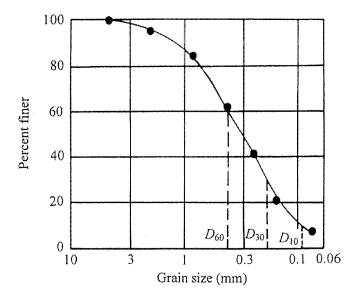
#### Chapter 2

- 2.1 a. False
  - b. True
  - c. False
  - d. False
  - e. True
- 2.2 a.

| U.S.<br>sieve<br>No. | Mass of soil<br>retained on<br>each sieve (g) | Percent retained on each sieve | Percent<br>finer |
|----------------------|---|--------------------------------|------------------|
| 4                    | 0.0   | 0.0                            | 100.0            |
| 10                   | 21.6  | 4.8                            | 95.2             |
| 20                   | 49.5  | 11.0                           | 84.2             |
| 40                   | 102.6   | 22.8                           | 61.4             |
| 60                   | 89.1  | 19.8                           | 41.6             |
| 100                  | 95.6  | 21.2                           | 20.4             |
| 200                  | 60.4  | 13.4                           | 7.0              |
| Pan                  | 31.2  | 7.0                            |                  |
|                      | Σ450  |                                |                  |

The grain-size distribution is shown.



b. From the figure on Page 1,  $D_{60} = 0.41$  mm,  $D_{30} = 0.185$  mm,  $D_{10} = 0.09$  mm

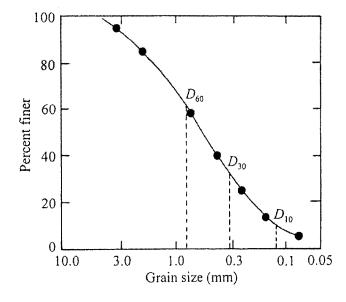
c. 
$$C_u = \frac{D_{60}}{D_{10}} = \frac{0.41}{0.09} = 4.56$$

d. 
$$C_c = \frac{D_{30}^2}{(D_{60})(D_{10})} = \frac{0.185^2}{(0.41)(0.09)} = \mathbf{0.928}$$

2.3 a.

| U.S.  | Mass of soil   | _                |         |
|-------|----------------|------------------|---------|
| sieve | retained on    | Percent retained | Percent |
| No.   | each sieve (g) | on each sieve    | finer   |
| 4     | 0.0            | 0.00             | 100.00  |
| 6     | 30.0           | 6.00             | 94.00   |
| 10    | 48.7           | 9.74             | 84.26   |
| 20    | 127.3          | 25.46            | 58.80   |
| 40    | 96.8           | 19.36            | 39.44   |
| 60    | 76.6           | 15.32            | 24.12   |
| 100   | 55,2           | 11.04            | 13.08   |
| 200   | 43.4           | 8.68             | 4.40    |
| Pan   | 22.0           | 4.40             | 0.00    |
|       | Σ500           |                  |         |

The grain-size distribution is shown.



b. From the figure,  $D_{60} = 0.82 \text{ mm}$ ,  $D_{30} = 0.31 \text{ mm}$ ,  $D_{10} = 0.12 \text{ mm}$ 

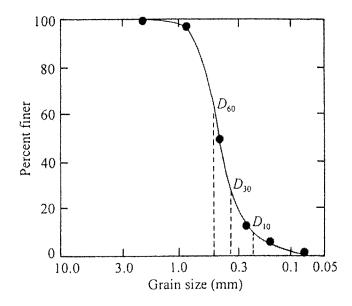
c. 
$$C_u = \frac{D_{60}}{D_{10}} = \frac{0.82}{0.12} = 6.83$$

d. 
$$C_c = \frac{D_{30}^2}{(D_{60})(D_{10})} = \frac{0.31^2}{(0.82)(0.12)} = \mathbf{0.98}$$

2.4 a.

| U.S.  | Mass of soil   |                  |         |
|-------|----------------|------------------|---------|
| sieve | retained on    | Percent retained | Percent |
| No.   | each sieve (g) | on each sieve    | finer   |
| 4     | 0.0            | 0.00             | 100.00  |
| 6     | 0.0            | 0.00             | 100.00  |
| 10    | 0.0            | 0.00             | 100.00  |
| 20    | 9.1            | 1.82             | 98.18   |
| 40    | 249.4          | 49.88            | 48.30   |
| 60    | 179.8          | 35.96            | 12.34   |
| 100   | 22.7           | 4.54             | 7.80    |
| 200   | 15.5           | 3.10             | 4.70    |
| Pan   | 23.5           | 4.70             | 0.00    |
|       | Σ500           |                  |         |

The grain-size distribution is shown in the figure.

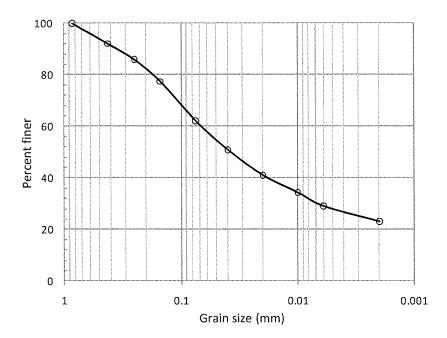


b. From the graph,  $D_{60} = 0.48 \text{ mm}$ ,  $D_{30} = 0.33 \text{ mm}$ ,  $D_{10} = 0.23 \text{ mm}$ 

c. 
$$C_u = \frac{0.48}{0.23} = 2.09$$

d. 
$$C_c = \frac{0.33^2}{(0.48)(0.23)} = 0.99$$

2.5 The grain-size distribution curve is shown.



- From the figure: Percent finer than 2 mm = 100%Percent finer than 0.06 mm = 58%Percent finer than 0.002 mm = 23%
- So, Gravel: 0%Sand: 100 - 58 = 42%

Silt: 58 - 23 = 35%Clay: 23 - 0 = 23%

- 2.6 Refer to the figure in Problem 2.5.
  - From Table 2.1: Portion larger than 2 mm is gravel
  - (USDA system) Portion between 2 mm and 0.05 mm is sand Portion between 0.05 mm and 0.002 mm is silt Portion smaller than 0.002 mm is clay

From the figure: Percent finer than 2 mm = 100%

Percent finer than 0.06 mm = 54%Percent finer than 0.002 mm = 23%

So, Gravel: 0%

Sand: 100 - 54 = 46%Silt: 54 - 23 = 31%Clay: 23 - 0 = 23%

2.7 Refer to the figure in Problem 2.5.

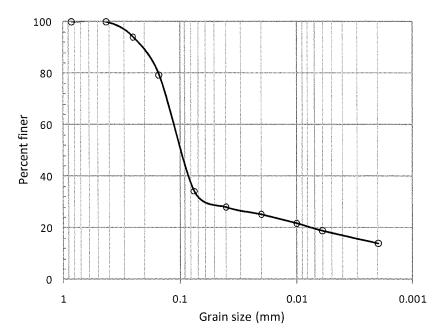
From the figure: Percent finer than 2 mm = 100%

Percent finer than 0.06 mm = 62%Percent finer than 0.002 mm = 23%

So, Gravel: 0%

Sand: 100 - 62 = 38%Silt: 62 - 23 = 39%Clay: 23 - 0 = 23%

2.8 The grain-size distribution is shown.



From the figure: Percent finer than 2 mm = 100%

Percent finer than 0.06 mm = 30% Percent finer than 0.002 mm = 14%

So, Gravel: 0%

Sand: 100 - 30 = 70%Silt: 40 - 14 = 16%Clay: 14 - 0 = 14%

2.9 Refer to the figure in Problem 2.8.

From the figure: Percent finer than 2 mm = 100%

Percent finer than 0.075 mm = 29%Percent finer than 0.002 mm = 14%

So, Gravel: 0%

Sand: 100 - 29 = 71%Silt: 29 - 14 = 15%Clay: 14 - 0 = 14%

2.10 Refer to the figure in Problem 2.8.

From the figure: Percent finer than 2 mm = 100%

Percent finer than 0.075 mm = 34%Percent finer than 0.002 mm = 14%

So, Gravel: 0%

Sand: 100 - 34 = 66%Silt: 34 - 14 = 20%Clay: 14 - 0 = 14%

2.11 <u>Soil A</u>:

Percent passing 75 mm sieve = 100 (percent of gravel + sand + fines = 100)

Percent passing 4.75 (No. 4) sieve = 67.5 (percent of sand + fines = 67.5)

Therefore percent of gravel = 32.5

Percent passing 0.075 mm (No. 200) sieve = 8.5

Therefore percent of fines = 8.5 and percent of sand = 59.0

Soil A contains 32.5% gravel, 59.0 % sand and 8.5% fines.

#### Soil B:

Following the same method, Percent of gravel 
$$+$$
 sand  $+$  fines  $=$  100  
Percent of sand  $+$  fines  $=$  100  
Percent of fines  $=$  0

Therefore, Soil B consists of 100% sand.

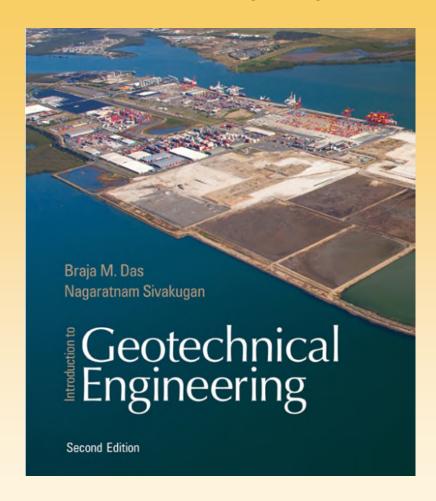
2.12 Percent of gravel + sand + fines = 100

Percent of sand + fines = 63

Percent of fines = 16

Therefore, percentages of gravel, sand and fines within the soil are 37, 47, and 16, respectively.

- 2.13 a. A has the largest (50%) percentage of gravel.
  - b. C is entirely sand, with grains in the size range of 0.2–4.75 mm.
  - c. Only D contains clay fractions (less than 0.002 mm) of about 35%.
  - d. In Soil A, there are no grains in the size range of 0.2-5.0 mm. It is known as gap graded.



Chapter 2
Grain-Size
Analysis



## Learning Objectives and Outline

- \* To learn the size ranges for gravels, sands, and fines
- \* To understand how soils are formed
- \* To be able to develop the grain-size distribution curve

#### 2.1 Introduction

- \* In engineering, soil is defined as "an uncemented aggregate of mineral grains and decayed organic matter (solid particles) with liquid and gas in the empty spaces between the solid particles."
- \* The grain-size distribution in soil influences its physical properties, such as compressibility and shear strength.

### 2.2 Soil-Grain Size

Several organizations have developed *soil-separate-size limits:* 

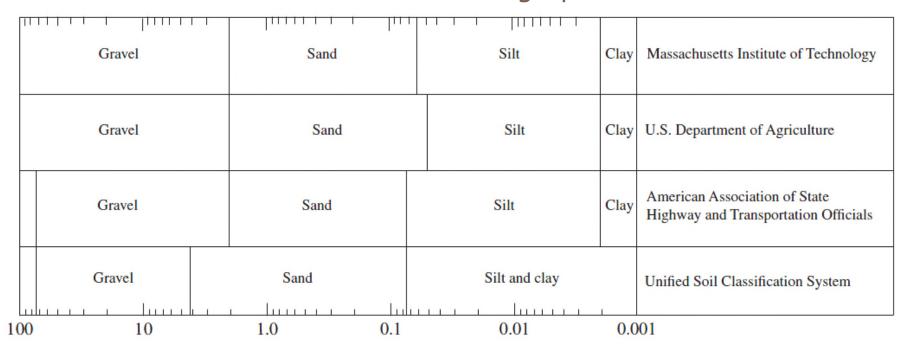
| - |      |      |      |
|---|------|------|------|
|   | POIN | CIZO | (mm) |
| u | all  | 3146 |      |
| _ |      |      |      |

| Name of organization   | Gravel       | Sand          | Silt                                 | Clay    |
|--|--------------|---------------|--------------------------------------|---------|
| Massachusetts Institute of<br>Technology (MIT)   | >2           | 2 to 0.06     | 0.06 to 0.002                        | < 0.002 |
| U.S. Department of<br>Agriculture (USDA)   | >2           | 2 to 0.05     | 0.05 to 0.002                        | < 0.002 |
| American Association<br>of State Highway and<br>Transportation Officials<br>(AASHTO)                   | 76.2 to 2    | 2 to 0.075    | 0.075 to 0.002                       | <0.002  |
| Unified Soil Classification<br>System (U.S. Army<br>Corps of Engineers, U.S.<br>Bureau of Reclamation) | 76.2 to 4.75 | 4.75 to 0.075 | Fines (i.e., silts and clays) <0.075 |         |

### 2.2 Soil-Grain Size Cont'd

 \* American Society of Testing and Materials (ASTM) adopted the Unified Soil Classification System.

#### Below are the size limits in graphical form:



#### 2.2 Soil-Grain Size Cont'd

**Gravel:** Pieces of rocks with occasional grains of quartz, feldspar, and other minerals.

**Sand:** Grains that are mostly made of quartz and feldspar. Other minerals may be present at times.

**Silts:** The microscopic soil fractions which consist of very fine quartz grains and some flake-shaped grains that are micaceous mineral fragments.

**Clays:** Mostly flake-shaped microscopic grains of mica, clay minerals, and other minerals. Grains are classified as *clay* based on their size; they do not always contain *clay minerals*.

#### 2.2 Soil-Grain Size Cont'd

- \* Three major types of clay minerals:
  - \* Kaolinite
  - \* Illite
  - \* Montmorillonite
- \* Their mineralogy, flakiness, and the large surface areas make the clays plastic and cohesive.
- \* Montmorillonite clays can swell in the presence of water which enters between layers. These expansive clays cause billions of dollars worth of annual damage to roads and buildings.

## 2.3 General Soil Deposits

Most of the soils that cover the earth are formed by the weathering of various rocks. The two general types of weathering are:

- \* **Mechanical Weathering**: Physical forces such as running water, wind, ocean waves, glacier ice and frost action break down rocks into smaller pieces
- \* **Chemical Weathering**: Chemical decomposition of the original rock. In this case, the original materials may be changed to something entirely different

## 2.3 General Soil Deposits Cont'd

- \* When the soil produced by the weathering process is transported by physical agents to other places, these deposits are called *transported soils*.
  - \* Alluvial: Deposited by running water
  - \* **Glacial:** Deposited by glacier action
  - \* **Aeolian:** Deposited by wind action
- \* The soils that stay in the place of their formation are referred to as *residual soils*.

## 2.3 General Soil Deposits Cont'd

- \* In addition to transported and residual soils, there are peats and organic soils.
- \* Organic soils have the following characteristics:
  - \* Usually found in low-lying areas with a high ground water table
  - \* Moisture content ranges from 200%-300%
  - \* Highly compressible
  - \* Under loads, a large amount of settlement is derived from secondary consolidation

#### 2.4 Some Local Terms for Soils

- 1. Caliche: Mostly found in the desert. Derived from Latin word "calix," meaning lime
- 2. Gumbo: Highly plastic, clayey
- 3. Adobe: Highly plastic, clayey soil found in southwestern U.S.
- 4. Terra Rosa: Residual, red, derived from limestone and dolomite
- 5. Muck: Organic soil with a very high moisture content
- 6. Muskeg: Organic soil deposit
- 7. Saprolite: Derived from mostly insoluble rock, residual
- 8. Loam: Mixture of various grain sizes
- 9. Laterite: Iron oxide and aluminum oxide accumulation, leaching of silica

## 2.5 Grain-Size Analysis

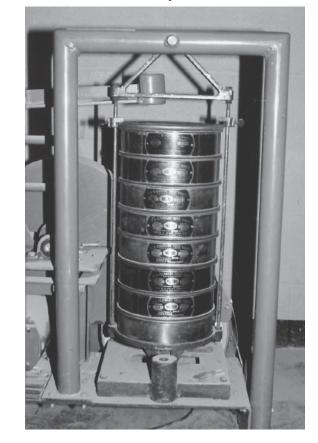
\* The size of grains may widely vary in a natural soil deposit.

 Determining the nature of distribution of the grain size and the degree of plasticity in a given soil is important for

design purposes.

- \* Grain-size analysis for grain sizes > 0.075 mm is done by sieve analysis.
- \* Sieve Analysis:

Shaking of the soil sample through a set of sieves that have progressively smaller openings.



# 2.5 Grain-Size Analysis Cont'd

- \* To conduct a sieve analysis, one must first oven-dry the soil and then break all lumps into small grains.
- \* The soil is then shaken through a stack of sieves with openings of decreasing size from top to bottom.
- \* The smallest sized sieve should be the U.S No. 200 sieve.
- \* After the process, the mass of soil retained on each sieve is determined.

## 2.5 Grain-Size Analysis Cont'd

#### Calculation for a sieve analysis:

- \* Determine the mass of soil retained on each sieve ( $M_1$ ,  $M_{2, \dots}$   $M_n$ ), and in the pan ( $M_p$ )
- \* Determine the total mass of the soil:

$$M_1 + M_2 + M_n + M_p = \Sigma M$$

- \* Determine the cumulative mass of soil retained above each sieve. For the *i*th sieve, it is  $M_1 + M_2 + ... + M_i$
- \* The mass of soil passing the *i*th sieve is:

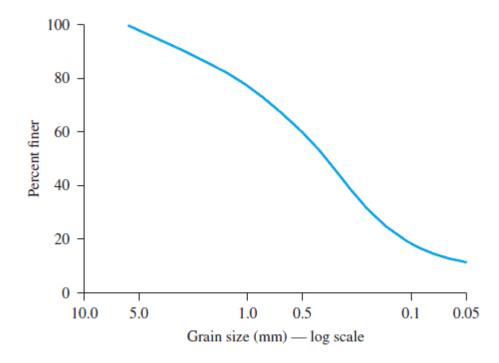
$$\Sigma M - (M_1 + M_2 + ... + M_i)$$

\* The percent of soil passing the *i*th sieve (or percent finer) is:

$$F = \frac{\sum M - (M_1 + M_2 + ... + M_i)}{\sum M} * 100$$

## 2.5 Grain-Size Analysis Cont'd

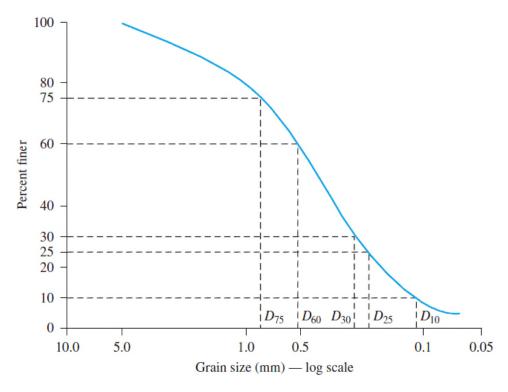
- Once the percent finer for each sieve has been calculated, values are plotted on semilogarithmic graph paper.
- \* This plot is called the *grain-size distribution curve*:



#### 2.6 Grain-Size Distribution Curve

The grain-size distribution curve can be used to determine the following four parameters:

1) Effective Size ( $D_{10}$ ): Diameter corresponding to 10% finer. It is a good measure to estimate the hydraulic conductivity and drainage through the soil.



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## 2.6 Grain-Size Distribution Curve Cont'd

2) Uniformity Coefficient (C<sub>u</sub>):

$$C_u = \frac{D_{60}}{D_{10}}$$

3) Coefficient of Gradation (C<sub>c</sub>):

$$C_C = \frac{D_{30}^2}{D_{60} \times D_{10}}$$

4) Sorting Coefficient  $(S_0)$ :

$$S_0 = \sqrt{(D_{75}/D_{25})}$$

Introduction to Geotechnical Engineering, 2e

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## 2.7 Summary

- \* Gravels, sands, silts, and clays are the four major groups of soil in geotechnical engineering.
- \* There are slight differences in the size ranges used. The Unified Soil Classification System is the most widely utilized system.
- \* Soil is a medium that has the solid grains often mixed with water and air.
- \* In coarse grained soils, grain-size distribution plays an important role in their engineering behavior.
- \* Grain-size analysis is carried out using sieves for coarsegrained soils, and the data is presented graphically (%finer vs. grain size).