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#### 2–1.

An air-filled rubber ball has a diameter of 6 in. If the air pressure within the ball is increased until the diameter becomes 7 in., determine the average normal strain in the rubber.

#### SOLUTION

$$d_0 = 6$$
 in.  
 $d = 7$  in.  
 $\epsilon = \frac{\pi d - \pi d_0}{\pi d_0} = \frac{7 - 6}{6} = 0.167$  in./in.

Ans.

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#### 2–2.

A thin strip of rubber has an unstretched length of 15 in. If it is stretched around a pipe having an outer diameter of 5 in., determine the average normal strain in the strip.

#### SOLUTION

 $L_0 = 15$  in.  $L = \pi(5 \text{ in.})$  $\epsilon = \frac{L - L_0}{L_0} = \frac{5\pi - 15}{15} = 0.0472$  in./in.

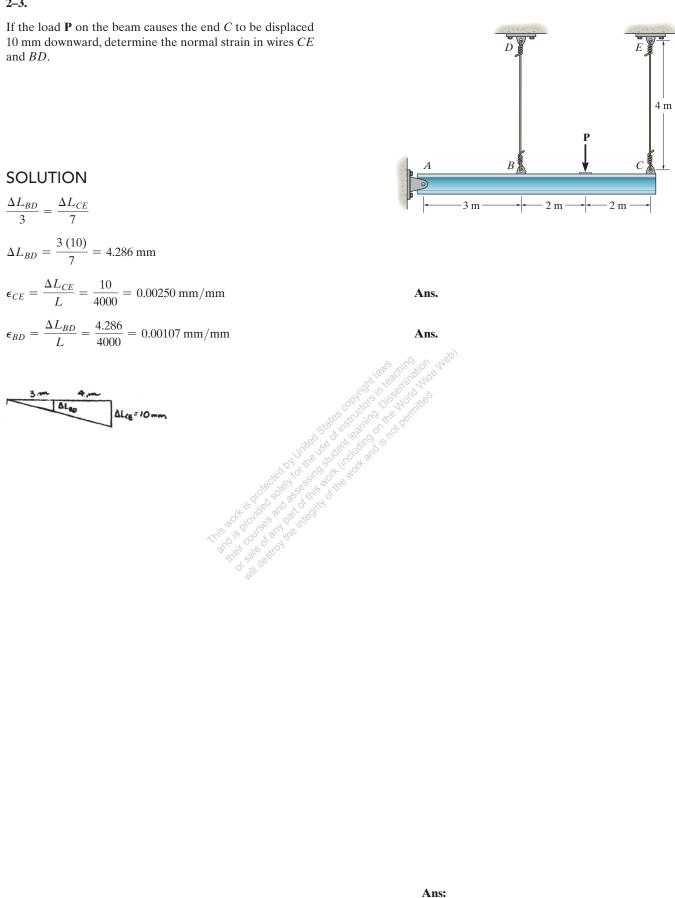
Ans.

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Ans:  $\epsilon = 0.0472$  in./in.

#### 2–3.

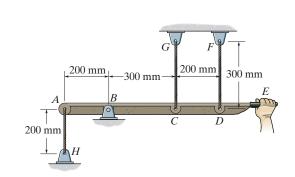
10 mm downward, determine the normal strain in wires CE and *BD*.



 $\epsilon_{CE} = 0.00250 \text{ mm/mm}, \epsilon_{BD} = 0.00107 \text{ mm/mm}$ 

#### \*2–4.

The force applied at the handle of the rigid lever causes the lever to rotate clockwise about the pin B through an angle of 2°. Determine the average normal strain in each wire. The wires are unstretched when the lever is in the horizontal position.



#### SOLUTION

**Geometry:** The lever arm rotates through an angle of  $\theta = \left(\frac{2^{\circ}}{180}\right)\pi$  rad = 0.03491 rad. Since  $\theta$  is small, the displacements of points *A*, *C*, and *D* can be approximated by

- $\delta_A = 200(0.03491) = 6.9813 \text{ mm}$
- $\delta_C = 300(0.03491) = 10.4720 \,\mathrm{mm}$
- $\delta_D = 500(0.03491) = 17.4533 \text{ mm}$

Average Normal Strain: The unstretched length of wires AH, CG, and DF are

 $L_{AH} = 200 \text{ mm}, L_{CG} = 300 \text{ mm}, \text{ and } L_{DF} = 300 \text{ mm}.$  We obtain

$$(\epsilon_{\text{avg}})_{AH} = \frac{\delta_A}{L_{AH}} = \frac{6.9813}{200} = 0.0349 \text{ mm/mm}$$

$$(\epsilon_{\text{avg}})_{CG} = \frac{\delta_C}{L_{CG}} = \frac{10.4720}{300} = 0.0349 \text{ mm/mm}$$

$$(\epsilon_{\text{avg}})_{DF} = \frac{\delta_D}{L_{DF}} = \frac{17.4533}{300} = 0.0582 \text{ mm/mm}$$
Ans.

$$A' = \frac{200 \text{ mm}}{300} = 0.0382 \text{ mm}/\text{m}}$$

(a)

Ans:  $(\epsilon_{avg})_{AH} = 0.0349 \text{ mm/mm}$   $(\epsilon_{avg})_{CG} = 0.0349 \text{ mm/mm}$  $(\epsilon_{avg})_{DF} = 0.0582 \text{ mm/mm}$ 

#### 2–5.

The rectangular plate is subjected to the deformation shown by the dashed line. Determine the average shear strain  $\gamma_{xy}$ in the plate.

#### SOLUTION

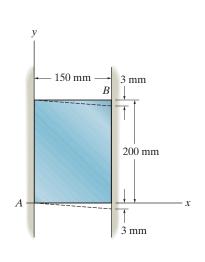
#### Geometry:

$$\theta' = \tan^{-1} \frac{3}{150} = 0.0200 \text{ rad}$$
  
 $\theta = \left(\frac{\pi}{2} + 0.0200\right) \text{ rad}$ 

**Shear Strain:** 

$$\gamma_{xy} = \frac{\pi}{2} - \theta = \frac{\pi}{2} - \left(\frac{\pi}{2} + 0.0200\right)$$

$$= -0.0200 \text{ rad}$$
Ans.
$$\int \frac{3}{1} \int \frac$$



#### 2-6.

The square deforms into the position shown by the dashed lines. Determine the shear strain at each of its corners, A, B, C, and D, relative to the x, y axes. Side D'B' remains horizontal.

#### SOLUTION

#### Geometry:

$$B'C' = \sqrt{(8+3)^2 + (53 \sin 88.5^\circ)^2} = 54.1117 \text{ mm}$$

$$C'D' = \sqrt{53^2 + 58^2 - 2(53)(58) \cos 91.5^\circ}$$

$$= 79.5860 \text{ mm}$$

$$B'D' = 50 + 53 \sin 1.5^\circ - 3 = 48.3874 \text{ mm}$$

$$\cos \theta = \frac{(B'D')^2 + (B'C')^2 - (C'D')^2}{2(B'D')(B'C')}$$

$$= \frac{48.3874^2 + 54.1117^2 - 79.5860^2}{2(48.3874)(54.1117)} = -0.20328$$

$$\theta = 101.73^\circ$$

$$\beta = 180^\circ - \theta = 78.27^\circ$$

#### **Shear Strain:**

$$\theta = 101.73^{\circ}$$

$$\beta = 180^{\circ} - \theta = 78.27^{\circ}$$
rain:
$$(\gamma_A)_{xy} = \frac{\pi}{2} - \pi \left(\frac{91.5^{\circ}}{180^{\circ}}\right) = -0.0262 \text{ rad}$$
Ans.
$$(\gamma_B)_{xy} = \frac{\pi}{2} - \theta = \frac{\pi}{2} - \pi \left(\frac{101.73^{\circ}}{180^{\circ}}\right) = -0.205 \text{ rad}$$
Ans.
$$(\gamma_C)_{xy} = \beta - \frac{\pi}{2} = \pi \left(\frac{78.27^{\circ}}{180^{\circ}}\right) - \frac{\pi}{2} = -0.205 \text{ rad}$$
Ans.
$$(\gamma_D)_{xy} = \pi \left(\frac{88.5^{\circ}}{180^{\circ}}\right) - \frac{\pi}{2} = -0.0262 \text{ rad}$$
Ans.

– 3 mm

 $50 \mathrm{mm}$ 

С

50 mm

r

8 mm

B'

В

D

A

53 mm

53 mm

Г

91.5

50 mm

91.5

50 mm

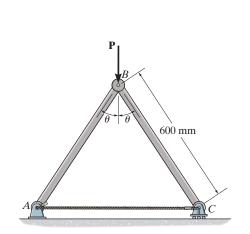
A

#### Ans:

 $(\gamma_A)_{xy} = -0.0262 \text{ rad}$   $(\gamma_B)_{xy} = -0.205 \text{ rad}$   $(\gamma_C)_{xy} = -0.205 \text{ rad}$  $(\gamma_D)_{xy} = -0.0262 \text{ rad}$ 

#### 2–7.

The pin-connected rigid rods *AB* and *BC* are inclined at  $\theta = 30^{\circ}$  when they are unloaded. When the force **P** is applied  $\theta$  becomes 30.2°. Determine the average normal strain in wire *AC*.



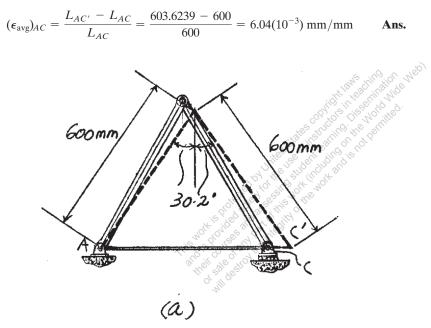
### SOLUTION

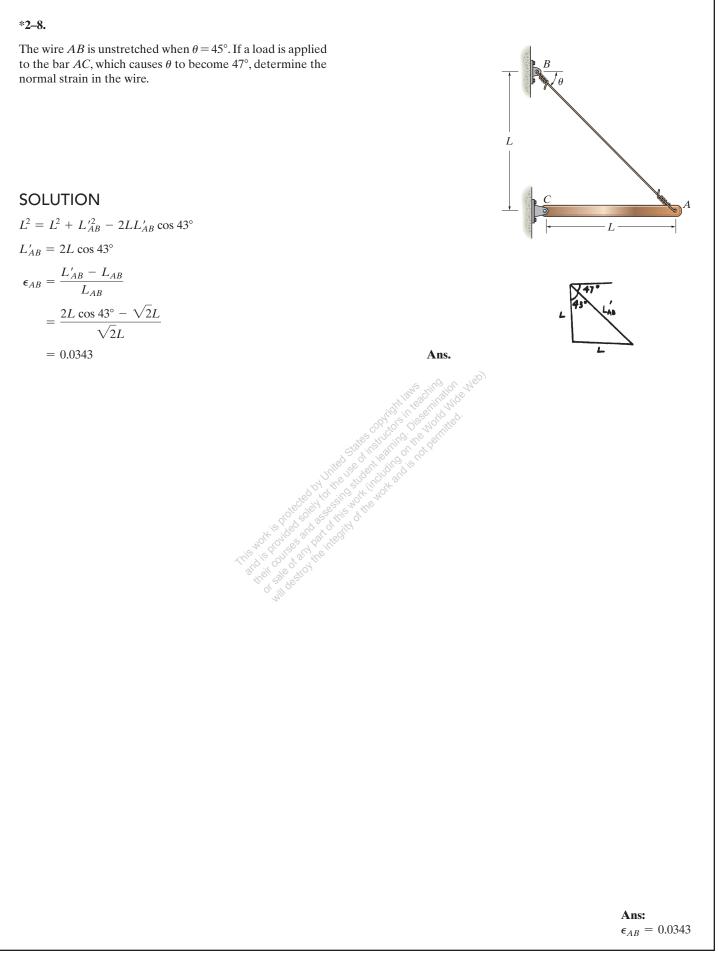
Geometry: Referring to Fig. a, the unstretched and stretched lengths of wire AD are

 $L_{AC} = 2(600 \sin 30^\circ) = 600 \text{ mm}$ 

 $L_{AC'} = 2(600 \sin 30.2^\circ) = 603.6239 \,\mathrm{mm}$ 

#### **Average Normal Strain:**





#### 2–9.

If a horizontal load applied to the bar AC causes point A to be displaced to the right by an amount  $\Delta L$ , determine the normal strain in the wire AB. Originally,  $\theta = 45^{\circ}$ .

#### SOLUTION

$$L'_{AB} = \sqrt{(\sqrt{2}L)^2 + \Delta L^2 - 2(\sqrt{2}L)(\Delta L)\cos 135^\circ}$$
$$= \sqrt{2L^2 + \Delta L^2 + 2L\Delta L}$$
$$\epsilon_{AB} = \frac{L'_{AB} - L_{AB}}{L_{AB}}$$
$$= \frac{\sqrt{2L^2 + \Delta L^2 + 2L\Delta L} - \sqrt{2}L}{\sqrt{2}L}$$
$$= \sqrt{1 + \frac{\Delta L^2}{2L^2} + \frac{\Delta L}{L}} - 1$$

Neglecting the higher-order terms,

$$\epsilon_{AB} = \left(1 + \frac{\Delta L}{L}\right)^{\frac{1}{2}} - 1$$

$$= 1 + \frac{1}{2}\frac{\Delta L}{L} + \dots - 1$$

$$= \frac{0.5\Delta L}{L}$$
(binomial theorem)
(binomial theorem)
(binomial theorem)

Also,

$$\epsilon_{AB} = \frac{\Delta L \sin 45^{\circ}}{\sqrt{2}L} = \frac{0.5 \ \Delta L}{L}$$

Ans.

Ans.

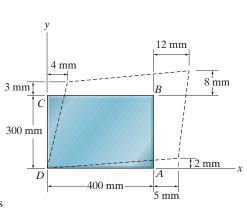
Ans:  $\epsilon_{AB} = \frac{0.5\Delta L}{2}$ 

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#### 2–10.

Determine the shear strain  $\gamma_{xy}$  at corners *A* and *B* if the plastic distorts as shown by the dashed lines.



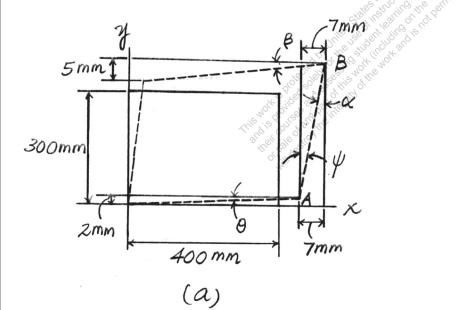
#### SOLUTION

Geometry: Referring to the geometry shown in Fig. a, the small-angle analysis gives

$$\alpha = \psi = \frac{7}{306} = 0.022876 \text{ rad}$$
$$\beta = \frac{5}{408} = 0.012255 \text{ rad}$$
$$\theta = \frac{2}{405} = 0.0049383 \text{ rad}$$

Shear Strain: By definition,

$$(\gamma_A)_{xy} = \theta + \psi = 0.02781 \text{ rad} = 27.8(10^{-3}) \text{ rad}$$
  
 $(\gamma_B)_{xy} = \alpha + \beta = 0.03513 \text{ rad} = 35.1(10^{-3}) \text{ rad}$ 



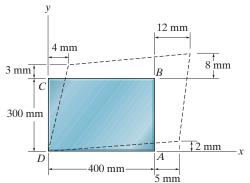
#### Ans:

 $(\gamma_A)_{xy} = 27.8(10^{-3})$  rad  $(\gamma_B)_{xy} = 35.1(10^{-3})$  rad

Ans.

#### 2–11.

Determine the shear strain  $\gamma_{xy}$  at corners D and C if the plastic distorts as shown by the dashed lines.



#### SOLUTION

Geometry: Referring to the geometry shown in Fig. a, the small-angle analysis gives

$$\alpha = \psi = \frac{4}{303} = 0.013201 \text{ rad}$$
$$\theta = \frac{2}{405} = 0.0049383 \text{ rad}$$
$$\beta = \frac{5}{408} = 0.012255 \text{ rad}$$

Shear Strain: By definition,

$$(\gamma_{xy})_C = \alpha + \beta = 0.02546 \text{ rad} = 25.5(10^{-3}) \text{ rad}$$
  
 $(\gamma_{xy})_D = \theta + \psi = 0.01814 \text{ rad} = 18.1(10^{-3}) \text{ rad}$ 

$$(\gamma_{xy})_{C} = \alpha + \beta = 0.02546 \text{ rad} = 25.5(10^{-3}) \text{ rad}$$

$$(\gamma_{xy})_{D} = \theta + \psi = 0.01814 \text{ rad} = 18.1(10^{-3}) \text{ rad}$$
Ans.
  

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$$(\gamma_{xy})_{D} = \theta + \psi = 0.01814 \text{ rad} = 18.1(10^{-3}) \text{ rad}$$

Ans:  $(\gamma_{xy})_C = 25.5(10^{-3})$  rad  $(\gamma_{xy})_D = 18.1(10^{-3})$  rad

#### \*2-12.

The material distorts into the dashed position shown. Determine the average normal strains  $\epsilon_x$ ,  $\epsilon_y$  and the shear strain  $\gamma_{xy}$  at A, and the average normal strain along line BE.

#### SOLUTION

Geometry: Referring to the geometry shown in Fig. a,

$$\tan \theta = \frac{15}{250}; \qquad \theta = (3.4336^{\circ}) \left(\frac{\pi}{180^{\circ}} \operatorname{rad}\right) = 0.05993 \operatorname{rad}$$
$$L_{AC}' = \sqrt{15^2 + 150^2} = \sqrt{62725} \operatorname{mm}$$
$$\frac{BB'}{15} = \frac{200}{250}; \qquad BB' = 12 \operatorname{mm} \quad \frac{EE'}{30} = \frac{50}{250}; \qquad EE' = 6 \operatorname{mm}$$
$$x' = 150 + EE' - BB' = 150 + 6 - 12 = 144 \operatorname{mm}$$

$$L_{BE} = \sqrt{150^2 + 150^2} = 150\sqrt{2} \text{ mm} \quad L_{B'E'} = \sqrt{144^2 + 150^2} = \sqrt{43236} \text{ mm}$$
  
werage Normal and Shear Strain: Since no deformation occurs along x axis,

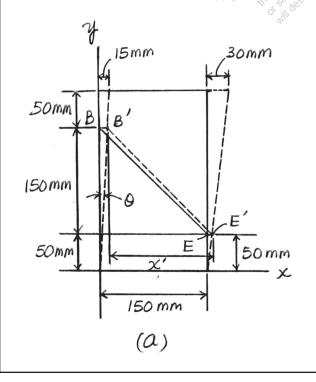
Average Normal and Shear Strain: Since no deformation occurs along x axis,

$$(\epsilon_x)_A = 0$$
 Ans.  
 $(\epsilon_y)_A = \frac{L_{AC'} - L_{AC}}{L_{AC}} = \frac{\sqrt{62725} - 250}{250} = 1.80(10^{-3}) \text{ mm/mm}$  Ans.

By definition,

 $(\gamma_{xy})_A = \theta = 0.0599$  rad

$$\epsilon_{BE} = \frac{L_{B'E'} - L_{BE}}{L_{BE}} = \frac{\sqrt{43236} - 150\sqrt{2}}{150\sqrt{2}} = -0.0198 \text{ mm/mm}$$
 Ans.



# Ans: $(\epsilon_x)_A = 0$ $(\epsilon_y)_A = 1.80(10^{-3}) \text{ mm/mm}$ $(\gamma_{xy})_A = 0.0599 \text{ rad}$ $\epsilon_{BE} = -0.0198 \text{ mm/mm}$

 $15 \mathrm{mm}$ 

С

В

A

50 mm

200 mm

Ans.

30 mm

D

E

-150 mm

F

50 mm

#### 2–13.

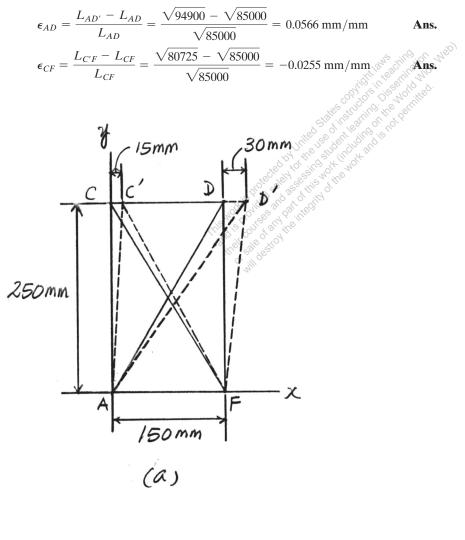
The material distorts into the dashed position shown. Determine the average normal strains along the diagonals *AD* and *CF*.

#### SOLUTION

**Geometry:** Referring to the geometry shown in Fig. *a*,

$$\begin{split} L_{AD} &= L_{CF} = \sqrt{150^2 + 250^2} = \sqrt{85000} \text{ mm} \\ L_{AD'} &= \sqrt{(150 + 30)^2 + 250^2} = \sqrt{94900} \text{ mm} \\ L_{C'F} &= \sqrt{(150 - 15)^2 + 250^2} = \sqrt{80725} \text{ mm} \end{split}$$

**Average Normal Strain:** 



Ans:  $\epsilon_{AD} = 0.0566 \text{ mm/mm}$  $\epsilon_{CF} = -0.0255 \text{ mm/mm}$ 

15 mm

С

В

A

50 mm

200 mm

30 mm

 $D^{\dagger}$ 

F

-150 mm

F

50 mm

#### 2–14.

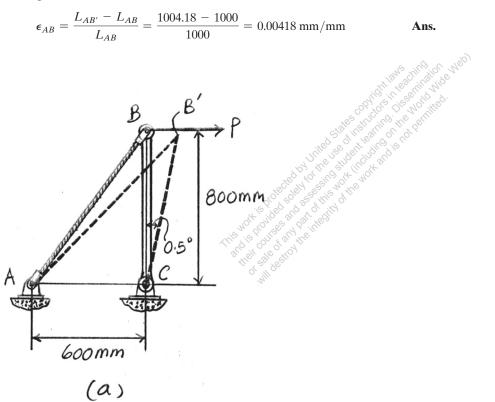
Part of a control linkage for an airplane consists of a rigid member *CB* and a flexible cable *AB*. If a force is applied to the end *B* of the member and causes it to rotate by  $\theta = 0.5^{\circ}$ , determine the normal strain in the cable. Originally the cable is unstretched.

#### SOLUTION

**Geometry:** Referring to the geometry shown in Fig. *a*, the unstretched and stretched lengths of cable *AB* are

$$L_{AB} = \sqrt{600^2 + 800^2} = 1000 \text{ mm}$$
$$L_{AB'} = \sqrt{600^2 + 800^2 - 2(600)(800) \cos 90.5^\circ} = 1004.18 \text{ mm}$$

**Average Normal Strain:** 



800 mm

C

600 mm

#### 2–15.

Part of a control linkage for an airplane consists of a rigid member CB and a flexible cable AB. If a force is applied to the end B of the member and causes a normal strain in the cable of 0.004 mm/mm, determine the displacement of point B. Originally the cable is unstretched.

#### SOLUTION

Geometry: Referring to the geometry shown in Fig. a, the unstretched and stretched lengths of cable AB are

$$L_{AB} = \sqrt{600^2 + 800^2} = 1000 \text{ mm}$$
$$L_{AB'} = \sqrt{600^2 + 800^2 - 2(600)(800) \cos(90^\circ + \theta)}$$
$$L_{AB'} = \sqrt{1(10^6) - 0.960(10^6) \cos(90^\circ + \theta)}$$

**Average Normal Strain:** 

$$\epsilon_{AB} = \frac{L_{AB'} - L_{AB}}{L_{AB}}; \quad 0.004 = \frac{\sqrt{1(10^6) - 0.960(10^6)\cos(90^\circ + \theta)} - 1000}{1000}$$
  
$$\theta = 0.4784^\circ \left(\frac{\pi}{180^\circ}\right) = 0.008350 \text{ rad}$$
  
$$\Delta_B = \theta L_{BC} = 0.008350(800) = 6.68 \text{ mm}$$
  
Ans.

Thus,

$$\Delta_B = \theta L_{BC} = 0.008350(800) = 6.68 \text{ mm}$$

$$\Delta_B = \theta L_{BC} = 0.008350(800) = 6.68 \text{ mm}$$

(a)

Р

800 mm

R

С

600 mm

A

Ans.

B

L

Ans.

Ans.

QED

#### \*2-16.

The nylon cord has an original length L and is tied to a bolt at A and a roller at B. If a force **P** is applied to the roller, determine the normal strain in the cord when the roller is at C, and at D. If the cord is originally unstrained when it is at C, determine the normal strain  $\epsilon'_D$  when the roller moves to D. Show that if the displacements  $\Delta_C$  and  $\Delta_D$  are small, then  $\epsilon'_D = \epsilon_D - \epsilon_C$ .

#### SOLUTION

 $\sqrt{-2}$ 

$$L_C = \sqrt{L^2 + \Delta_C^2}$$

$$\epsilon_C = \frac{\sqrt{L^2 + \Delta_C^2} - L}{L}$$

$$= \frac{L\sqrt{1 + \left(\frac{\Delta_C^2}{L^2}\right)} - L}{L} = \sqrt{1 + \left(\frac{\Delta_C^2}{L^2}\right)} - 1$$

For small  $\Delta_C$ ,

$$\epsilon_C = 1 + \frac{1}{2} \left( \frac{\Delta_C^2}{L^2} \right) - 1 = \frac{1}{2} \frac{\Delta_C^2}{L^2}$$

In the same manner,

$$\epsilon_{D} = \frac{1}{2} \frac{\Delta_{D}^{2}}{L^{2}}$$

$$\epsilon_{D}' = \frac{\sqrt{L^{2} + \Delta_{D}^{2}} - \sqrt{L^{2} + \Delta_{C}^{2}}}{\sqrt{L^{2} + \Delta_{C}^{2}}} = \frac{\sqrt{1 + \frac{\Delta_{D}^{2}}{L^{2}}} - \sqrt{1 + \frac{\Delta_{C}^{2}}{L^{2}}}}{\sqrt{1 + \frac{\Delta_{C}^{2}}{L^{2}}}}$$

For small  $\Delta_C$  and  $\Delta_D$ ,

$$\epsilon_{D'} = \frac{\left(1 + \frac{1}{2}\frac{\Delta_{C}^{2}}{L^{2}}\right) - \left(1 + \frac{1}{2}\frac{\Delta_{D}^{2}}{L^{2}}\right)}{\left(1 + \frac{1}{2}\frac{\Delta_{C}^{2}}{L^{2}}\right)} = \frac{\frac{1}{2L^{2}}\left(\Delta_{C}^{2} + \Delta_{D}^{2}\right)}{\frac{1}{2L^{2}}\left(2L^{2} + \Delta_{C}^{2}\right)}$$
$$\epsilon_{D'} = \frac{\Delta_{C}^{2} - \Delta_{D}^{2}}{2L^{2} - \Delta_{C}^{2}} = \frac{1}{2L^{2}}\left(\Delta_{C}^{2} - \Delta_{D}^{2}\right) = \epsilon_{C} - \epsilon_{D}$$

Also this problem can be solved as follows:

$$A_{C} = L \sec \theta_{C}; \qquad A_{D} = L \sec \theta_{D}$$
$$\epsilon_{C} = \frac{L \sec \theta_{C} - L}{L} = \sec \theta_{C} - 1$$
$$\epsilon_{D} = \frac{L \sec \theta_{D} - L}{L} = \sec \theta_{D} - 1$$

$$\epsilon_D = \frac{L \sec \theta_D - L}{L} = \sec \theta_D - 1$$

Expanding sec  $\theta$ 

 $\sec \theta = 1 + \frac{\theta^2}{2!} + \frac{5 \, \theta^4}{4!} \dots$ 

#### \*2-16. Continued

For small  $\theta$  neglect the higher order terms

$$\sec\theta = 1 + \frac{\theta^2}{2}$$

Hence,

$$\epsilon_{C} = 1 + \frac{\theta_{C}^{2}}{2} - 1 = \frac{\theta_{C}^{2}}{2}$$

$$\epsilon_{D} = 1 + \frac{\theta_{D}^{2}}{2} - 1 = \frac{\theta_{D}^{2}}{2}$$

$$\epsilon_{D}' = \frac{L \sec \theta_{D} - L \sec \theta_{C}}{L \sec \theta_{C}} = \frac{\sec \theta_{D}}{\sec \theta_{C}} - 1 = \sec \theta_{D} \cos \theta_{C} - 1$$
Since  $\cos \theta = 1 - \frac{\theta^{2}}{2!} + \frac{\theta^{4}}{4!}$ .....
$$\sec \theta_{D} \cos \theta_{C} = \left(1 + \frac{\theta_{D}^{2}}{2} - \cdots\right) \left(1 - \frac{\theta_{C}^{2}}{2} - \cdots\right)$$

$$= 1 - \frac{\theta^{2}_{C}}{2} + \frac{\theta^{2}_{D}}{2} - \frac{\theta^{2}_{C}}{4}$$
Neglecting the higher order terms
$$\sec \theta_{D} \cos \theta_{C} = 1 + \frac{\theta^{2}_{D}}{2} - \frac{\theta^{2}_{C}}{2}$$

Neglecting the higher order terms

Neglecting the higher order terms  

$$\sec \theta_D \cos \theta_C = 1 + \frac{\theta_D^2}{2} - \frac{\theta_C^2}{2}$$

$$\epsilon_D' = \left[1 + \frac{\theta_2^2}{2} - \frac{\theta_1^2}{2}\right] - 1 = \frac{\theta_D^2}{2} - \frac{\theta_C^2}{2}$$

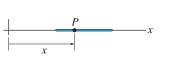
$$= \epsilon_D - \epsilon_C$$

QED

Ans:  $\epsilon_C = \frac{1}{2} \frac{\Delta_C^2}{L^2}$   $\epsilon_D = \frac{1}{2} \frac{\Delta_D^2}{L^2}$ 

#### 2–17.

A thin wire, lying along the x axis, is strained such that each point on the wire is displaced  $\Delta x = kx^2$  along the x axis. If k is constant, what is the normal strain at any point P along the wire?



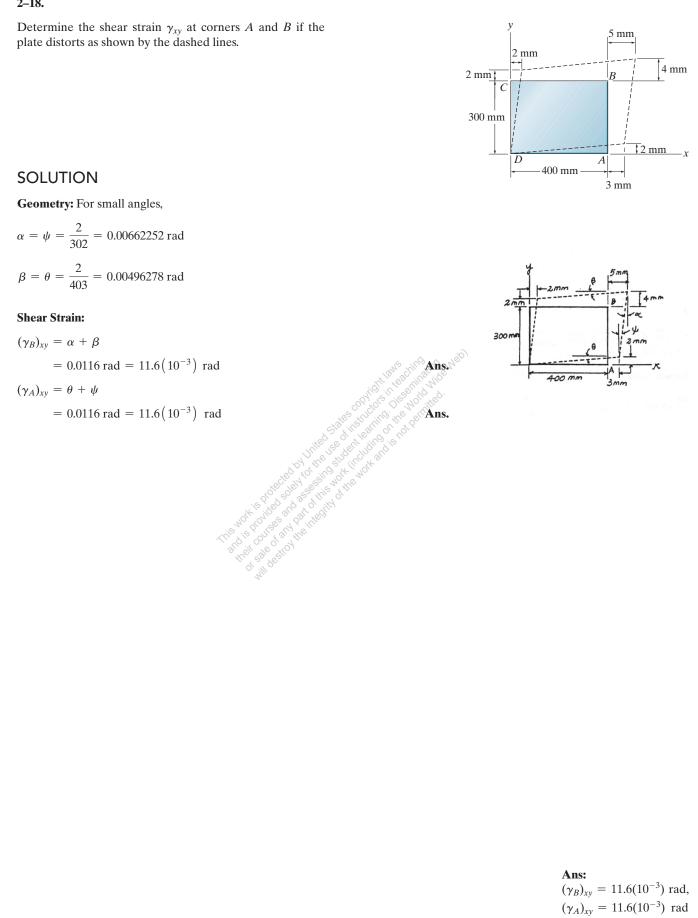
#### SOLUTION

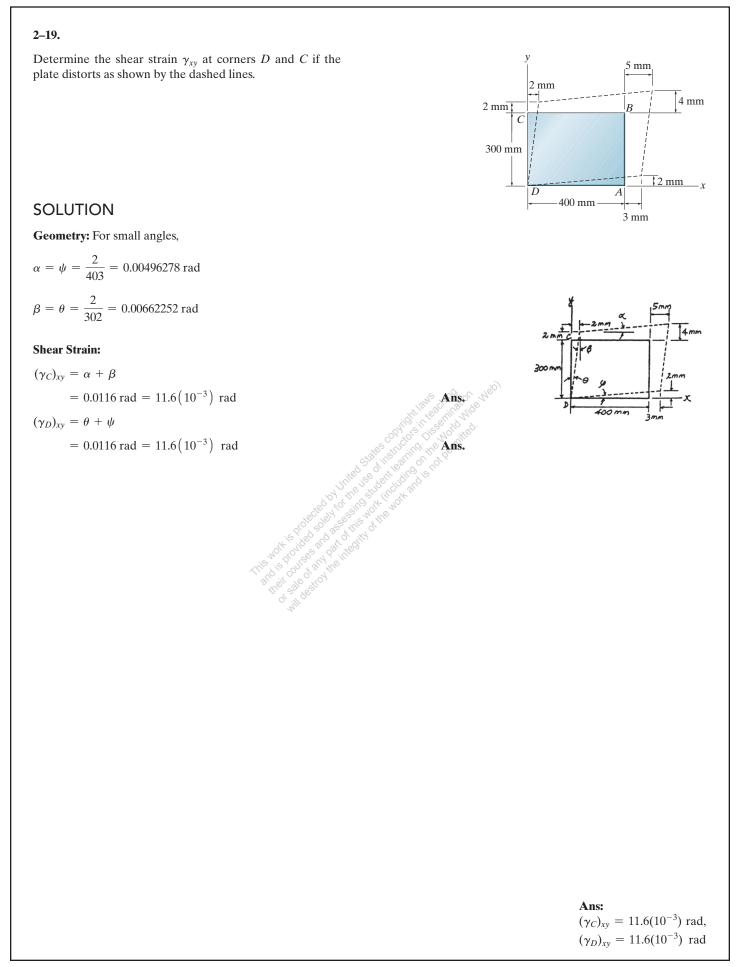
$$\epsilon = \frac{d(\Delta x)}{dx} = 2 k x$$

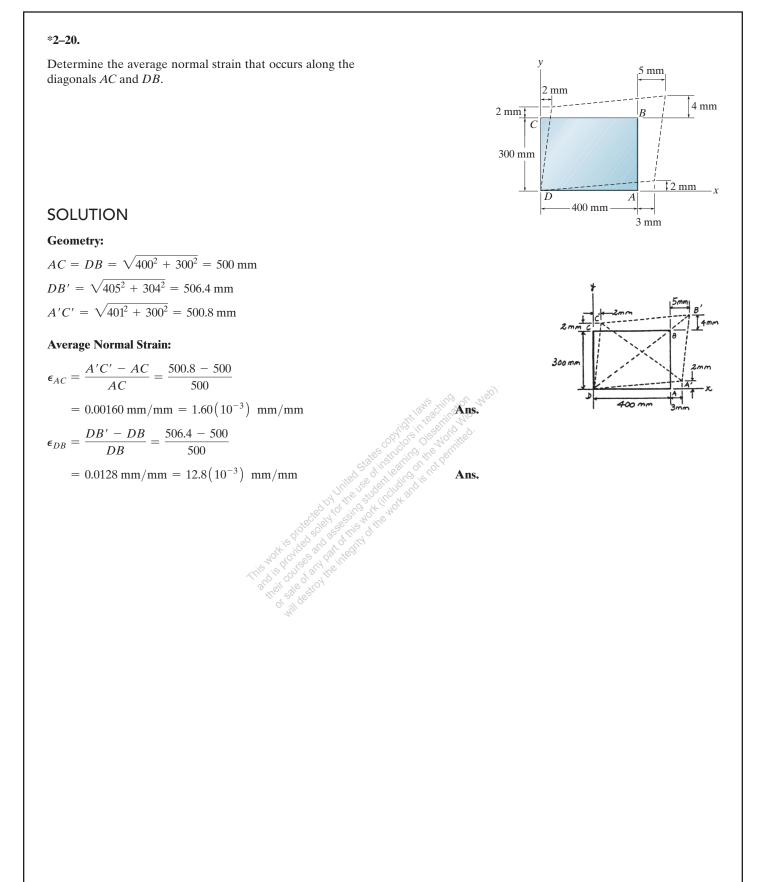
Ans.



#### 2–18.



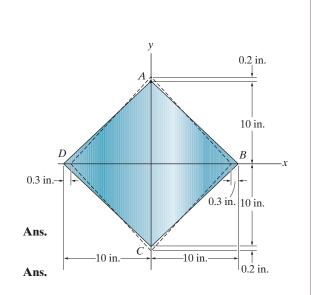




#### Ans: $\epsilon_{AC} = 1.60 (10^{-3}) \text{ mm/mm}$ $\epsilon_{DB} = 12.8 (10^{-3}) \text{ mm/mm}$

#### 2–21.

The corners of the square plate are given the displacements indicated. Determine the average normal strains  $\epsilon_x$  and  $\epsilon_y$  along the *x* and *y* axes.



#### SOLUTION

$$\epsilon_x = \frac{-0.3}{10} = -0.03 \text{ in./in.}$$
  
 $\epsilon_y = \frac{0.2}{10} = 0.02 \text{ in./in.}$ 



Ans:  $\epsilon_x = -0.03 \text{ in./in.}$  $\epsilon_y = 0.02 \text{ in./in.}$ 

#### 2–22.

The triangular plate is fixed at its base, and its apex A is given a horizontal displacement of 5 mm. Determine the shear strain,  $\gamma_{xy}$ , at A.

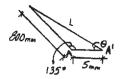
#### SOLUTION

 $L = \sqrt{800^2 + 5^2 - 2(800)(5)\cos 135^\circ} = 803.54 \,\mathrm{mm}$  $\frac{\sin 135^{\circ}}{803.54} = \frac{\sin \theta}{800}; \qquad \theta = 44.75^{\circ} = 0.7810 \text{ rad}$ 

$$\gamma_{xy} = \frac{\pi}{2} - 2\theta = \frac{\pi}{2} - 2(0.7810)$$

= 0.00880 rad





800 mm

5 mm

45°

45

800 mm

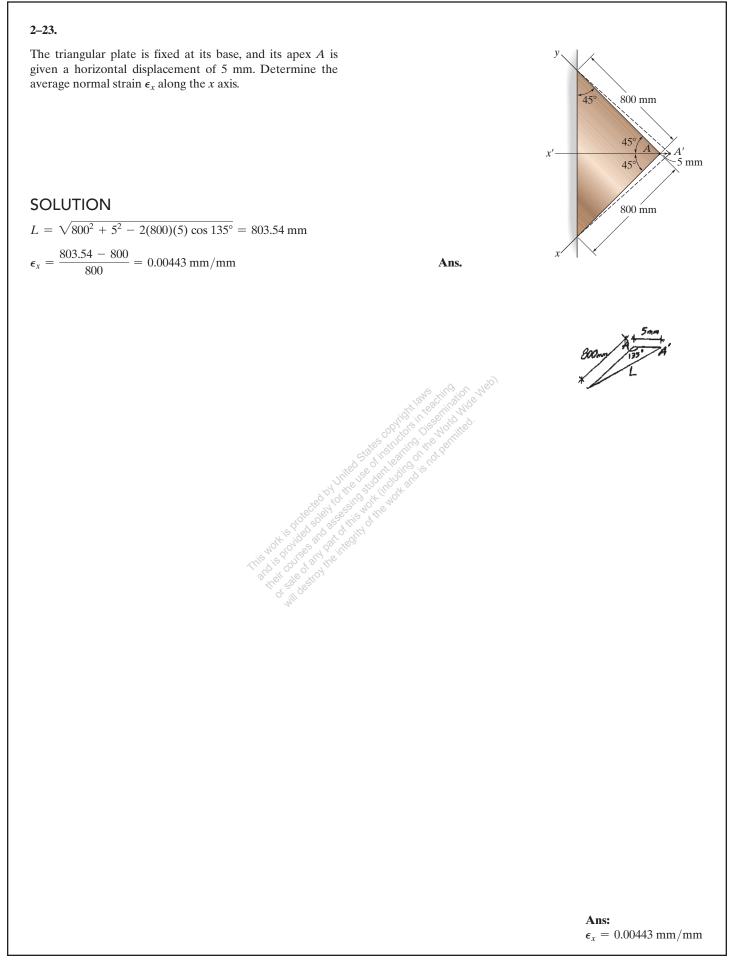
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X

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#### \*2–24.

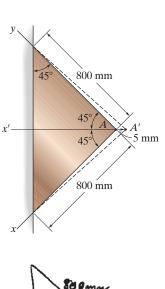
The triangular plate is fixed at its base, and its apex A is given a horizontal displacement of 5 mm. Determine the average normal strain  $\epsilon_{x'}$  along the x' axis.

#### SOLUTION

$$L = 800 \cos 45^\circ = 565.69 \,\mathrm{mm}$$

$$\epsilon_{x'} = \frac{5}{565.69} = 0.00884 \,\mathrm{mm/mm}$$

Ans.





Ans:  $\epsilon_{x'} = 0.00884 \text{ mm/mm}$ 

#### 2–25.

The polysulfone block is glued at its top and bottom to the rigid plates. If a tangential force, applied to the top plate, causes the material to deform so that its sides are described by the equation  $y = 3.56 x^{1/4}$ , determine the shear strain at the corners *A* and *B*.

#### SOLUTION

$$y = 3.56 x^{1/4}$$
$$\frac{dy}{dx} = 0.890 x^{-3/4}$$
$$\frac{dx}{dy} = 1.123 x^{3/4}$$

At A, x = 0

$$\gamma_A = \frac{dx}{dy} = 0$$

#### At *B*,

 $2 = 3.56 \, x^{1/4}$ 

x = 0.0996 in.

$$\gamma_B = \frac{dx}{dy} = 1.123(0.0996)^{3/4} = 0.199$$
 rad

strong of the states

v

B

2 in.

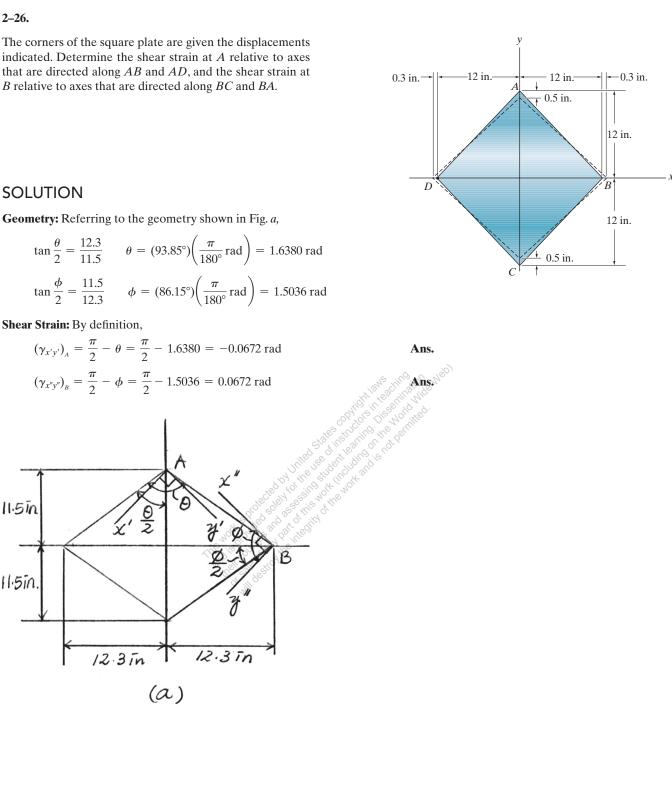
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#### 2-26.

11.5ir

11.5in

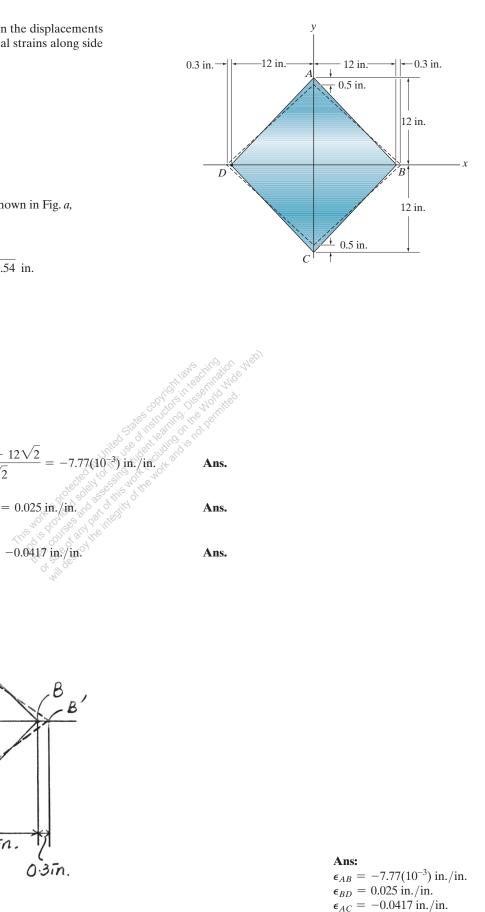
The corners of the square plate are given the displacements indicated. Determine the shear strain at A relative to axes that are directed along AB and AD, and the shear strain at B relative to axes that are directed along BC and BA.



Ans:  $(\gamma_{x'y'})_A = -0.0672 \text{ rad}$  $(\gamma_{x'y''})_B = 0.0672 \text{ rad}$ 

#### 2–27.

The corners of the square plate are given the displacements indicated. Determine the average normal strains along side AB and diagonals AC and BD.



## Geometry: Referring to the geometry shown in Fig. a,

SOLUTION

$$L_{AB} = \sqrt{12^2 + 12^2} = 12\sqrt{2} \text{ in.}$$
$$L_{A'B'} = \sqrt{12.3^2 + 11.5^2} = \sqrt{283.54} \text{ in.}$$
$$L_{BD} = 2(12) = 24 \text{ in.}$$
$$L_{B'D'} = 2(12 + 0.3) = 24.6 \text{ in.}$$

$$L_{AC} = 2(12) = 24$$
 in.

$$L_{A'C'} = 2(12 - 0.5) = 23$$
 in.

**Average Normal Strain:** 

$$\epsilon_{AB} = \frac{L_{A'B'} - L_{AB}}{L_{AB}} = \frac{\sqrt{283.54} - 12\sqrt{2}}{12\sqrt{2}} = -7.77(10^{-3}) \text{ in./in.} \qquad \text{An}$$

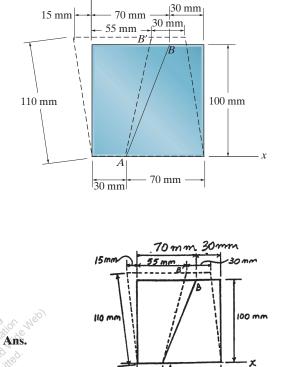
$$\epsilon_{BD} = \frac{L_{B'D'} - L_{BD}}{L_{BD}} = \frac{24.6 - 24}{24} = 0.025 \text{ in./in.} \qquad \text{An}$$

$$\epsilon_{AC} = \frac{L_{A'C'} - L_{AC}}{L_{AC}} = \frac{23 - 24}{24} = -0.0417 \text{ in./in.} \qquad \text{An}$$

0.5in 12 in D 12 in. 0.5in.] C 12in. 12, m 0.3in. (a)

#### \*2-28.

The block is deformed into the position shown by the dashed lines. Determine the average normal strain along line AB.



70 mm

1300

#### SOLUTION

#### Geometry:

 $AB = \sqrt{100^2 + (70 - 30)^2} = 107.7033 \,\mathrm{mm}$  $AB' = \sqrt{(70 - 30 - 15)^2 + (110^2 - 15^2)} = 111.8034 \,\mathrm{mm}$ 

#### **Average Normal Strain:**

$$\epsilon_{AB} = \frac{AB' - AB}{AB}$$
111 8024 - 10

$$=\frac{111.8034 - 107.7033}{107.7033}$$

 $= 0.0381 \text{ mm/mm} = 38.1 (10^{-3}) \text{ mm}$ 

Ans:  $\epsilon_{AB} = 38.1 (10^{-3}) \text{ mm}$ 

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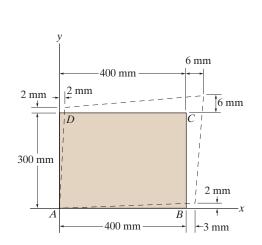
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#### 2–29.

The rectangular plate is deformed into the shape shown by the dashed lines. Determine the average normal strain along diagonal AC, and the average shear strain at corner A relative to the x, y axes.



#### SOLUTION

**Geometry:** The unstretched length of diagonal *AC* is

$$L_{AC} = \sqrt{300^2 + 400^2} = 500 \,\mathrm{mm}$$

Referring to Fig. a, the stretched length of diagonal AC is

$$L_{AC'} = \sqrt{(400 + 6)^2 + (300 + 6)^2} = 508.4014 \text{ mm}$$

Referring to Fig. a and using small angle analysis,

$$\phi = \frac{2}{300 + 2} = 0.006623 \text{ rad}$$
$$\alpha = \frac{2}{400 + 3} = 0.004963 \text{ rad}$$

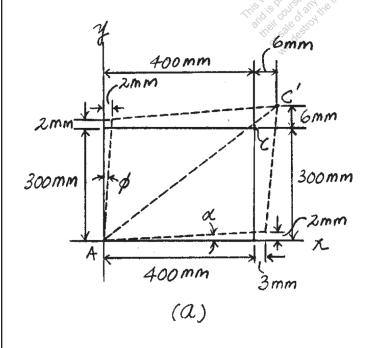
Average Normal Strain: Applying Eq. 2,

$$(\epsilon_{\text{avg}})_{AC} = \frac{L_{AC'} - L_{AC}}{L_{AC}} = \frac{508.4014 - 500}{500} = 0.0168 \text{ mm/mm}$$
 Ans.

Shear Strain: Referring to Fig. a,

(

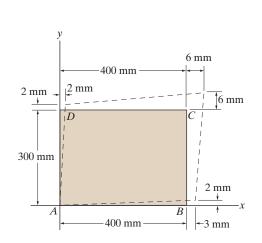
$$(\gamma_A)_{xy} = \phi + \alpha = 0.006623 + 0.004963 = 0.0116 \text{ rad}$$
 Ans.



**Ans:**  $(\epsilon_{avg})_{AC} = 0.0168 \text{ mm/mm}, (\gamma_A)_{xy} = 0.0116 \text{ rad}$ 

#### 2-30.

The rectangular plate is deformed into the shape shown by the dashed lines. Determine the average normal strain along diagonal BD, and the average shear strain at corner Brelative to the *x*, *y* axes.



#### SOLUTION

Geometry: The unstretched length of diagonal BD is

$$L_{BD} = \sqrt{300^2 + 400^2} = 500 \,\mathrm{mm}$$

Referring to Fig. a, the stretched length of diagonal BD is

$$L_{B'D'} = \sqrt{(300 + 2 - 2)^2 + (400 + 3 - 2)^2} = 500.8004 \,\mathrm{mm}$$

Referring to Fig. a and using small angle analysis,

$$\phi = \frac{2}{403} = 0.004963$$
 rad  
 $\alpha = \frac{3}{300 + 6 - 2} = 0.009868$  rad

Average Normal Strain: Applying Eq. 2,

$$\alpha = \frac{3}{300 + 6 - 2} = 0.009868 \text{ rad}$$
  
**Normal Strain:** Applying Eq. 2,  

$$(\epsilon_{\text{avg}})_{BD} = \frac{L_{B'D'} - L_{BD}}{L_{BD}} = \frac{500.8004 - 500}{500} = 1.60(10^{-3}) \text{ mm/mm} \text{ Ans.}$$

Shear Strain: Referring to Fig. a,

$$(\gamma_B)_{xy} = \phi + \alpha = 0.004963 + 0.009868 = 0.0148$$
 rad Ans

$$\frac{2mm}{2mm} \frac{D'}{1 + 16mm} \frac{3mm}{1 + 16mm}$$

$$\frac{300mm}{2mm} \frac{2mm}{1 + 2mm} \frac{B'}{1 + 2mm} \frac{300mm}{B'} \frac{300mm}{3mm}$$

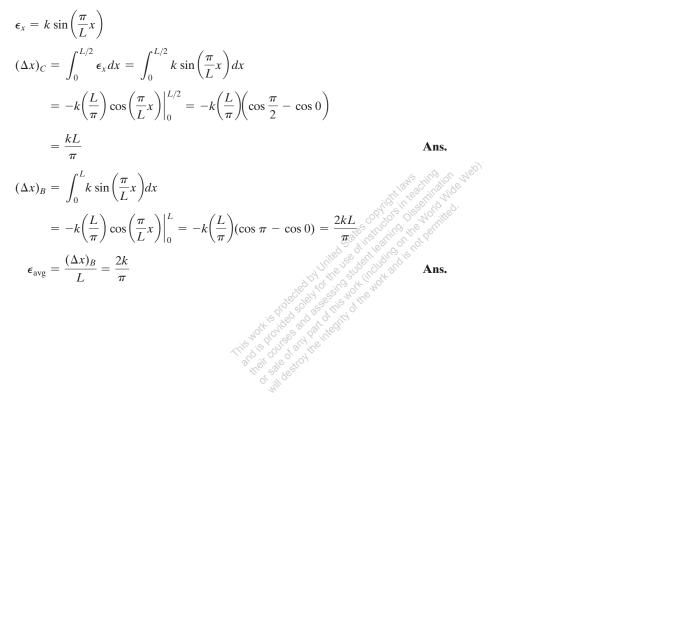
Ans:  $(\epsilon_{\rm avg})_{BD} = 1.60(10^{-3}) \, {\rm mm/mm},$  $(\gamma_B)_{xy} = 0.0148 \text{ rad}$ 

#### 2–31.

The nonuniform loading causes a normal strain in the shaft that can be expressed as  $\epsilon_x = k \sin\left(\frac{\pi}{L}x\right)$ , where k is a constant. Determine the displacement of the center C and the average normal strain in the entire rod.

# $A \xrightarrow{C} B \xrightarrow{C} B \xrightarrow{C} B$

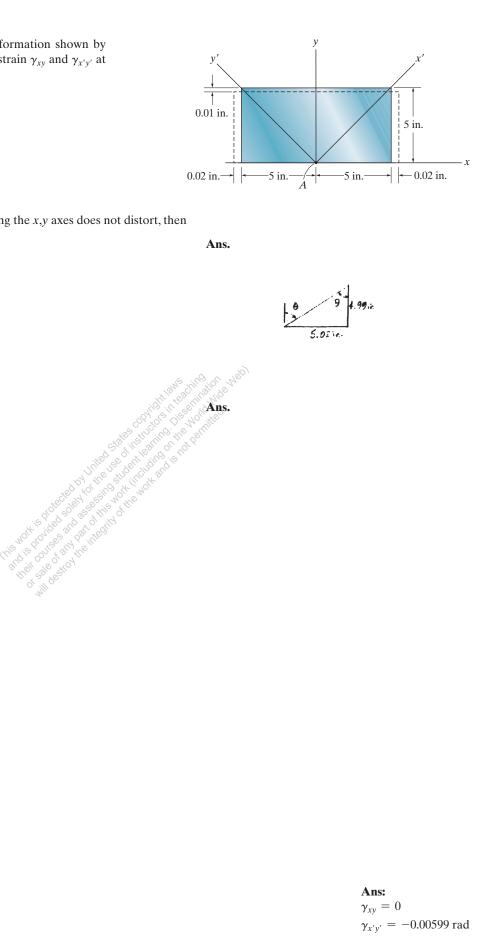
### SOLUTION





#### \*2-32.

The rectangular plate undergoes a deformation shown by the dashed lines. Determine the shear strain  $\gamma_{xy}$  and  $\gamma_{x'y'}$  at point *A*.



#### SOLUTION

 $\gamma_{xy} = 0$ 

 $\tan\theta = \frac{5.02}{4.99}$ 

 $\gamma_{x'y'}=\frac{\pi}{2}-2\theta$ 

 $\theta = 45.17^{\circ} = 0.7884 \text{ rad}$ 

 $=\frac{\pi}{2}-2(0.7884)$ 

= -0.00599 rad

Since the right angle of an element along the *x*,*y* axes does not distort, then

#### 2-33.

The fiber AB has a length L and orientation  $\theta$ . If its ends A and B undergo very small displacements  $u_A$  and  $v_B$ respectively, determine the normal strain in the fiber when it is in position A' B'.

#### SOLUTION

#### Geometry:

$$L_{A'B'} = \sqrt{(L\cos\theta - u_A)^2 + (L\sin\theta + v_B)^2}$$
  
=  $\sqrt{L^2 + u_A^2 + v_B^2 + 2L(v_B\sin\theta - u_A\cos\theta)}$ 

**Average Normal Strain:** 

$$\epsilon_{AB} = \frac{L_{A'B'} - L}{L}$$
$$= \sqrt{1 + \frac{u_A^2 + v_B^2}{L^2} + \frac{2(v_B \sin \theta - u_A \cos \theta)}{L} - 1}$$

Neglecting higher terms  $u_A^2$  and  $v_B^2$ 

$$\epsilon_{AB} = \left[1 + \frac{2(v_B \sin \theta - u_A \cos \theta)}{L}\right]^{\frac{1}{2}} - 1$$

Using the binomial theorem:

Neglecting higher terms 
$$u_A^2$$
 and  $v_B^2$   
 $\epsilon_{AB} = \left[1 + \frac{2(v_B \sin \theta - u_A \cos \theta)}{L}\right]^{\frac{1}{2}} - 1$   
Using the binomial theorem:  
 $\epsilon_{AB} = 1 + \frac{1}{2} \left(\frac{2v_B \sin \theta}{L} - \frac{2u_A \cos \theta}{L}\right) + \dots - 1$   
 $= \frac{v_B \sin \theta}{L} - \frac{u_A \cos \theta}{L}$ 
Ans.

B'

 $v_B$ 

R

θ

A  $u_A$ Α

Ans.

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#### 2–34.

If the normal strain is defined in reference to the final length  $\Delta s'$ , that is,

$$\epsilon' = \lim_{\Delta s' \to 0} \left( \frac{\Delta s' - \Delta s}{\Delta s'} \right)$$

instead of in reference to the original length, Eq. 2-2, show that the difference in these strains is represented as a second-order term, namely,  $\epsilon - \epsilon' = \epsilon \epsilon'$ .

#### SOLUTION

$$\epsilon = \frac{\Delta s' - \Delta s}{\Delta s}$$

$$\epsilon - \epsilon' = \frac{\Delta s' - \Delta s}{\Delta s} - \frac{\Delta s' - \Delta s}{\Delta s'}$$

$$= \frac{\Delta s'^2 - \Delta s \Delta s' - \Delta s' \Delta s + \Delta s^2}{\Delta s \Delta s'}$$

$$= \frac{\Delta s'^2 + \Delta s^2 - 2\Delta s' \Delta s}{\Delta s \Delta s'}$$

$$= \frac{(\Delta s' - \Delta s)^2}{\Delta s \Delta s'} = \left(\frac{\Delta s' - \Delta s}{\Delta s}\right) \left(\frac{\Delta s' - \Delta s}{\Delta s'}\right)$$

$$= \epsilon \epsilon'$$
(Q.E.D)

Ans: N/A