

DESIGN OF WOOD STRUCTURES – ASD/LRFD (7th edition)

- 4.1 a. narrow, needle-like leaves; evergreens; conifers
 b. broadleafed; deciduous
 c. softwoods
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- 4.2 See Fig. 4.3.
 a. Annual Ring – wood cells developed on the outside of the tree in one growing season
 b. Latewood (summerwood) – smaller, darker, more dense, from late in growing season
 Earlywood (springwood) – larger, light color, less dense, from early in growing season
 c. Heartwood –center of log; inactive cells; collects deposits as tree ages; darker
 Sapwood – outer, living, active cells; stores food and transports water
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- 4.3 a. Amount of water expressed as percent of dry weight of wood material:

$$MC = \frac{\text{moistweight} - \text{ovendryweight}}{\text{ovendryweight}} \times 100\%$$

 b. FSP = MC at point of “no free water” and fully saturated (bound water) wood.
 c. EMC = MC wood assumes in service for a given set of atmospheric conditions
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- 4.4 a. $MC \leq 19\%$
 b. $MC > 19\%$
 Note: These values are for sawn lumber; for glulam see Chap. 5 (dry MC < 16%).
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- 4.5 EMC for buildings in “dry southwest states” is approximately 9%, ranging from 7% to 12% (Ref. 4.4)
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- 4.6 *National Design Specification for Wood Construction (NDS) with Commentary*
 Design Values for Wood Construction (NDS Design Values Supplement)
 Special Design Provisions for Wind & Seismic (NDS Wind & Seismic Supplement)
 ASD/LRFD Manual for Engineered Wood Construction
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- 4.7 bending stress (F_b)
tension stress parallel to grain (F_t)
shear stress parallel to grain (F_v)
compression stress parallel to grain (F_c)
compression stress perpendicular to grain ($F_{c\perp}$)
modulus of elasticity (E)

4.8

	Nominal Size	Dressed (in. x in.)	Area (in²)	I_x (in⁴)	S_x (in³)	I_y (in⁴)	S_y (in³)
a.	2 x 4	1.5 x 3.5	5.25	5.359	3.063	0.984	1.313
b.	8 x 8	7.5 x 7.5	56.25	263.7	70.31	263.7	70.31
c.	4 x 10	3.5 x 9.25	32.38	230.8	49.91	33.05	18.89
d.	6 x 16	5.5 x 15.5	85.25	1707	220.2	214.9	78.15

- 4.9
- Nominal 2 to 4 in. thick; any width; practically 2 x 2 to 4 x 16.
 - Minimum nominal dimension of 5 in. or larger; includes beams & stringers (width more than 2 in. > thickness) and posts & timbers (square; not more than 2 in. out of square).
 - Design values for the main size categories are determined following different procedures.
Dimension Lumber- primarily from in-grade test program: ASTM D1990.
Timbers – tests of small clear specimens: ASTM D2555 & D245
Dimension Lumber: NDS Supplement Tables 4A, 4B, 4C, 4E, 4F
Timbers: NDS Supplement Table 4D

- 4.10
- Timbers; 5 in. and thicker, width more than 2 in. > thickness
 - Dimension Lumber; 2 to 4 in. thick, 2 to 4 in. wide
 - Dimension Lumber; 2 to 4 in. thick, 4 in. and wider
 - Dimension Lumber; 2 to 4 in. thick, 5 in. and wider
 - Timbers; 5 in. and thicker, width not more than 2 in. > thickness
 - Dimension Lumber; 2 to 4 in. thick, 2 to 4 in. wide
 - Dimension Lumber; 2 to 4 in. thick, 2 in. and wider, ≤ 10 ft long

- 4.11 Visually graded is graded visually by inspecting and marking each piece. NDS Supplement Tables 4A, 4B, 4D, 4E, and 4F
MSR refers to lumber graded mechanically by subjecting each piece to a nondestructive test that measure E about the weak axis. A visual check is also included. MSR grading is only used for lumber with thickness ≤ 2 in. NDS Supplement Table 4C

4.12 Visually graded sawn lumber other than Southern Pine

	Size	Size Category	NDS Supplement
a.	10 x 12	P & T	Table 4D
b.	14 x 14	P & T	Table 4D
c.	4 x 8	Dimension	Table 4A
d.	4 x 4	Dimension	Table 4A
e.	2 x 12	Dimension	Table 4A
f.	6 x 12	B & S	Table 4D
g.	8 x 12	B & S	Table 4D
h.	8 x 10	P & T	Table 4D

4.13 Visually graded sawn lumber – Southern Pine

	Size	Size Category	NDS Supplement
a.	10 x 12	P & T	Table 4D
b.	14 x 14	P & T	Table 4D
c.	4 x 8	Dimension	Table 4B
d.	4 x 4	Dimension	Table 4B
e.	2 x 12	Dimension	Table 4B
f.	6 x 12	B & S	Table 4D
g.	8 x 12	B & S	Table 4D
h.	8 x 10	P & T	Table 4D

4.14 Stress grades of visually graded Hem-Fir

- a. Dimension Lumber (NDS Supplement Table 4A)
Select Structural; No.1 & Btr; No.1; No.2; No.3; Stud; Construction;
Standard; Utility
 - b. Beams and Stringers (NDS Supplement Table 4D)
Select Structural; No.1; No.2
 - c. Posts and Timbers (NDS Supplement Table 4D)
Select Structural; No.1; No.2
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4.15 Stress grades of visually graded Southern Pine

a. Dimension Lumber-stress grades vary with size (NDS Supplement Table 4B)

2 in. – 4 in. thick 2 in. – 12 in. wide	Dense Select Structural; Select Structural; Non-Dense Select Structural; No.1 Dense; No.1; No.1 Non-Dense; No. 2 Dense; No. 2; No.2 Non-Dense; No.3 and Stud
2 in. – 4 in. thick 4 in. wide	Construction; Standard; Utility

2 – 4 in. thick 2 in. and wider	Dense Structural 86; Dense Structural 72; Dense Structural 65
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b. Beams & Stringers and c. Posts & Timbers (NDS Supplement Table 4D)

5 in. x 5 in. and larger	Dense Select Structural; Select Structural; No. 1 Dense; No.1; No.2 Dense; No. 2; Dense Structural 86; Dense Structural 72; Dense Structural 65
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4.16 Reference design values for No. 2 DF-L
Dimension Lumber (NDS Supplement Table 4A)

c. 4 x 16 – Dimension Lumber

d. 4 x 4 – Dimension Lumber

e. 2 x 10 – Dimension Lumber

$$\begin{aligned}F_b &= 900 \text{ psi} \\F_t &= 575 \text{ psi} \\F_v &= 180 \text{ psi} \\F_{c\perp} &= 625 \text{ psi} \\F_c &= 1350 \text{ psi} \\E &= 1,600,000 \text{ psi} \\E_{\min} &= 580,000 \text{ psi}\end{aligned}$$

Beams and Stringers (NDS Supplement Table 4D)

f. 6 x 12 – Beams & Stringers

h. 10 x 14 – Beams & Stringers

$$\begin{aligned}F_b &= 875 \text{ psi} \\F_t &= 425 \text{ psi} \\F_v &= 170 \text{ psi} \\F_{c\perp} &= 625 \text{ psi} \\F_c &= 600 \text{ psi} \\E &= 1,300,000 \text{ psi} \\E_{\min} &= 470,000 \text{ psi}\end{aligned}$$

Posts and Timbers (NDS Supplement Table 4D)

a. 10 x 10 – Posts & Timbers

b. 12 x 14 – Posts & Timbers

g. 6 x 8 – Posts & Timbers

$$\begin{aligned}F_b &= 750 \text{ psi} \\F_t &= 475 \text{ psi} \\F_v &= 170 \text{ psi} \\F_{c\perp} &= 625 \text{ psi} \\F_c &= 700 \text{ psi} \\E &= 1,300,000 \text{ psi} \\E_{\min} &= 470,000 \text{ psi}\end{aligned}$$

4.17 Nominal design values (LRFD) for No. 2 DF-L
Dimension Lumber (NDS Supplement Table 4A)

c. 4 x 16 – Dimension Lumber

d. 4 x 4 – Dimension Lumber

e. 2 x 10 – Dimension Lumber

$$F_{bn} = F_b (K_F) = 900 \text{ psi (2.54)} = 2.29 \text{ ksi} \quad (\Phi_b = 0.85)$$

$$F_{tn} = F_t (K_F) = 575 \text{ psi (2.70)} = 1.55 \text{ ksi} \quad (\Phi_t = 0.8)$$

$$F_{vn} = F_v (K_F) = 180 \text{ psi (2.88)} = 0.518 \text{ ksi} \quad (\Phi_v = 0.75)$$

$$F_{c\perp n} = F_{c\perp} (K_F) = 625 \text{ psi (1.67)} = 1.04 \text{ ksi} \quad (\Phi_c = 0.9)$$

$$F_{cn} = F_c (K_F) = 1350 \text{ psi (2.40)} = 3.24 \text{ ksi} \quad (\Phi_c = 0.9)$$

$$E = 1,600,000 \text{ psi}$$

$$E_{\min-n} = E_{\min} (K_F) = 580,000 \text{ psi (1.76)} = 1021 \text{ ksi} \quad (\Phi_s = 0.85)$$

Beams and Stringers (NDS Supplement Table 4D)

f. 6 x 12 – Beams & Stringers

h. 10 x 14 – Beams & Stringers

$$F_{bn} = F_b (K_F) = 875 \text{ psi (2.54)} = 2.22 \text{ ksi} \quad (\Phi_b = 0.85)$$

$$F_{tn} = F_t (K_F) = 425 \text{ psi (2.70)} = 1.15 \text{ ksi} \quad (\Phi_t = 0.8)$$

$$F_{vn} = F_v (K_F) = 170 \text{ psi (2.88)} = 0.490 \text{ ksi} \quad (\Phi_v = 0.75)$$

$$F_{c\perp n} = F_{c\perp} (K_F) = 625 \text{ psi (1.67)} = 1.04 \text{ ksi} \quad (\Phi_c = 0.9)$$

$$F_{cn} = F_c (K_F) = 600 \text{ psi (2.40)} = 1.44 \text{ ksi} \quad (\Phi_c = 0.9)$$

$$E = 1,300,000 \text{ psi}$$

$$E_{\min-n} = E_{\min} (K_F) = 470,000 \text{ psi (1.76)} = 827 \text{ ksi} \quad (\Phi_s = 0.85)$$

Posts and Timbers (NDS Supplement Table 4D)

a. 10 x 10 – Posts & Timbers

b. 12 x 14 – Posts & Timbers

g. 6 x 8 – Posts & Timbers

$$F_{bn} = F_b (K_F) = 750 \text{ psi (2.54)} = 1.91 \text{ ksi} \quad (\Phi_b = 0.85)$$

$$F_{tn} = F_t (K_F) = 475 \text{ psi (2.70)} = 1.28 \text{ ksi} \quad (\Phi_t = 0.8)$$

$$F_{vn} = F_v (K_F) = 170 \text{ psi (2.88)} = 0.490 \text{ ksi} \quad (\Phi_v = 0.75)$$

$$F_{c\perp n} = F_{c\perp} (K_F) = 625 \text{ psi (1.67)} = 1.04 \text{ ksi} \quad (\Phi_c = 0.9)$$

$$F_{cn} = F_c (K_F) = 700 \text{ psi (2.40)} = 1.68 \text{ ksi} \quad (\Phi_c = 0.9)$$

$$E = 1,300,000 \text{ psi}$$

$$E_{\min-n} = E_{\min} (K_F) = 470,000 \text{ psi (1.76)} = 827 \text{ ksi} \quad (\Phi_s = 0.85)$$

4.18

Adjustment Factor	Design values that may require adjustment
a. Size Factor (C_F)	$F_b; F_t; F_c$
b. Time Effect Factor (λ)	$F_b; F_t; F_v; F_c$
c. Load Duration Factor (C_D)	$F_b; F_t; F_v; F_c$
d. Repetitive Member Factor (C_r)	F_b
e. Temperature Factor (C_t)	$F_b; F_t; F_v; F_c; F_{c\perp}; E; E_{\min}$
f. Wet Service Factor (C_M)	$F_b; F_t; F_v; F_c; F_{c\perp}; E; E_{\min}$
g. Flat Use Factor (C_{fu})	F_b

4.19

- a. Load Duration Factor, C_D : The strength of a wood member is affected by the total accumulated length of time that a load is applied. The shorter the duration of load, the higher the strength of a wood member. C_D is the multiplier that adjusts reference design values (F_b , F_t , F_v and F_c) from normal duration (10 years) to other durations for ASD. See NDS 2.3.2 and Appendix B.
- b. Time Effect Factor, λ : The strength of a wood member is affected by the total accumulated length of time that a load is applied. λ is the multiplier that adjusts the LRFD resistance of wood members (F_b , F_t , F_v and F_c) to ensure that consistent reliability is achieved for load duration effects in various LRFD load combinations. See NDS Appendix N.
- c. Wet Service Factor, C_M : The moisture content (MC) of a wood member affects its load capacity. Most reference design values for sawn lumber apply to $MC \leq 19$ percent in service. Higher moisture contents require reduction of design values by C_M . The following reference design values are subject to adjustment for increased moisture content: F_b , F_t , F_v , $F_{c\perp}$, F_c , E and E_{min} . See NDS 4.3.3 and the Adjustment Factors sections of NDS Supplement Tables 4A, 4B, 4C, 4D, 4E, and 4F.
- d. Size Factor, C_F : The size of a wood member affects its strength. For visually graded Dimension Lumber, C_F applies to F_b , F_t and F_c . See NDS 4.3.6.1 and the Adjustment Factor section of NDS Supplement Tables 4A and 4F. For Timbers, the size factor applies to F_b . See NDS 4.3.6.2 and the Adjustment Factors section of NDS Supplement Table 4D. For Decking, C_F applies only to F_b . See NDS 4.3.6.4 and the Adjustment Factors section of NDS Supplement Table 4E.
- e. Repetitive Member Factor, C_r : Applies to Dimension Lumber, but not to Timbers. When three or more wood members are spaced not more than 24 in. o/c and are connected together by a load distributing element (such as sheathing), the bending design value F_b may be increased by $C_r = 1.15$. This is a 15 percent increase over single member bending design values. The C_r adjustment recognizes that failure of a single member in a repetitive application will not mean failure of the overall system. The load will be distributed to other members.

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- 4.20 Wood has the ability to support higher stresses for short periods of time. Both the load duration factor (C_D) and the time effect factor (λ) are employed to adjust wood strength properties based on the duration of applied design loads. The load duration factor (C_D) is used to adjust reference design values in allowable stress design (ASD), and is based on the shortest duration load in an ASD load combination. The time effect factor (λ) is used to adjust nominal design values in load and resistance factor design (LRFD), and is based on the dominant transient load in an LRFD load combination. Time effect factors (λ) are intended to ensure consistent reliability for load duration effects across various load combinations.

- 4.21 a. Snow (S): $C_D = 1.15$
 b. Wind (W): $C_D = 1.6$
 c. Floor Live Load (L): $C_D = 1.0$
 d. Roof Live Load (L_r): $C_D = 1.25$
 e. Dead Load (D): $C_D = 0.9$
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- 4.22 a. $1.2D + 1.6S + L$: $\lambda = 0.8$
 b. $1.2D + W + L + 0.5S$: $\lambda = 1.0$
 c. $1.2D + 1.6L + 0.5S$: $\lambda = 0.8$ (for L due to occupancy)
 d. $1.2D + 1.6L_r + L$: $\lambda = 0.8$
 e. $1.4D$: $\lambda = 0.6$
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- 4.23 Compression perpendicular to grain ($F_{c\perp}$), average modulus of elasticity (E), and reduced modulus of elasticity for stability calculations (E_{min}) are not adjusted by C_D in ASD calculations.
 Compression perpendicular to grain ($F_{c\perp}$), average modulus of elasticity (E) and reduced modulus of elasticity for stability calculations (E_{min}) are not adjusted by λ in LRFD calculations.
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- 4.24 Most reference design values apply to dry service conditions^{*}. Dry service conditions are defined as:
 a. Sawn Lumber $MC \leq 19$ percent
 b. Glulam $MC < 16$ percent
 When the moisture content exceeds these limits, the reference design values are reduced by a wet service factor C_M that is less than 1.0
 ^{*} *Southern Pine has C_M included in some of the reference design values (NDS Supplement Table 4B). Many of the reference design values for Timbers (NDS Supplement Table 4D) have already been adjusted for C_M .*
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- 4.25 The load capacity of wood decreases as the temperature increases. Reductions in strength caused by heating up to 150 degrees F are generally reversible when the temperature returns to normal. Reductions in strength may not be reversible when heating exceeds 150 degrees F. Reduction in strength occurs when the member is subjected to the full design capacity.
 When a wood member is consistently heated above 100 degrees F and is subjected to the full design load, an adjustment for temperature effects will be required. This may occur in an industrial plant, but reductions are not normally required in ordinary roof structures. See NDS 2.3.3 and Appendix C.
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- 4.26 Pressure preservative treated wood has chemicals impregnated in the treated zone which resist attack by decay, termites and other insects, and marine borers. Reference design values apply directly to preservative treated wood, and an adjustment factor is not required unless the member has been incised to increase the penetration of preservatives.

Fire-retardant-treated wood has much higher concentrations of chemicals than preservative treated wood. At one time a 10 percent reduction in reference design values was specified. However, the reduction in strength varies with the treating process, and the NDS refers the designer to the company providing the fire retardant treatment for appropriate reduction factors.

- 4.27 Wood that is *continuously submerged* in fresh water will not decay and does not need to be preservative treated. However, wood that is partially submerged, or wood that undergoes cycles of submersion followed by exposure to the atmosphere, should be preservative treated. Wood that is submerged in salt water should be preservative treated to protect from marine borers. Preservative treated wood has an extensive record of resisting attack in both fresh water and salt water environments.

- 4.28 Critical ASD load combination for a fully braced member

ASD Combination	Load	C_D	Load/ C_D *
D (roof + floor)	$3 + 6 = 9$ k	0.9	10 k
D + L	$9 + 10 = 19$ k	1	19 k
D + L_r	$9 + 5 = 14$ k	1.25	11.2 k
D + 0.6W	$9 + 10.2 = 19.2$ k	1.6	12 k
D + $\frac{3}{4}(L + L_r)$	$9 + \frac{3}{4}(10 + 5) = 20.25$ k	1.25	16.2 k
D + $\frac{3}{4}(0.6W + L + L_r)$	$9 + \frac{3}{4}(10.2 + 10 + 5) = 27.75$ k	1.6	17.4 k

* The largest load in this column defines the critical ASD load combination for a fully braced member: **D + L**

Note: Actual loads (i.e., loads that have not been divided by C_D) should be used in design calculations. The load duration factor should then be used to adjust the appropriate reference design values. In this problem, the actual critical load is 19 k and $C_D = 1.0$. The above analysis is used to define the critical combination only for fully braced members, tension members, or connections.

- 4.29 Critical ASD load combination for a fully braced member
 $[0.6W = 0.6(17 \text{ k}) = 10.2 \text{ k}] > [0.7E = 0.7(12 \text{ k}) = 8.4 \text{ k}]$
 $[S = 18 \text{ k}] > [L_r = 7 \text{ k}]$

Combination	Load	C_D	Load/ C_D *
D (roof + floor)	$5 + 6 = 11 \text{ k}$	0.9	12.2 k
D + L	$11 + 15 = 26 \text{ k}$	1	26.0 k
D + S	$11 + 18 = 29 \text{ k}$	1.15	25.2 k
D + L_r	$11 + 7 = 18 \text{ k}$	1.25	14.4 k
D + 0.75(L + S)	$11 + 0.75(15 + 18) = 35.75 \text{ k}$	1.15	31.1 k
D + 0.75(L + L_r)	$11 + 0.75(15 + 7) = 27.5 \text{ k}$	1.25	22.0 k
D + (0.6W or 0.7E)	$11 + 10.2 = 21.2 \text{ k}$	1.6	13.3 k
D + 0.75(0.6W or 0.7E) + 0.75L + 0.75(L_r or S)	$11 + 0.75(10.2 + 15 + 18) = 43.4 \text{ k}$	1.6	27.1 k

* The largest load in this column defines the critical ASD load combination for a fully braced member: **D + 0.75(L + S)**

Note: Actual loads (i.e., loads that have not been divided by C_D) should be used in design calculations. The load duration factor should then be used to adjust the appropriate reference design values. In this problem, the actual critical load is 35.75 k and $C_D = 1.15$. The above analysis is used to define the critical combination only for fully braced members, tension members, or connections.

- 4.30 ASD – Hem-Fir No.2, fully braced; bending about strong axis
- a. **2 x 10 joists** at 16 in. o.c. ($C_r = 1.15$); D + S load combination ($C_D = 1.15$)
 C_F applies for bending, tension and compression; other factors equal to unity
 $F_b' = F_b (C_D)(C_F)(C_r) = 850 \text{ psi } (1.15)(1.1)(1.15) = 1237 \text{ psi}$
 $F_t' = F_t (C_D)(C_F) = 525 \text{ psi } (1.15)(1.1) = 664 \text{ psi}$
 $F_v' = F_v (C_D) = 150 \text{ psi } (1.15) = 173 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} = 405 \text{ psi}$
 $F_c' = F_c (C_D)(C_F) = 1300 \text{ psi } (1.15)(1.0) = 1495 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E = 1,300,000 \text{ psi}$
 $E_{\min}' = E_{\min} = 470,000 \text{ psi}$
- b. **6 x 14 (Beams & Stringers)**; supports permanent load ($C_D = 0.9$)
 $C_F = (12/13.5)^{0.111} = 0.987$ for bending; other factors equal to unity
 $F_b' = F_b (C_D)(C_F) = 675 \text{ psi } (0.9)(0.987) = 600 \text{ psi}$
 $F_t' = F_t (C_D) = 350 \text{ psi } (0.9) = 315 \text{ psi}$
 $F_v' = F_v (C_D) = 140 \text{ psi } (0.9) = 126 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} = 405 \text{ psi}$
 $F_c' = F_c (C_D) = 500 \text{ psi } (0.9) = 450 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E = 1,100,000 \text{ psi}$
 $E_{\min}' = E_{\min} = 400,000 \text{ psi}$
- c. **4 x 14 purlins** at 8 ft o.c.; D + L_r load combination ($C_D = 1.25$)
 C_F applies for bending, tension and compression; other factors equal to unity
 $F_b' = F_b (C_D)(C_F) = 850 \text{ psi } (1.25)(1.0) = 1063 \text{ psi}$
 $F_t' = F_t (C_D)(C_F) = 525 \text{ psi } (1.25)(0.9) = 591 \text{ psi}$
 $F_v' = F_v (C_D) = 150 \text{ psi } (1.25) = 188 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} = 405 \text{ psi}$
 $F_c' = F_c (C_D)(C_F) = 1300 \text{ psi } (1.25)(0.9) = 1463 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E = 1,300,000 \text{ psi}$
 $E_{\min}' = E_{\min} = 470,000 \text{ psi}$
- d. **4 x 6 beams** at 4 ft o.c.; D + L load combination ($C_D = 1.0$); C_M applies
 C_F applies for bending, tension and compression; other factors equal to unity
 $F_b' = F_b (C_D)(C_M)(C_F) = 850 \text{ psi } (1.0)(1.0)(1.3) = 1105 \text{ psi}$
 $C_M = 1.0$ for bending since $F_b (C_F) = 1105 \text{ psi} < 1150 \text{ psi}$
 $F_t' = F_t (C_D)(C_M)(C_F) = 525 \text{ psi } (1.0)(1.0)(1.3) = 683 \text{ psi}$
 $F_v' = F_v (C_D)(C_M) = 150 \text{ psi } (1.0)(0.97) = 146 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} (C_M) = 405 \text{ psi } (0.67) = 271 \text{ psi}$
 $F_c' = F_c (C_D)(C_M)(C_F) = 1300 \text{ psi } (1.0)(0.8)(1.1) = 1144 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E (C_M) = 1,300,000 \text{ psi } (0.9) = 1,170,000 \text{ psi}$
 $E_{\min}' = E_{\min} (C_M) = 470,000 \text{ psi } (0.9) = 423,000 \text{ psi}$
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- 4.31 LRFD (K_F and Φ apply) – Hem-Fir No.2, fully braced; bending about strong axis
a. **2 x 10 joists** at 16 in. o.c. ($C_r = 1.15$); 1.2D + 1.6S load combination ($\lambda = 0.8$)

C_F applies for bending, tension and compression; other factors equal to unity

$$A = 13.88 \text{ in}^2; S_x = 21.39 \text{ in}^3$$

Bending moment

$$F_{bn} = F_b (K_F) = 850 \text{ psi} (2.54) = 2159 \text{ psi} = 2.16 \text{ ksi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_F)(C_r) = 2.16 \text{ ksi} (0.85)(0.8)(1.1)(1.15) = 1.86 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 1.86 \text{ ksi} (21.39 \text{ in}^3) = 39.7 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 525 \text{ psi} (2.7) = 1418 \text{ psi} = 1.42 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda)(C_F) = 1.42 \text{ ksi} (0.8)(0.8)(1.1) = 0.998 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 0.998 \text{ ksi} (13.88 \text{ in}^2) = 13.9 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 150 \text{ psi} (2.88) = 432 \text{ psi} = 0.432 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.432 \text{ ksi} (0.75)(0.8) = 0.259 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.259 \text{ ksi} (2/3)(13.88 \text{ in}^2) = 2.4 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 405 \text{ psi} (1.67) = 676 \text{ psi} = 0.676 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c) = 0.676 \text{ ksi} (0.9) = 0.609 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 1300 \text{ psi} (2.4) = 3120 \text{ psi} = 3.12 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda)(C_F) = 3.12 \text{ ksi} (0.9)(0.8)(1.0) = 2.25 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 2.25 \text{ ksi} (13.88 \text{ in}^2) = 31.2 \text{ k}$$

Note that C_P would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E = 1,300,000 \text{ psi} = 1300 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 470,000 \text{ psi} (1.76) = 827,200 \text{ psi} = 827 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s) = 827 \text{ ksi} (0.85) = 703 \text{ ksi}$$

- b. **6 x 16 (Beams & Stringers)**; 1.2D + 1.6L (storage) load ($\lambda = 0.7$)

$C_F = (12/15.5)^{0.111} = 0.972$ for bending; other factors equal to unity

$$A = 85.25 \text{ in}^2; S_x = 220.2 \text{ in}^3$$

Bending moment

$$F_{bn} = F_b (K_F) = 675 \text{ psi} (2.54) = 1714.5 \text{ psi} = 1.71 \text{ ksi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_F) = 1.71 \text{ ksi} (0.85)(0.7)(0.972) = 0.992 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 0.992 \text{ ksi} (220.2 \text{ in}^3) = 218 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 350 \text{ psi} (2.7) = 945 \text{ psi} = 0.945 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 0.945 \text{ ksi} (0.8)(0.7) = 0.529 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 0.529 \text{ ksi} (85.25 \text{ in}^2) = 45.1 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 140 \text{ psi} (2.88) = 403 \text{ psi} = 0.403 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.403 \text{ ksi} (0.75)(0.7) = 0.212 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.212 \text{ ksi} (2/3)(85.25 \text{ in}^2) = 12.0 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 405 \text{ psi} (1.67) = 676 \text{ psi} = 0.676 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c) = 0.676 \text{ ksi} (0.9) = 0.609 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 500 \text{ psi} (2.4) = 1200 \text{ psi} = 1.20 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 1.20 \text{ ksi} (0.9)(0.7) = 0.756 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 0.756 \text{ ksi} (85.25 \text{ in}^2) = 64.4 \text{ k}$$

Note that C_P would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E = 1,100,000 \text{ psi} = 1100 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 400,000 \text{ psi} (1.76) = 704,000 \text{ psi} = 704 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s) = 704 \text{ ksi} (0.85) = 598 \text{ ksi}$$

- c. **4 x 14 purlins** at 8 ft o.c.; 1.2D + 1.6L_r load combination ($\lambda = 0.8$)

C_F applies for bending, tension and compression; other factors equal to unity

$$A = 46.38 \text{ in}^2; S_x = 102.4 \text{ in}^3$$

Bending moment

$$F_{bn} = F_b (K_F) = 850 \text{ psi} (2.54) = 2159 \text{ psi} = 2.16 \text{ ksi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_F) = 2.16 \text{ ksi} (0.85)(0.8)(1.0) = 1.47 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 1.47 \text{ ksi} (102.4 \text{ in}^3) = 150 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 525 \text{ psi} (2.7) = 1418 \text{ psi} = 1.42 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda)(C_F) = 1.42 \text{ ksi} (0.8)(0.8)(0.9) = 0.816 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 0.816 \text{ ksi} (46.38 \text{ in}^2) = 37.9 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 150 \text{ psi} (2.88) = 432 \text{ psi} = 0.432 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.432 \text{ ksi} (0.75)(0.8) = 0.259 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.259 \text{ ksi} (2/3)(46.38 \text{ in}^2) = 8.0 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 405 \text{ psi} (1.67) = 676 \text{ psi} = 0.676 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c) = 0.676 \text{ ksi} (0.9) = 0.609 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 1300 \text{ psi} (2.4) = 3120 \text{ psi} = 3.12 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda)(C_F) = 3.12 \text{ ksi} (0.9)(0.8)(0.9) = 2.02 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 2.02 \text{ ksi} (46.38 \text{ in}^2) = 93.8 \text{ k}$$

Note that C_P would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E = 1,300,000 \text{ psi} = 1300 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 470,000 \text{ psi} (1.76) = 827,200 \text{ psi} = 827 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s) = 827 \text{ ksi} (0.85) = 703 \text{ ksi}$$

- d. **4 x 6 beams** at 4 ft o.c.; 1.2D + 1.6L (occupancy) load ($\lambda = 0.8$); C_M applies
 C_F applies for bending, tension and compression; other factors equal to unity
 $A = 19.25 \text{ in}^2$; $S_x = 17.65 \text{ in}^3$

Bending moment

$$F_{bn} = F_b (K_F) = 850 \text{ psi} (2.54) = 2159 \text{ psi} = 2.16 \text{ ksi}$$

$$C_M = 1.0 \text{ for bending since } F_b (C_F) = 1105 \text{ psi} < 1150 \text{ psi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_M)(C_F) = 2.16 \text{ ksi} (0.85)(0.8)(1.0)(1.3) = 1.91 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 1.91 \text{ ksi} (17.65 \text{ in}^3) = 33.7 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 525 \text{ psi} (2.7) = 1418 \text{ psi} = 1.42 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda)(C_M)(C_F) = 1.42 \text{ ksi} (0.8)(0.8)(1.0)(1.3) = 1.18 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 1.18 \text{ ksi} (19.25 \text{ in}^2) = 22.7 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 150 \text{ psi} (2.88) = 432 \text{ psi} = 0.432 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda)(C_M) = 0.432 \text{ ksi} (0.75)(0.8)(0.97) = 0.251 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.251 \text{ ksi} (2/3)(19.25 \text{ in}^2) = 3.2 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 405 \text{ psi} (1.67) = 676 \text{ psi} = 0.676 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c)(C_M) = 0.676 \text{ ksi} (0.9)(0.67) = 0.408 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 1300 \text{ psi} (2.4) = 3120 \text{ psi} = 3.12 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda)(C_M)(C_F) = 3.12 \text{ ksi} (0.9)(0.8)(0.8)(1.1) = 1.98 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 1.98 \text{ ksi} (19.25 \text{ in}^2) = 38.1 \text{ k}$$

Note that C_P would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E (C_M) = 1,300,000 \text{ psi} (0.9) = 1,170,000 = 1170 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 470,000 \text{ psi} (1.76) = 827,200 \text{ psi} = 827 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s)(C_M) = 827 \text{ ksi} (0.85)(0.9) = 633 \text{ ksi}$$

- 4.32 ASD – Select Structural Southern Pine, fully braced; bending about strong axis
- a. **2 x 6 joists** at 24 in. o.c. ($C_r = 1.15$); D + S load combination ($C_D = 1.15$)
 C_F is already included in NDS Table 4B values; other factors equal to unity
 $F_b' = F_b (C_D)(C_r) = 2100 \text{ psi} (1.15)(1.15) = 2777 \text{ psi}$
 $F_t' = F_t (C_D) = 1450 \text{ psi} (1.15) = 1668 \text{ psi}$
 $F_v' = F_v (C_D) = 175 \text{ psi} (1.15) = 201 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} = 565 \text{ psi}$
 $F_c' = F_c (C_D) = 1800 \text{ psi} (1.15) = 2070 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E = 1,800,000 \text{ psi}$
 $E_{\min}' = E_{\min} = 660,000 \text{ psi}$
- b. **4 x 12 beam**; D + 0.75(L + L_r) load combination ($C_D = 1.25$)
 $C_F = 1.1$ for bending; other factors equal to unity
 $F_b' = F_b (C_D)(C_F) = 1600 \text{ psi} (1.25)(1.1) = 2200 \text{ psi}$
 $F_t' = F_t (C_D) = 1100 \text{ psi} (1.25) = 1375 \text{ psi}$
 $F_v' = F_v (C_D) = 175 \text{ psi} (1.25) = 219 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} = 565 \text{ psi}$
 $F_c' = F_c (C_D) = 1650 \text{ psi} (1.25) = 2063 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E = 1,800,000 \text{ psi}$
 $E_{\min}' = E_{\min} = 660,000 \text{ psi}$
- c. **2 x 10 purlins** at 4 ft o.c.; D + L_r load combination ($C_D = 1.25$)
 C_F is already incorporated in NDS Table 4B values; other factors equal to unity
 $F_b' = F_b (C_D) = 1700 \text{ psi} (1.25) = 2125 \text{ psi}$
 $F_t' = F_t (C_D) = 1150 \text{ psi} (1.25) = 1438 \text{ psi}$
 $F_v' = F_v (C_D) = 175 \text{ psi} (1.25) = 219 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} = 565 \text{ psi}$
 $F_c' = F_c (C_D) = 1650 \text{ psi} (1.25) = 2063 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E = 1,800,000 \text{ psi}$
 $E_{\min}' = E_{\min} = 660,000 \text{ psi}$
- d. **4 x 10 beams** at 4 ft o.c.; D + 0.75(L + 0.6W) load combination ($C_D = 1.6$)
 $C_F = 1.1$ for bending; other factors equal to unity
 $F_b' = F_b (C_D)(C_F) = 1700 \text{ psi} (1.6)(1.1) = 2992 \text{ psi}$
 $F_t' = F_t (C_D) = 1150 \text{ psi} (1.6) = 1840 \text{ psi}$
 $F_v' = F_v (C_D) = 175 \text{ psi} (1.6) = 280 \text{ psi}$
 $F_{c\perp}' = F_{c\perp} = 565 \text{ psi}$
 $F_c' = F_c (C_D) = 1650 \text{ psi} (1.6) = 2640 \text{ psi}$
Note that C_P would also apply for column buckling of an axially loaded member.
 $E' = E = 1,800,000 \text{ psi}$
 $E_{\min}' = E_{\min} = 660,000 \text{ psi}$
-

4.33 LRFD (K_F and Φ apply) – Select Structural Southern Pine, fully braced; bending about strong axis

a. **2 x 6 joists** at 24 in. o.c. ($C_r = 1.15$); 1.2D + 1.6S load combination ($\lambda = 0.8$)

C_F is already included in NDS Table 4B values; other factors equal to unity

$$A = 8.25 \text{ in}^2; S_x = 7.563 \text{ in}^3$$

Bending moment

$$F_{bn} = F_b (K_F) = 2100 \text{ psi} (2.54) = 5334 \text{ psi} = 5.33 \text{ ksi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_r) = 5.33 \text{ ksi} (0.85)(0.8)(1.15) = 4.17 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 5.07 \text{ ksi} (7.563 \text{ in}^3) = 31.5 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 1450 \text{ psi} (2.7) = 3915 \text{ psi} = 3.92 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 3.92 \text{ ksi} (0.8)(0.8) = 2.51 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 2.51 \text{ ksi} (8.25 \text{ in}^2) = 20.7 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 175 \text{ psi} (2.88) = 504 \text{ psi} = 0.504 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} (0.75)(0.8) = 0.302 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.302 \text{ ksi} (2/3)(8.25 \text{ in}^2) = 1.7 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 565 \text{ psi} (1.67) = 944 \text{ psi} = 0.944 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c) = 0.944 \text{ ksi} (0.9) = 0.849 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 1800 \text{ psi} (2.4) = 4320 \text{ psi} = 4.32 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 4.32 \text{ ksi} (0.9)(0.8) = 3.11 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 3.11 \text{ ksi} (8.25 \text{ in}^2) = 25.7 \text{ k}$$

Note that C_p would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E = 1,800,000 \text{ psi} = 1800 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 660,000 \text{ psi} (1.765) = 1,165,000 \text{ psi} = 1165 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s) = 1165 \text{ ksi} (0.85) = 990 \text{ ksi}$$

b. **4 x 12 beam**; 1.2D + 1.6L + 0.5L_r (occupancy) load combination ($\lambda = 0.8$)

$C_F = 1.1$ for bending; other factors equal to unity

$$A = 39.38 \text{ in}^2; S_x = 73.83 \text{ in}^3$$

Bending moment

$$F_{bn} = F_b (K_F) = 1600 \text{ psi} (2.54) = 4064 \text{ psi} = 4.06 \text{ ksi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_F) = 4.06 \text{ ksi} (0.85)(0.8)(1.1) = 3.04 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 3.04 \text{ ksi} (73.83 \text{ in}^3) = 224 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 1100 \text{ psi} (2.7) = 2970 \text{ psi} = 2.97 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 2.97 \text{ ksi} (0.8)(0.8) = 1.90 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 1.90 \text{ ksi} (39.38 \text{ in}^2) = 74.8 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 175 \text{ psi} (2.88) = 504 \text{ psi} = 0.504 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} (0.75)(0.8) = 0.302 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.302 \text{ ksi} (2/3)(39.38 \text{ in}^2) = 7.9 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 565 \text{ psi} (1.67) = 944 \text{ psi} = 0.944 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c) = 0.944 \text{ ksi} (0.9) = 0.849 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 1650 \text{ psi} (2.4) = 3960 \text{ psi} = 3.96 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 3.96 \text{ ksi} (0.9)(0.8) = 2.85 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 2.85 \text{ ksi} (39.38 \text{ in}^2) = 112 \text{ k}$$

Note that C_P would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E = 1,800,000 \text{ psi} = 1800 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 660,000 \text{ psi} (1.76) = 1,161,600 \text{ psi} = 1162 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s) = 1162 \text{ ksi} (0.85) = 987 \text{ ksi}$$

- c. **2 x 10 purlins** at 4 ft o.c.; 1.2D + 1.6L_T load combination ($\lambda = 0.8$)

C_F is already incorporated in NDS Table 4B values; other factors equal to unity

$$A = 13.88 \text{ in}^2; S_x = 21.39 \text{ in}^3$$

Bending moment

$$F_{bn} = F_b (K_F) = 1700 \text{ psi} (2.54) = 4318 \text{ psi} = 4.32 \text{ ksi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda) = 4.32 \text{ ksi} (0.85)(0.8) = 2.94 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 3.54 \text{ ksi} (21.39 \text{ in}^3) = 62.8 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 1150 \text{ psi} (2.7) = 3105 \text{ psi} = 3.11 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 3.11 \text{ ksi} (0.8)(0.8) = 1.99 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 1.99 \text{ ksi} (13.88 \text{ in}^2) = 26.6 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 175 \text{ psi} (2.88) = 504 \text{ psi} = 0.504 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} (0.75)(0.8) = 0.302 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.302 \text{ ksi} (2/3)(13.88 \text{ in}^2) = 2.8 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 565 \text{ psi} (1.67) = 944 \text{ psi} = 0.944 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c) = 0.944 \text{ ksi} (0.9) = 0.849 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 1650 \text{ psi} (2.4) = 3960 \text{ psi} = 3.96 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 3.96 \text{ ksi} (0.9)(0.8) = 2.85 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 2.85 \text{ ksi} (13.88 \text{ in}^2) = 39.6 \text{ k}$$

Note that C_P would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E = 1,800,000 \text{ psi} = 1800 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 660,000 \text{ psi} (1.76) = 1,161,600 \text{ psi} = 1162 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s) = 1162 \text{ ksi} (0.85) = 987 \text{ ksi}$$

- d. **4 x 10 beams** at 4 ft o.c.; 1.2D + W + L load combination ($\lambda = 1.0$)

$C_F = 1.1$ for bending; other factors equal to unity

$$A = 32.38 \text{ in}^2; S_x = 49.91 \text{ in}^3$$

Bending moment

$$F_{bn} = F_b (K_F) = 1700 \text{ psi} (2.54) = 4318 \text{ psi} = 4.32 \text{ ksi}$$

$$F_{bn}' = F_{bn} (\Phi_b)(\lambda)(C_F) = 4.32 \text{ ksi} (0.85)(1.0)(1.1) = 4.04 \text{ ksi}$$

$$M_n' = F_{bn}' (S_x) = 4.04 \text{ ksi} (49.91 \text{ in}^3) = 202 \text{ k-in.}$$

Tension

$$F_{tn} = F_t (K_F) = 1150 \text{ psi} (2.7) = 3105 \text{ psi} = 3.11 \text{ ksi}$$

$$F_{tn}' = F_{tn} (\Phi_t)(\lambda) = 3.11 \text{ ksi} (0.8)(1.0) = 2.48 \text{ ksi}$$

$$T_n' = F_{tn}' (A) = 2.48 \text{ ksi} (32.38 \text{ in}^2) = 80.4 \text{ k}$$

Flexural Shear

$$F_{vn} = F_v (K_F) = 175 \text{ psi} (2.88) = 504 \text{ psi} = 0.504 \text{ ksi}$$

$$F_{vn}' = F_{vn} (\Phi_v)(\lambda) = 0.504 \text{ ksi} (0.75)(1.0) = 0.378 \text{ ksi}$$

$$V_n' = F_{vn}' (2/3)(A) = 0.378 \text{ ksi} (2/3)(32.38 \text{ in}^2) = 8.2 \text{ k}$$

Compression perpendicular to grain (bearing)

$$F_{c\perp n} = F_{c\perp} (K_F) = 565 \text{ psi} (1.67) = 944 \text{ psi} = 0.944 \text{ ksi}$$

$$F_{c\perp n}' = F_{c\perp n} (\Phi_c) = 0.944 \text{ ksi} (0.9) = 0.849 \text{ ksi}$$

Compression parallel to grain

$$F_{cn} = F_c (K_F) = 1650 \text{ psi} (2.4) = 3960 \text{ psi} = 3.96 \text{ ksi}$$

$$F_{cn}' = F_{cn} (\Phi_c)(\lambda) = 3.96 \text{ ksi} (0.9)(1.0) = 3.56 \text{ ksi}$$

$$P_n' = F_{cn}' (A) = 3.56 \text{ ksi} (32.38 \text{ in}^2) = 115 \text{ k}$$

Note that C_P would also apply for column buckling of an axially loaded member.

Modulus of Elasticity

$$E' = E = 1,800,000 \text{ psi} = 1800 \text{ ksi}$$

$$E_{\min-n} = E_{\min} (K_F) = 660,000 \text{ psi} (1.76) = 1,161,600 \text{ psi} = 1162 \text{ ksi}$$

$$E_{\min-n}' = E_{\min-n} (\Phi_s) = 1162 \text{ ksi} (0.85) = 987 \text{ ksi}$$

4.34 $SV = \frac{6}{30} = 0.2\%$ per 1% change in MC = 0.002 in./in./percent change in MC
 $\Delta MC = 10 - 19 = -9$ (drying)
Shrinkage = (SV)(ΔMC) $d = (0.002)(-9)(13.25 \text{ in.}) = 0.24 \text{ in.}$
Depth after shrinkage = $13.25 - 0.24 \text{ in.} = 13 \text{ in.}$

4.35 $SV = \frac{6}{30} = 0.2\%$ per 1% change in MC = 0.002 in./in./percent change in MC
 $\Delta MC = 9 - 19 = -10$ (drying)
Shrinkage in 2 x 10 = (SV)(ΔMC) $d = (0.002)(-10)(9.25 \text{ in.}) = 0.185 \text{ in.}$
Shrinkage in 2 x plate = (SV)(ΔMC) $d = (0.002)(-10)(1.5 \text{ in.}) = 0.03 \text{ in.}$
three 2 x 12's; twelve 2 x plates
Total shrinkage = $3(0.185 \text{ in.}) + 12(0.03 \text{ in.}) = 0.9 \text{ in.}$
