Delta S}{\Delta S}\right) \left(\frac{\Delta S' - \Delta S}{\Delta S'}\right)$$

$$= \epsilon_{A} \epsilon'_{B} (Q.E.D)$$