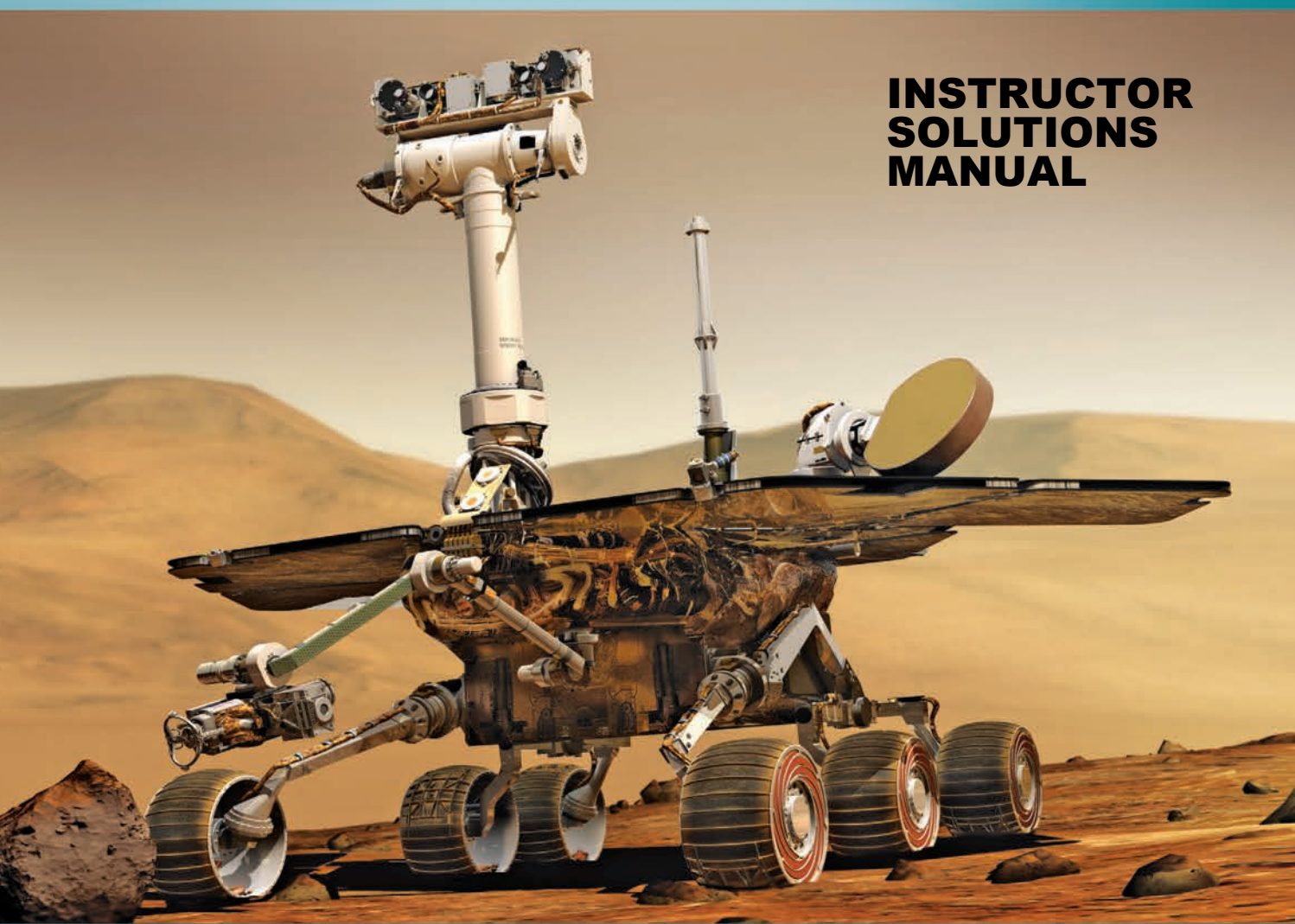


FIFTH EDITION

# Fundamentals of Electric Circuits

**INSTRUCTOR  
SOLUTIONS  
MANUAL**



Charles K. Alexander | Matthew N. O. Sadiku

### **Chapter 1, Solution 1**

(a)  $q = 6.482 \times 10^{17} \times [-1.602 \times 10^{-19} \text{ C}] = \mathbf{-103.84 \text{ mC}}$

(b)  $q = 1.24 \times 10^{18} \times [-1.602 \times 10^{-19} \text{ C}] = \mathbf{-198.65 \text{ mC}}$

(c)  $q = 2.46 \times 10^{19} \times [-1.602 \times 10^{-19} \text{ C}] = \mathbf{-3.941 \text{ C}}$

(d)  $q = 1.628 \times 10^{20} \times [-1.602 \times 10^{-19} \text{ C}] = \mathbf{-26.08 \text{ C}}$

## Chapter 1, Solution 2

- (a)  $i = dq/dt = 3 \text{ mA}$
- (b)  $i = dq/dt = (16t + 4) \text{ A}$
- (c)  $i = dq/dt = (-3e^{-t} + 10e^{-2t}) \text{ nA}$
- (d)  $i = dq/dt = 1200\pi \cos 120\pi t \text{ pA}$
- (e)  $i = dq/dt = -e^{-4t} (80 \cos 50t + 1000 \sin 50t) \mu\text{A}$

Chapter 1, Solution 3

$$(a) \quad q(t) = \int i(t)dt + q(0) = \underline{(3t + 1) \text{ C}}$$

$$(b) \quad q(t) = \int (2t + s) dt + q(v) = \underline{(t^2 + 5t) \text{ mC}}$$

$$(c) \quad q(t) = \int 20 \cos (10t + \pi / 6) + q(0) = \underline{(2 \sin(10t + \pi / 6) + 1) \mu C}$$

$$(d) \quad q(t) = \int 10e^{-30t} \sin 40t + q(0) = \frac{10e^{-30t}}{900 + 1600} (-30 \sin 40t - 40 \cos t) \\ = \underline{-e^{-30t} (0.16 \cos 40t + 0.12 \sin 40t) \text{ C}}$$

#### Chapter 1, Solution 4

$$q = it = 7.4 \times 20 = \underline{\underline{148 \text{ C}}}$$

**Chapter 1, Solution 5**

$$q = \int i dt = \int_0^{10} \frac{1}{2} t dt = \frac{t^2}{4} \bigg|_0^{10} = \underline{\underline{25 \text{ C}}}$$

Chapter 1, Solution 6

(a) At  $t = 1\text{ms}$ ,  $i = \frac{dq}{dt} = \frac{30}{2} = \underline{\underline{15\text{ A}}}$

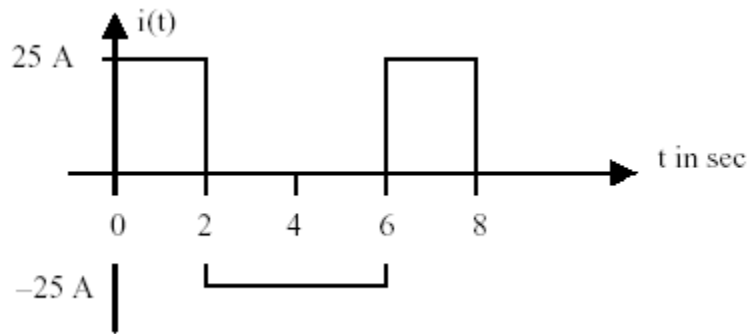
(b) At  $t = 6\text{ms}$ ,  $i = \frac{dq}{dt} = \underline{\underline{0\text{ A}}}$

(c) At  $t = 10\text{ms}$ ,  $i = \frac{dq}{dt} = \frac{-30}{4} = \underline{\underline{-7.5\text{ A}}}$

Chapter 1, Solution 7

$$i = \frac{dq}{dt} = \begin{cases} 25A, & 0 < t < 2 \\ -25A, & 2 < t < 6 \\ 25A, & 6 < t < 8 \end{cases}$$

which is sketched below:





Chapter 1, Solution 8

$$q = \int i dt = \frac{10 \times 1}{2} + 10 \times 1 = \underline{15 \mu\text{C}}$$

Chapter 1, Solution 9

$$(a) \quad q = \int i \, dt = \int_0^1 10 \, dt = \underline{10 \, C}$$

$$(b) \quad q = \int_0^3 i \, dt = 10 \times 1 + \left( 10 - \frac{5 \times 1}{2} \right) + 5 \times 1 \\ = 15 + 7.5 + 5 = \underline{22.5 \, C}$$

$$(c) \quad q = \int_0^5 i \, dt = 10 + 10 + 10 = \underline{30 \, C}$$

**Chapter 1, Solution 10**

$$q = it = 10 \times 10^3 \times 15 \times 10^{-6} = \underline{\underline{150 \text{ mC}}}$$

### Chapter 1, Solution 11

$$q = it = 90 \times 10^{-3} \times 12 \times 60 \times 60 = \mathbf{3.888 \text{ kC}}$$

$$E = pt = ivt = qv = 3888 \times 1.5 = \mathbf{5.832 \text{ kJ}}$$

## Chapter 1, Solution 12

For  $0 < t < 6\text{s}$ , assuming  $q(0) = 0$ ,

$$q(t) = \int_0^t i dt + q(0) = \int_0^t 3t dt + 0 = 1.5t^2$$

$$\text{At } t=6, q(6) = 1.5(6)^2 = 54$$

For  $6 < t < 10\text{s}$ ,

$$q(t) = \int_6^t i dt + q(6) = \int_6^t 18 dt + 54 = 18t - 54$$

$$\text{At } t=10, q(10) = 180 - 54 = 126$$

For  $10 < t < 15\text{s}$ ,

$$q(t) = \int_{10}^t i dt + q(10) = \int_{10}^t (-12) dt + 126 = -12t + 246$$

$$\text{At } t=15, q(15) = -12 \times 15 + 246 = 66$$

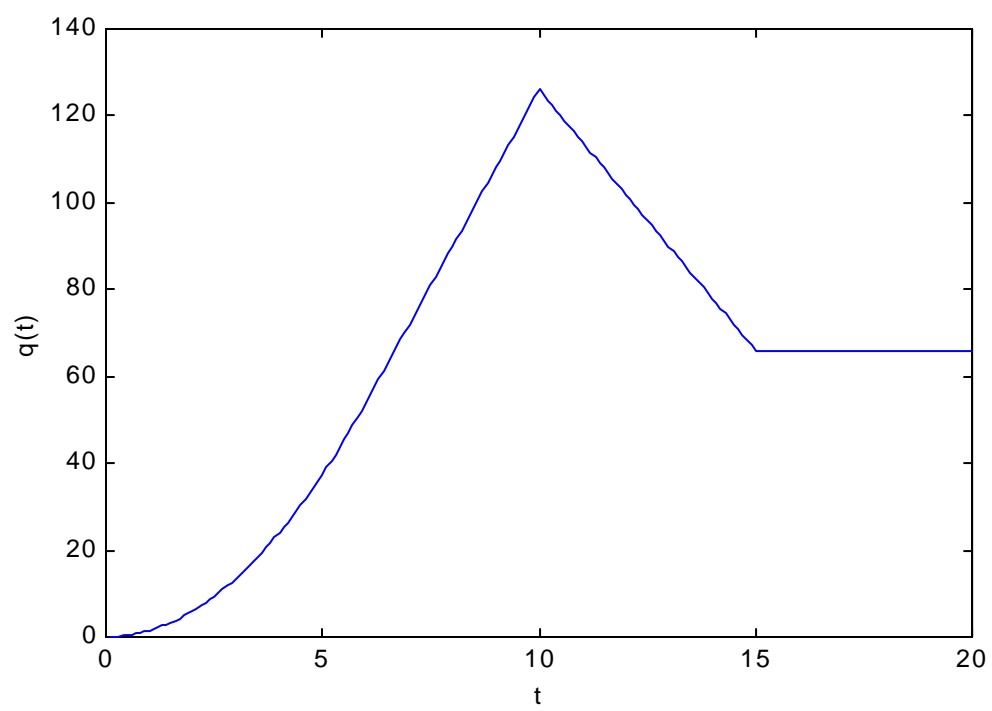
For  $15 < t < 20\text{s}$ ,

$$q(t) = \int_{15}^t 0 dt + q(15) = 66$$

Thus,

$$q(t) = \begin{cases} 1.5t^2 \text{ C, } 0 < t < 6\text{s} \\ 18t - 54 \text{ C, } 6 < t < 10\text{s} \\ -12t + 246 \text{ C, } 10 < t < 15\text{s} \\ 66 \text{ C, } 15 < t < 20\text{s} \end{cases}$$

The plot of the charge is shown below.



### Chapter 1, Solution 13

$$(a) \quad i = [dq/dt] = 20\pi \cos(4\pi t) \text{ mA}$$

$$p = vi = 60\pi \cos^2(4\pi t) \text{ mW}$$

At  $t=0.3\text{s}$ ,

$$p = vi = 60\pi \cos^2(4\pi 0.3) \text{ mW} = \mathbf{123.37 \text{ mW}}$$

$$(b) \quad W = \int p dt = 60\pi \int_0^{0.6} \cos^2(4\pi t) dt = 30\pi \int_0^{0.6} [1 + \cos(8\pi t)] dt$$

$$W = 30\pi[0.6 + (1/(8\pi))[\sin(8\pi 0.6) - \sin(0)]] = \mathbf{58.76 \text{ mJ}}$$

Chapter 1, Solution 14

$$(a) \quad q = \int i dt = \int_0^1 0.02(1 - e^{-0.5t}) dt = 0.02 \left( t + 2e^{-0.5t} \right) \Big|_0^1 = 0.02(1 + 2e^{-0.5} - 2) = \mathbf{4.261 \text{ mC}}$$

$$(b) \quad p(t) = v(t)i(t) \\ p(1) = 10\cos(2) \times 0.02(1 - e^{-0.5}) = (-4.161)(0.007869) \\ = \mathbf{-32.74 \text{ mW}}$$



Chapter 1, Solution 15

$$\begin{aligned}
 \text{(a)} \quad q &= \int i dt = \int_0^2 0.006e^{-2t} dt = \left. \frac{-0.006}{2} e^{2t} \right|_0^2 \\
 &= -0.003(e^{-4} - 1) = \\
 &\quad \mathbf{2.945 \text{ mC}}
 \end{aligned}$$

$$\begin{aligned}
 \text{(b)} \quad v &= \frac{10 di}{dt} = -0.012e^{-2t} (10) = -0.12e^{-2t} \text{ V this leads to } p(t) = v(t)i(t) = \\
 &(-0.12e^{-2t})(0.006e^{-2t}) = \mathbf{-720e^{-4t} \mu W}
 \end{aligned}$$

$$\text{(c)} \quad w = \int p dt = -0.72 \int_0^3 e^{-4t} dt = \left. \frac{-720}{-4} e^{-4t} 10^{-6} \right|_0^3 = \mathbf{-180 \mu J}$$

## Chapter 1, Solution 16

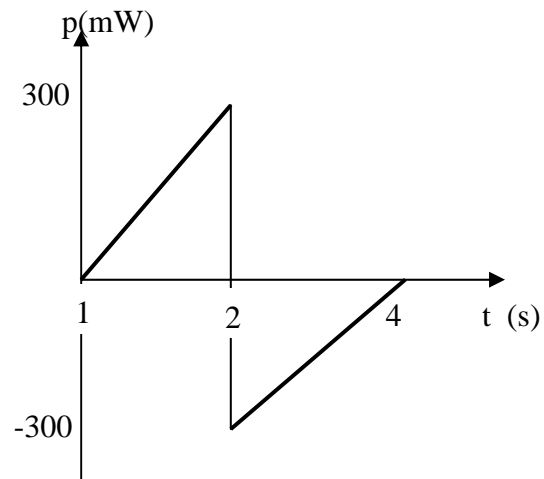
(a)

$$i(t) = \begin{cases} 30t \text{ mA}, & 0 < t < 2 \\ 120 - 30t \text{ mA}, & 2 < t < 4 \end{cases}$$

$$v(t) = \begin{cases} 5 \text{ V}, & 0 < t < 2 \\ -5 \text{ V}, & 2 < t < 4 \end{cases}$$

$$p(t) = \begin{cases} 150t \text{ mW}, & 0 < t < 2 \\ -600 + 150t \text{ mW}, & 2 < t < 4 \end{cases}$$

which is sketched below.



(b) From the graph of  $p$ ,

$$W = \int_0^4 p dt = \underline{0 \text{ J}}$$

**Chapter 1, Solution 17**

$$\sum p = 0 \rightarrow -205 + 60 + 45 + 30 + p_3 = 0$$

$$p_3 = 205 - 135 = 70 \text{ W}$$

Thus element 3 receives **70 W**.

**Chapter 1, Solution 18**

$$p_1 = 30(-10) = \mathbf{-300\text{ W}}$$

$$p_2 = 10(10) = \mathbf{100\text{ W}}$$

$$p_3 = 20(14) = \mathbf{280\text{ W}}$$

$$p_4 = 8(-4) = \mathbf{-32\text{ W}}$$

$$p_5 = 12(-4) = \mathbf{-48\text{ W}}$$