Introductory Econometrics A Modern Approach 5th Edition Wooldridge Solutions Manual

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CHAPTER 2

TEACHING NOTES

This is the chapter where I expect students to follow most, if not all, of the algebraic derivations. In class I like to derive at least the unbiasedness of the OLS slope coefficient, and usually I derive the variance. At a minimum, I talk about the factors affecting the variance. To simplify the notation, after I emphasize the assumptions in the population model, and assume random sampling, I just condition on the values of the explanatory variables in the sample. Technically, this is justified by random sampling because, for example, $E(u_i|x_1,x_2,...,x_n) = E(u_i|x_i)$ by independent sampling. I find that students are able to focus on the key assumption SLR.4 and subsequently take my word about how conditioning on the independent variables in the sample is harmless. (If you prefer, the appendix to Chapter 3 does the conditioning argument carefully.) Because statistical inference is no more difficult in multiple regression than in simple regression, I postpone inference until Chapter 4. (This reduces redundancy and allows you to focus on the interpretive differences between simple and multiple regression.)

You might notice how, compared with most other texts, I use relatively few assumptions to derive the unbiasedness of the OLS slope estimator, followed by the formula for its variance. This is because I do not introduce redundant or unnecessary assumptions. For example, once SLR.4 is assumed, nothing further about the relationship between u and x is needed to obtain the unbiasedness of OLS under random sampling.

Incidentally, one of the uncomfortable facts about finite-sample analysis is that there is a difference between an estimator that is unbiased conditional on the outcome of the covariates and one that is unconditionally unbiased. If the distribution of the x_i is such that they can all equal the same value with positive probability – as is the case with discreteness in the distribution – then the unconditional expectation does not really exist. Or, if it is made to exist then the estimator is not unbiased. I do not try to explain these subtleties in an introductory course, but I have had instructors ask me about the difference.

SOLUTIONS TO PROBLEMS

- **2.1** (i) Income, age, and family background (such as number of siblings) are just a few possibilities. It seems that each of these could be correlated with years of education. (Income and education are probably positively correlated; age and education may be negatively correlated because women in more recent cohorts have, on average, more education; and number of siblings and education are probably negatively correlated.)
- (ii) Not if the factors we listed in part (i) are correlated with *educ*. Because we would like to hold these factors fixed, they are part of the error term. But if u is correlated with *educ* then $E(u|educ) \neq 0$, and so SLR.4 fails.
- **2.2** In the equation $y = \beta_0 + \beta_1 x + u$, add and subtract α_0 from the right hand side to get $y = (\alpha_0 + \beta_0) + \beta_1 x + (u \alpha_0)$. Call the new error $e = u \alpha_0$, so that E(e) = 0. The new intercept is $\alpha_0 + \beta_0$, but the slope is still β_1 .
- **2.3** (i) Let $y_i = GPA_i$, $x_i = ACT_i$, and n = 8. Then $\overline{x} = 25.875$, $\overline{y} = 3.2125$, $\sum_{i=1}^{n} (x_i \overline{x})(y_i \overline{y}) = 3.2125$
- 5.8125, and $\sum_{i=1}^{n} (x_i \overline{x})^2 = 56.875$. From equation (2.9), we obtain the slope as $\hat{\beta}_1 =$
- $5.8125/56.875 \approx .1022$, rounded to four places after the decimal. From (2.17), $\hat{\beta}_0 = \overline{y} \hat{\beta}_1 \overline{x}$ $\approx 3.2125 (.1022)25.875 \approx .5681$. So we can write

$$GPA = .5681 + .1022 ACT$$

 $n = 8$.

The intercept does not have a useful interpretation because ACT is not close to zero for the population of interest. If ACT is 5 points higher, \overrightarrow{GPA} increases by .1022(5) = .511.

(ii) The fitted values and residuals — rounded to four decimal places — are given along with the observation number i and GPA in the following table:

i	GPA	GPA	û
1	2.8	2.7143	.0857
2	3.4	3.0209	.3791
3	3.0	3.2253	2253
4	3.5	3.3275	.1725
5	3.6	3.5319	.0681
6	3.0	3.1231	1231
7	2.7	3.1231	4231
8	3.7	3.6341	.0659

You can verify that the residuals, as reported in the table, sum to -.0002, which is pretty close to zero given the inherent rounding error.

(iii) When
$$ACT = 20$$
, $GPA = .5681 + .1022(20) \approx 2.61$.

(iv) The sum of squared residuals, $\sum_{i=1}^{n} \hat{u}_{i}^{2}$, is about .4347 (rounded to four decimal places),

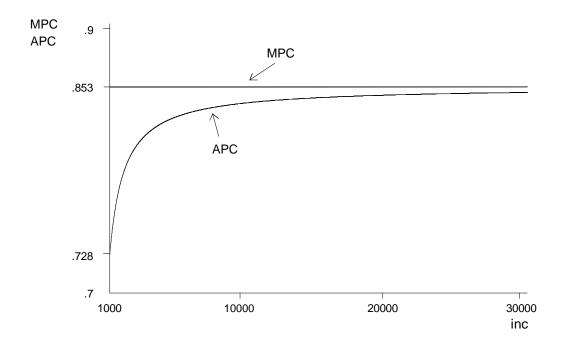
and the total sum of squares, $\sum_{i=1}^{n} (y_i - \overline{y})^2$, is about 1.0288. So the *R*-squared from the regression is

$$R^2 = 1 - SSR/SST \approx 1 - (.4347/1.0288) \approx .577.$$

Therefore, about 57.7% of the variation in *GPA* is explained by *ACT* in this small sample of students.

- **2.4** (i) When cigs = 0, predicted birth weight is 119.77 ounces. When cigs = 20, $\overrightarrow{bwght} = 109.49$. This is about an 8.6% drop.
- (ii) Not necessarily. There are many other factors that can affect birth weight, particularly overall health of the mother and quality of prenatal care. These could be correlated with cigarette smoking during birth. Also, something such as caffeine consumption can affect birth weight, and might also be correlated with cigarette smoking.
- (iii) If we want a predicted *bwght* of 125, then $cigs = (125 119.77)/(-.524) \approx -10.18$, or about -10 cigarettes! This is nonsense, of course, and it shows what happens when we are trying to predict something as complicated as birth weight with only a single explanatory variable. The largest predicted birth weight is necessarily 119.77. Yet almost 700 of the births in the sample had a birth weight higher than 119.77.

- (iv) 1,176 out of 1,388 women did not smoke while pregnant, or about 84.7%. Because we are using only cigs to explain birth weight, we have only one predicted birth weight at cigs = 0. The predicted birth weight is necessarily roughly in the middle of the observed birth weights at cigs = 0, and so we will under predict high birth rates.
- **2.5** (i) The intercept implies that when inc = 0, cons is predicted to be negative \$124.84. This, of course, cannot be true, and reflects that fact that this consumption function might be a poor predictor of consumption at very low-income levels. On the other hand, on an annual basis, \$124.84 is not so far from zero.
 - (ii) Just plug 30,000 into the equation: cons = -124.84 + .853(30,000) = 25,465.16 dollars.
- (iii) The MPC and the APC are shown in the following graph. Even though the intercept is negative, the smallest APC in the sample is positive. The graph starts at an annual income level of \$1,000 (in 1970 dollars).



- **2.6** (i) Yes. If living closer to an incinerator depresses housing prices, then being farther away increases housing prices.
- (ii) If the city chose to locate the incinerator in an area away from more expensive neighborhoods, then log(dist) is positively correlated with housing quality. This would violate SLR.4, and OLS estimation is biased.

- (iii) Size of the house, number of bathrooms, size of the lot, age of the home, and quality of the neighborhood (including school quality), are just a handful of factors. As mentioned in part (ii), these could certainly be correlated with dist [and log(dist)].
- **2.7** (i) When we condition on *inc* in computing an expectation, \sqrt{inc} becomes a constant. So $E(u|inc) = E(\sqrt{inc} \cdot e|inc) = \sqrt{inc} \cdot E(e|inc) = \sqrt{inc} \cdot 0$ because E(e|inc) = E(e) = 0.
- (ii) Again, when we condition on *inc* in computing a variance, \sqrt{inc} becomes a constant. So $Var(u|inc) = Var(\sqrt{inc} \cdot e|inc) = (\sqrt{inc})^2 Var(e|inc) = \sigma_e^2 inc$ because $Var(e|inc) = \sigma_e^2$.
- (iii) Families with low incomes do not have much discretion about spending; typically, a low-income family must spend on food, clothing, housing, and other necessities. Higher income people have more discretion, and some might choose more consumption while others more saving. This discretion suggests wider variability in saving among higher income families.
- **2.8** (i) From equation (2.66),

$$\tilde{\beta}_1 = \left(\sum_{i=1}^n x_i y_i\right) / \left(\sum_{i=1}^n x_i^2\right).$$

Plugging in $y_i = \beta_0 + \beta_1 x_i + u_i$ gives

$$\tilde{\beta}_1 = \left(\sum_{i=1}^n x_i (\beta_0 + \beta_1 x_i + u_i)\right) / \left(\sum_{i=1}^n x_i^2\right).$$

After standard algebra, the numerator can be written as

$$\beta_0 \sum_{i=1}^n x_i + \beta_1 \sum_{i=1}^n x_i^2 + \sum_{i=1}^n x_i u_i$$
.

Putting this over the denominator shows we can write $\tilde{\beta}_1$ as

$$\tilde{\beta}_1 = \beta_0 \left(\sum_{i=1}^n x_i \right) / \left(\sum_{i=1}^n x_i^2 \right) + \beta_1 + \left(\sum_{i=1}^n x_i u_i \right) / \left(\sum_{i=1}^n x_i^2 \right).$$

Conditional on the x_i , we have

$$E(\tilde{\beta}_1) = \beta_0 \left(\sum_{i=1}^n x_i \right) / \left(\sum_{i=1}^n x_i^2 \right) + \beta_1$$

because $E(u_i) = 0$ for all i. Therefore, the bias in $\tilde{\beta}_1$ is given by the first term in this equation. This bias is obviously zero when $\beta_0 = 0$. It is also zero when $\sum_{i=1}^n x_i = 0$, which is the same as $\overline{x} = 0$. In the latter case, regression through the origin is identical to regression with an intercept. (ii) From the last expression for $\tilde{\beta}_1$ in part (i) we have, conditional on the x_i ,

$$\operatorname{Var}(\tilde{\beta}_{1}) = \left(\sum_{i=1}^{n} x_{i}^{2}\right)^{-2} \operatorname{Var}\left(\sum_{i=1}^{n} x_{i} u_{i}\right) = \left(\sum_{i=1}^{n} x_{i}^{2}\right)^{-2} \left(\sum_{i=1}^{n} x_{i}^{2} \operatorname{Var}(u_{i})\right)$$
$$= \left(\sum_{i=1}^{n} x_{i}^{2}\right)^{-2} \left(\sigma^{2} \sum_{i=1}^{n} x_{i}^{2}\right) = \sigma^{2} / \left(\sum_{i=1}^{n} x_{i}^{2}\right).$$

(iii) From (2.57), $\operatorname{Var}(\hat{\beta}_1) = \sigma^2 / \left(\sum_{i=1}^n (x_i - \overline{x})^2 \right)$. From the hint, $\sum_{i=1}^n x_i^2 \ge \sum_{i=1}^n (x_i - \overline{x})^2$, and so $\operatorname{Var}(\tilde{\beta}_1) \le \operatorname{Var}(\hat{\beta}_1)$. A more direct way to see this is to write $\sum_{i=1}^n (x_i - \overline{x})^2 = \sum_{i=1}^n x_i^2 - n(\overline{x})^2$, which is less than $\sum_{i=1}^n x_i^2$ unless $\overline{x} = 0$.

- (iv) For a given sample size, the bias in $\tilde{\beta}_1$ increases as \overline{x} increases (holding the sum of the x_i^2 fixed). But as \overline{x} increases, the variance of $\hat{\beta}_1$ increases relative to $\text{Var}(\tilde{\beta}_1)$. The bias in $\tilde{\beta}_1$ is also small when β_0 is small. Therefore, whether we prefer $\tilde{\beta}_1$ or $\hat{\beta}_1$ on a mean squared error basis depends on the sizes of β_0 , \overline{x} , and n (in addition to the size of $\sum_{i=1}^n x_i^2$).
- **2.9** (i) We follow the hint, noting that $\overline{c_1 y} = c_1 \overline{y}$ (the sample average of $c_1 y_i$ is c_1 times the sample average of y_i) and $\overline{c_2 x} = c_2 \overline{x}$. When we regress $c_1 y_i$ on $c_2 x_i$ (including an intercept) we use equation (2.19) to obtain the slope:

$$\begin{split} \tilde{\beta}_{1} &= \frac{\sum_{i=1}^{n} (c_{2}x_{i} - c_{2}x)(c_{1}\overline{y}_{i} - c_{1}\overline{y})}{\sum_{i=1}^{n} (c_{2}x_{i} - c_{2}\overline{x})^{2}} = \frac{\sum_{i=1}^{n} c_{1}c_{2}(x_{i} - \overline{x})(y_{i} - \overline{y})}{\sum_{i=1}^{n} c_{2}^{2}(x_{i} - \overline{x})^{2}} \\ &= \frac{c_{1}}{c_{2}} \cdot \frac{\sum_{i=1}^{n} (x_{i} - \overline{x})(y_{i} - \overline{y})}{\sum_{i=1}^{n} (x_{i} - \overline{x})^{2}} = \frac{c_{1}}{c_{2}} \hat{\beta}_{1}. \end{split}$$

From (2.17), we obtain the intercept as $\tilde{\beta}_0 = (c_1 \, \overline{y}) - \tilde{\beta}_1(c_2 \, \overline{x}) = (c_1 \, \overline{y}) - [(c_1/c_2) \, \hat{\beta}_1](c_2 \, \overline{x}) = c_1(\overline{y}) - \hat{\beta}_1(\overline{x}) = c_1(\overline{y}) - \hat{\beta}_1(\overline{y}) = c_1(\overline{y}) + c_1(\overline{y}) = c_1(\overline{y}) + c_1(\overline{y}) = c_1(\overline{y$

- (ii) We use the same approach from part (i) along with the fact that $(\overline{c_1+y})=c_1+\overline{y}$ and $(\overline{c_2+x})=c_2+\overline{x}$. Therefore, $(c_1+y_i)-(\overline{c_1+y})=(c_1+y_i)-(c_1+\overline{y})=y_i-\overline{y}$ and $(c_2+x_i)-(\overline{c_2+x})=x_i-\overline{x}$. So c_1 and c_2 entirely drop out of the slope formula for the regression of (c_1+y_i) on (c_2+x_i) , and $\tilde{\beta}_1=\hat{\beta}_1$. The intercept is $\tilde{\beta}_0=(\overline{c_1+y})-\tilde{\beta}_1(\overline{c_2+x})=(c_1+\overline{y})-\hat{\beta}_1(c_2+\overline{x})=(\overline{y}-\hat{\beta}_1\overline{x})+c_1-c_2\hat{\beta}_1=\hat{\beta}_0+c_1-c_2\hat{\beta}_1$, which is what we wanted to show.
- (iii) We can simply apply part (ii) because $\log(c_1y_i) = \log(c_1) + \log(y_i)$. In other words, replace c_1 with $\log(c_1)$, y_i with $\log(y_i)$, and set $c_2 = 0$.
- (iv) Again, we can apply part (ii) with $c_1 = 0$ and replacing c_2 with $\log(c_2)$ and x_i with $\log(x_i)$. If $\hat{\beta}_0$ and $\hat{\beta}_1$ are the original intercept and slope, then $\tilde{\beta}_1 = \hat{\beta}_1$ and $\tilde{\beta}_0 = \hat{\beta}_0 \log(c_2)\hat{\beta}_1$.
- **2.10** (i) This derivation is essentially done in equation (2.52), once $(1/SST_x)$ is brought inside the summation (which is valid because SST_x does not depend on *i*). Then, just define $w_i = d_i/SST_x$.
- (ii) Because $\text{Cov}(\hat{\beta}_1, \overline{u}) = \text{E}[(\hat{\beta}_1 \beta_1)\overline{u}]$, we show that the latter is zero. But, from part (i), $\text{E}[(\hat{\beta}_1 \beta_1)\overline{u}] = \text{E}\Big[\Big(\sum_{i=1}^n w_i u_i\Big)\overline{u}\Big] = \sum_{i=1}^n w_i \text{E}(u_i\overline{u})$. Because the u_i are pairwise uncorrelated (they are independent), $\text{E}(u_i\overline{u}) = \text{E}(u_i^2/n) = \sigma^2/n$ (because $\text{E}(u_i u_h) = 0$, $i \neq h$). Therefore, $\sum_{i=1}^n w_i \text{E}(u_i\overline{u}) = \sum_{i=1}^n w_i (\sigma^2/n) = (\sigma^2/n) \sum_{i=1}^n w_i = 0$.
- (iii) The formula for the OLS intercept is $\hat{\beta}_0 = \overline{y} \hat{\beta}\overline{x}$ and, plugging in $\overline{y} = \beta_0 + \beta_1\overline{x} + \overline{u}$ gives $\hat{\beta}_0 = (\beta_0 + \beta_1\overline{x} + \overline{u}) \hat{\beta}_1\overline{x} = \beta_0 + \overline{u} (\hat{\beta}_1 \beta_1)\overline{x}$.
 - (iv) Because $\hat{\beta}_1$ and \overline{u} are uncorrelated,

 $\operatorname{Var}(\hat{\beta}_0) = \operatorname{Var}(\overline{u}) + \operatorname{Var}(\hat{\beta}_1)\overline{x}^2 = \sigma^2/n + (\sigma^2/\operatorname{SST}_x)\overline{x}^2 = \sigma^2/n + \sigma^2\overline{x}^2/\operatorname{SST}_x,$ which is what we wanted to show.

(v) Using the hint and substitution gives $\operatorname{Var}(\hat{\beta}_0) = \sigma^2 [\left(\operatorname{SST}_x/n\right) + \overline{x}^2]/\operatorname{SST}_x$ = $\sigma^2 \left[\left(n^{-1}\sum_{i=1}^n x_i^2 - \overline{x}^2\right) + \overline{x}^2\right]/\operatorname{SST}_x = \sigma^2 \left(n^{-1}\sum_{i=1}^n x_i^2\right)/\operatorname{SST}_x$.

- **2.11** (i) We would want to randomly assign the number of hours in the preparation course so that *hours* is independent of other factors that affect performance on the SAT. Then, we would collect information on SAT score for each student in the experiment, yielding a data set $\{(sat_i, hours_i): i = 1,...,n\}$, where n is the number of students we can afford to have in the study. From equation (2.7), we should try to get as much variation in $hours_i$ as is feasible.
- (ii) Here are three factors: innate ability, family income, and general health on the day of the exam. If we think students with higher native intelligence think they do not need to prepare for the SAT, then ability and *hours* will be negatively correlated. Family income would probably be positively correlated with *hours*, because higher income families can more easily afford preparation courses. Ruling out chronic health problems, health on the day of the exam should be roughly uncorrelated with hours spent in a preparation course.
- (iii) If preparation courses are effective, β_1 should be positive: other factors equal, an increase in *hours* should increase *sat*.
- (iv) The intercept, β_0 , has a useful interpretation in this example: because E(u) = 0, β_0 is the average SAT score for students in the population with *hours* = 0.
- **2.12** (i) I will show the result without using calculus. Let \bar{y} be the sample average of the y_i and write

$$\sum_{i=1}^{n} (y_i - b_0)^2 = \sum_{i=1}^{n} [(y_i - \overline{y}) + (\overline{y} - b_0)]^2$$

$$= \sum_{i=1}^{n} (y_i - \overline{y})^2 + 2\sum_{i=1}^{n} (y_i - \overline{y})(\overline{y} - b_0) + \sum_{i=1}^{n} (\overline{y} - b_0)^2$$

$$= \sum_{i=1}^{n} (y_i - \overline{y})^2 + 2(\overline{y} - b_0)\sum_{i=1}^{n} (y_i - \overline{y}) + n(\overline{y} - b_0)^2$$

$$= \sum_{i=1}^{n} (y_i - \overline{y})^2 + n(\overline{y} - b_0)^2$$

where we use the fact (see Appendix A) that $\sum_{i=1}^{n} (y_i - \overline{y}) = 0$ always. The first term does not depend on b_0 and the second term, $n(\overline{y} - b_0)^2$, which is nonnegative, is clearly minimized when $b_0 = \overline{y}$.

(ii) If we define $\tilde{u}_i = y_i - \overline{y}$ then $\sum_{i=1}^n \tilde{u}_i = \sum_{i=1}^n (y_i - \overline{y})$ and we already used the fact that this sum is zero in the proof in part (i).

SOLUTIONS TO COMPUTER EXERCISES

- **C2.1** (i) The average *prate* is about 87.36 and the average *mrate* is about .732.
 - (ii) The estimated equation is

$$prate = 83.05 + 5.86 \text{ mrate}$$

 $n = 1,534, R^2 = .075.$

- (iii) The intercept implies that, even if *mrate* = 0, the predicted participation rate is 83.05 percent. The coefficient on *mrate* implies that a one-dollar increase in the match rate a fairly large increase is estimated to increase *prate* by 5.86 percentage points. This assumes, of course, that this change *prate* is possible (if, say, *prate* is already at 98, this interpretation makes no sense).
- (iv) If we plug mrate = 3.5 into the equation we get $pr\hat{a}te = 83.05 + 5.86(3.5) = 103.59$. This is impossible, as we can have at most a 100 percent participation rate. This illustrates that, especially when dependent variables are bounded, a simple regression model can give strange predictions for extreme values of the independent variable. (In the sample of 1,534 firms, only 34 have $mrate \ge 3.5$.)
- (v) *mrate* explains about 7.5% of the variation in *prate*. This is not much, and suggests that many other factors influence 401(k) plan participation rates.
- **C2.2** (i) Average salary is about 865.864, which means \$865,864 because *salary* is in thousands of dollars. Average *ceoten* is about 7.95.
 - (ii) There are five CEOs with ceoten = 0. The longest tenure is 37 years.
 - (iii) The estimated equation is

$$\log(salary) = 6.51 + .0097 \ ceoten$$

 $n = 177, \ R^2 = .013.$

We obtain the approximate percentage change in *salary* given $\Delta ceoten = 1$ by multiplying the coefficient on *ceoten* by 100, 100(.0097) = .97%. Therefore, one more year as CEO is predicted to increase salary by almost 1%.

C2.3 (i) The estimated equation is

steep =
$$3,586.4 - .151 \text{ totwrk}$$

 $n = 706, R^2 = .103.$

The intercept implies that the estimated amount of sleep per week for someone who does not work is 3,586.4 minutes, or about 59.77 hours. This comes to about 8.5 hours per night.

- (ii) If someone works two more hours per week then $\Delta totwrk = 120$ (because totwrk is measured in minutes), and so $\Delta sleep = -.151(120) = -18.12$ minutes. This is only a few minutes a night. If someone were to work one more hour on each of five working days, $\Delta sleep = -.151(300) = -45.3$ minutes, or about five minutes a night.
- **C2.4** (i) Average salary is about \$957.95 and average IQ is about 101.28. The sample standard deviation of IQ is about 15.05, which is pretty close to the population value of 15.
 - (ii) This calls for a level-level model:

$$wage = 116.99 + 8.30 IQ$$

$$n = 935, R^2 = .096.$$

An increase in IQ of 15 increases predicted monthly salary by 8.30(15) = \$124.50 (in 1980 dollars). IQ score does not even explain 10% of the variation in wage.

(iii) This calls for a log-level model:

$$\log(wage) = 5.89 + .0088 IQ$$

$$n = 935, R^2 = .099.$$

If $\Delta IQ = 15$ then $\Delta \log(wage) = .0088(15) = .132$, which is the (approximate) proportionate change in predicted wage. The percentage increase is therefore approximately 13.2.

C2.5 (i) The constant elasticity model is a log-log model:

$$\log(rd) = \beta_0 + \beta_1 \log(sales) + u,$$

where β_1 is the elasticity of rd with respect to sales.

(ii) The estimated equation is

$$\log(rd) = -4.105 + 1.076 \log(sales)$$

$$n = 32, R^2 = .910.$$

The estimated elasticity of rd with respect to sales is 1.076, which is just above one. A one percent increase in sales is estimated to increase rd by about 1.08%.

- **C2.6** (i) It seems plausible that another dollar of spending has a larger effect for low-spending schools than for high-spending schools. At low-spending schools, more money can go toward purchasing more books, computers, and for hiring better qualified teachers. At high levels of spending, we would expend little, if any, effect because the high-spending schools already have high-quality teachers, nice facilities, plenty of books, and so on.
 - (ii) If we take changes, as usual, we obtain $\Delta math 10 = \beta_1 \Delta \log(expend) \approx (\beta_1/100)(\% \Delta expend),$

just as in the second row of Table 2.3. So, if $\%\Delta expend = 10$, $\Delta math 10 = \beta_1/10$.

(iii) The regression results are

$$math10 = -69.34 + 11.16 \log(expend)$$

 $n = 408, R^2 = .0297$

- (iv) If *expend* increases by 10 percent, *math*10 increases by about 1.1 percentage points. This is not a huge effect, but it is not trivial for low-spending schools, where a 10 percent increase in spending might be a fairly small dollar amount.
- (v) In this data set, the largest value of *math10* is 66.7, which is not especially close to 100. In fact, the largest fitted values is only about 30.2.
- **C2.7** (i) The average gift is about 7.44 Dutch guilders. Out of 4,268 respondents, 2,561 did not give a gift, or about 60 percent.
- (ii) The average mailings per year is about 2.05. The minimum value is .25 (which presumably means that someone has been on the mailing list for at least four years) and the maximum value is 3.5.
 - (iii) The estimated equation is

gift =
$$2.01 + 2.65$$
 mailsyear
 $n = 4,268$, $R^2 = .0138$

- (iv) The slope coefficient from part (iii) means that each mailing per year is associated with perhaps even "causes" an estimated 2.65 additional guilders, on average. Therefore, if each mailing costs one guilder, the expected profit from each mailing is estimated to be 1.65 guilders. This is only the average, however. Some mailings generate no contributions, or a contribution less than the mailing cost; other mailings generated much more than the mailing cost.
- (v) Because the smallest *mailsyear* in the sample is .25, the smallest predicted value of *gifts* is $2.01 + 2.65(.25) \approx 2.67$. Even if we look at the overall population, where some people have received no mailings, the smallest predicted value is about two. So, with this estimated equation, we never predict zero charitable gifts.

C2.8 There is no "correct" answer to this question because all answers depend on how the random outcomes are generated. I used Stata 11 and, before generating the outcomes on the x_i , I set the seed to the value 123. I reset the seed to 123 to generate the outcomes on the u_i . Specifically, to answer parts (i) through (v), I used the sequence of commands

```
set obs 500
set seed 123
gen x = 10*runiform()
sum x
set seed 123
gen u = 6*rnormal()
sum u
gen y = 1 + 2*x + u
reg y x
predict uh, resid
gen x_uh = x*uh
sum uh x_uh
gen x_u = x*u
sum u x_u
```

- (i) The sample mean of the x_i is about 4.912 with a sample standard deviation of about 2.874.
- (ii) The sample average of the u_i is about .221, which is pretty far from zero. We do not get zero because this is just a sample of 500 from a population with a zero mean. The current sample is "unlucky" in the sense that the sample average is far from the population average. The sample standard deviation is about 5.768, which is nontrivially below 6, the population value.
- (iii) After generating the data on y_i and running the regression, I get, rounding to three decimal places,

$$\hat{\beta}_0 = 1.862$$
 and $\hat{\beta}_1 = 1.870$

The population values are 1 and 2, respectively. Thus, the estimated intercept based on this sample of data is well above the population value. The estimated slope is somewhat below the population value, 2. When we sample from a population our estimates contain sampling error; that is why the estimates differ from the population values.

(iv) When I use the command sum uh x_uh and multiply by 500 I get, using scientific notation, sums equal to 4.181e-06 and .00003776, respectively. These are zero for practical purposes, and differ from zero only due to rounding inherent in the machine imprecision (which is unimportant).

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- (v) We already computed the sample average of the u_i in part (ii). When we multiply by 500 the sample average is about 110.74. The sum of $x_i u_i$ is about 6.46. Neither is close to zero, and nothing says they should be particularly close.
- (vi) For this part I set the seed to 789. The sample average and standard deviation of the x_i are about 5.030 and 2.913; those for the u_i are about -.077 and 5.979. When I generated the y_i and run the regression I get

$$\hat{\beta}_0 = .701$$
 and $\hat{\beta}_1 = 2.044$

These are different from those in part (iii) because they are obtained from a different random sample. Here, for both the intercept and slope, we get estimates that are much closer to the population values. Of course, in practice we would never know that.