#### Numerical Methods for Engineers 6th Edition Chapra Solutions Manual

Full Download: http://alibabadownload.com/product/numerical-methods-for-engineers-6th-edition-chapra-solutions-manual/

1

# **CHAPTER 2**

2.1 Two possible versions can be developed:

```
IF x \ge 10 THEN
       IF x \ge 10 THEN
         DO
                                           DO
           x = x - 5
                                             x = x - 5
           IF x < 50 EXIT
                                             IF x < 50 EXIT
         END DO
                                            END DO
       ELSE
                                          ELSEIF x < 5
         IF x < 5 THEN
                                           x = 5
           x = 5
                                          ELSE
         ELSE
                                           x = 7.5
           x = 7.5
                                          ENDIF
         END IF
       ENDIF
2.2
   DO
     i = i + 1
     IF z > 50 EXIT
     x = x + 5
     IF x > 5 THEN
       y = x
     ELSE
      y = 0
     ENDIF
     z = x + y
   ENDDO
```

**2.3** Students could implement the subprogram in any number of languages. The following VBA program is one example. It should be noted that the availability of complex variables in languages such as Fortran 90 would allow this subroutine to be made even more concise. However, we did not exploit this feature, in order to make the code more compatible with languages that do not support complex variables.

```
Option Explicit
Sub Rootfind()
Dim ier As Integer
Dim a As Double, b As Double, c As Double
Dim r1 As Double, i1 As Double, r2 As Double, i2 As Double
a = 7: b = 6: c = 2
Call Roots(a, b, c, ier, r1, i1, r2, i2)
If ier = 0 Then
 MsqBox "No roots"
ElseIf ier = 1 Then
 MsgBox "single root=" & r1
ElseIf ier = 2 Then
 MsgBox "real roots = " & r1 & ", " & r2
ElseIf ier = 3 Then
 MsgBox "complex roots =" & r1 & "," & i1 & " i" & "; "_
                         & r2 & "," & i2 & " i"
End If
End Sub
Sub Roots(a, b, c, ier, r1, i1, r2, i2)
Dim d As Double
r1 = 0: r2 = 0: i1 = 0: i2 = 0
```

**PROPRIETARY MATERIAL.** © The McGraw-Hill Companies, Inc. All rights reserved. <u>No part of this Manual</u> may be displayed, reproduced or distributed in any form or by any means, without the prior written permission of the publisher, or used beyond the limited distribution to teachers and educators permitted by McGraw-Hill for their individual course preparation. If you are a student using this Manual, you are using it without permission.

#### This sample only, Download all chapters at: alibabadownload.com

```
If a = 0 Then
  If b <> 0 Then
    r1 = -c / b
    ier = 1
  Else
   ier = 0
  End If
Else
  d = b ^ 2 - 4 * a * c
  If (d \ge 0) Then
    r1 = (-b + Sqr(d)) / (2 * a)
   r2 = (-b - Sqr(d)) / (2 * a)
    ier = 2
  Else
    r1 = -b / (2 * a)
    r2 = r1
    i1 = Sqr(Abs(d)) / (2 * a)
    i2 = -i1
    ier = 3
  End If
End If
End Sub
```

The answers for the 3 test cases are: (a) -0.3542, -5.646; (b) 0.4; (c) -0.4167 + 1.4696i; -0.4167 - 1.4696i.

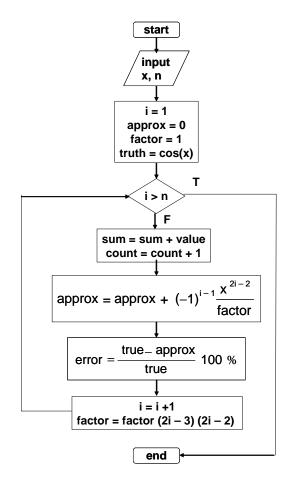
Several features of this subroutine bear mention:

- The subroutine does not involve input or output. Rather, information is passed in and out via the arguments. This is often the preferred style, because the I/O is left to the discretion of the programmer within the calling program.
- Note that a variable is passed (IER) in order to distinguish among the various cases.
- **2.4** The development of the algorithm hinges on recognizing that the series approximation of the cosine can be represented concisely by the summation,

$$\sum_{i=1}^{n} (-1)^{i-1} \frac{x^{2i-2}}{(2i-2)!}$$

where i = the order of the approximation.

(a) Structured flowchart



(b) Pseudocode:

```
SUBROUTINE Coscomp(n,x)

i = 1

approx = 0

factor = 1

truth = cos(x)

DO

IF i > n EXIT

approx = approx + (-1)^{i-1} \cdot x^{2 \cdot i-2} / factor

error = (true - approx) / true) * 100

DISPLAY i, true, approx, error

i = i + 1

factor = factor \cdot (2 \cdot i - 3) \cdot (2 \cdot i - 2)

END DO

END
```

2.5 Students could implement the subprogram in any number of languages. The following MATLAB Mfile is one example. It should be noted that MATLAB allows direct calculation of the factorial through its intrinsic function factorial. However, we did not exploit this feature, in order to make the code more compatible with languages such as Visual BASIC and Fortran.

```
function coscomp(x,n)
i = 1;
tru = cos(x);
approx = 0;
f = 1;
```

```
fprintf('\n');
fprintf('order true value approximation error\n');
while (1)
    if i > n, break, end
    approx = approx + (-1)^(i - 1) * x^(2*i-2) / f;
    er = (tru - approx) / tru * 100;
    fprintf('%3d %14.10f %14.10f %12.8f\n',i,tru,approx,er);
    i = i + 1;
    f = f*(2*i-3)*(2*i-2);
end
```

Here is a run of the program showing the output that is generated:

**2.6 (a)** The following pseudocode provides an algorithm for this problem. Notice that the input of the quizzes and homeworks is done with logical loops that terminate when the user enters a negative grade:

```
INPUT WQ, WH, WF
nq = 0
sumq = 0
DO
 INPUT quiz (enter negative to signal end of quizzes)
 IF quiz < 0 EXIT
 nq = nq + 1
 sumq = sumq + quiz
END DO
AQ = sumq / nq
nh = 0
sumh = 0
DO
  INPUT homework (enter negative to signal end of homeworks)
 TF homework < 0 EXTT
 nh = nh + 1
 sumh = sumh + homework
END DO
AH = sumh / nh
DISPLAY "Is there a final grade (y or n)"
INPUT answer
IF answer = "y" THEN
  TNPUT FE
  AG = (WQ * AQ + WH * AH + WF * FE) / (WQ + WH + WF)
ELSE
  AG = (WQ * AQ + WH * AH) / (WQ + WH)
END IF
DISPLAY AG
END
```

(b) Students could implement the program in any number of languages. The following VBA code is one example.

```
Sub Grader()
Dim WQ As Double, WH As Double, WF As Double
Dim ng As Integer, sumg As Double, AQ As Double
Dim nh As Integer, sumh As Double, AH As Double
Dim answer As String, FE As Double
Dim AG As Double
'enter weights
WQ = InputBox("enter quiz weight")
WH = InputBox("enter homework weight")
WF = InputBox("enter final exam weight")
'enter quiz grades
nq = 0
sumq = 0
Do
 quiz = InputBox("enter negative to signal end of quizzes")
 If quiz < 0 Then Exit Do
 nq = nq + 1
 sumq = sumq + quiz
Loop
AQ = sumq / nq
'enter homework grades
nh = 0
sumh = 0
Do
 homework = InputBox("enter negative to signal end of homeworks")
 If homework < 0 Then Exit Do
 nh = nh + 1
 sumh = sumh + homework
Loop
AH = sumh / nh
'determine and display the average grade
answer = InputBox("Is there a final grade (y or n)")
If answer = "y" Then
 FE = InputBox("final grade:")
 AG = (WQ * AQ + WH * AH + WF * FE) / (WQ + WH + WF)
Else
 AG = (WQ * AQ + WH * AH) / (WQ + WH)
End If
MsgBox "Average grade = " & AG
End Sub
```

The results should conform to:

AQ = 437/5 = 87.4AH = 541/6 = 90.1667

without final

$$AG = \frac{35(87.4) + 30(90.1667)}{35 + 30} = 88.677$$

with final

$$AG = \frac{35(87.4) + 30(90.1667) + 35(92)}{35 + 30 + 35} = 89.84$$

2.7 (a) Pseudocode:

$$IF a > 0 THEN$$
$$tol = 10^{-5}$$

```
x = a/2

DO

y = (x + a/x)/2

e = |(y - x)/y|

x = y

IF e < tol EXIT

END DO

SquareRoot = x

ELSE

SquareRoot = 0

END IF
```

(b) Students could implement the function in any number of languages. The following VBA and MATLAB codes are two possible options.

VBA Function Procedure	MATLAB M-File
Option Explicit	<pre>function s = SquareRoot(a)</pre>
Function SquareRoot(a)	if a > 0
Dim x As Double, y As Double	tol = 0.00001;
Dim e As Double, tol As Double	x = a / 2;
If a > 0 Then	while(1)
tol = 0.00001	y = (x + a / x) / 2;
x = a / 2	e = abs((y - x) / y);
Do	x = y;
y = (x + a / x) / 2	if e < tol, break, end
e = Abs((y - x) / y)	end
x = y	s = xi
If e < tol Then Exit Do	else
Loop	s = 0;
SquareRoot = $x$	end
Else	
SquareRoot = 0	
End If	
End Function	

2.8 A MATLAB M-file can be written to solve this problem as

```
function futureworth(P, i, n)
nn = 0:n;
F = P*(1+i).^nn;
y = [nn;F];
fprintf('\n year future worth\n');
fprintf('%5d %14.2f\n',y);
```

This function can be used to evaluate the test case,

2.9 A MATLAB M-file can be written to solve this problem as

```
function annualpayment(P, i, n)
nn = 1:n;
```

```
A = P*i*(1+i).^nn./((1+i).^nn-1);
y = [nn;A];
fprintf('\n year annual payment\n');
fprintf('%5d %14.2f\n',y);
```

This function can be used to evaluate the test case,

**2.10** Students could implement the function in any number of languages. The following VBA and MATLAB codes are two possible options.

VBA Function Procedure	MATLAB M-File
Option Explicit	<pre>function Ta = avgtemp(Tm,Tp,ts,te)</pre>
Function avgtemp(Tm, Tp, ts, te)	w = 2*pi/365;
Dim pi As Double, w As Double	t = ts:te;
Dim Temp As Double, t As Double	T = Tm + (Tp-Tm)*cos(w*(t-205));
Dim sum As Double, i As Integer	Ta = mean(T);
Dim n As Integer	
pi = 4 * Atn(1)	
w = 2 * pi / 365	
sum = 0	
n = 0	
t = ts	
For i = ts To te	
Temp = Tm + (Tp - Tm) * Cos(w*(t-205))	
sum = sum + Temp	
n = n + 1	
t = t + 1	
Next i	
avgtemp = sum / n	
End Function	

The function can be used to evaluate the test cases. The following show the results for MATLAB,

```
>> avgtemp(22.1,28.3,0,59)
ans =
    16.2148
>> avgtemp(10.7,22.9,180,242)
ans =
    22.2491
```

**2.11** The programs are student specific and will be similar to the codes developed for VBA and MATLAB as outlined in sections 2.4 and 2.5. The numerical results for the different time steps are tabulated below along with an estimate of the absolute value of the true relative error at t = 12 s:

Step	<i>v</i> (12)	$ \varepsilon_t $ (%)
2	49.96	5.2
1	48.70	2.6

The general conclusion is that the error is halved when the step size is halved.

**2.12** Students could implement the subprogram in any number of languages. The following VBA/Excel and MATLAB programs are two examples based on the algorithm outlined in Fig. P2.15.

VBA/Excel	MATLAB
Option Explicit	
Sub Bubble(n, b)	function $y = Bubble(x)$
Dim m As Integer, i As Integer	n = length(x);
Dim switch As Boolean, dum As Double	m = n - 1;
m = n - 1	b = xi
Do	while(1)
switch = False	s = 0;
For i = 1 To m	for i = 1:m
If $b(i) > b(i + 1)$ Then	if b(i) > b(i + 1)
dum = b(i)	dum = b(i);
b(i) = b(i + 1)	b(i) = b(i + 1);
b(i + 1) = dum	b(i + 1) = dum;
switch = True	s = 1;
End If	end
Next i	end
If switch = False Then Exit Do	if s == 0, break, end
m = m - 1	m = m - 1;
Loop	end
End Sub	y = b;

Notice how the MATLAB length function allows us to omit the length of the vector in the function argument. Here is an example MATLAB session that invokes the function to sort a vector:

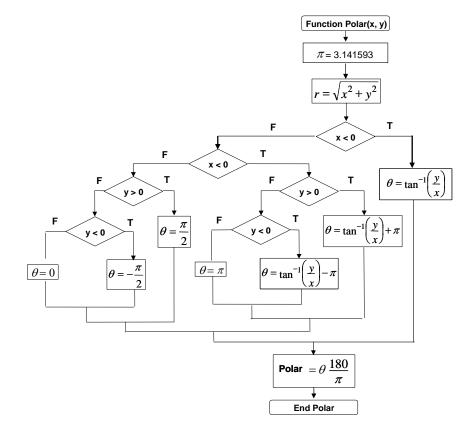
**2.13** Students could implement the function in any number of languages. The following VBA and MATLAB codes are two possible options.

VBA Function Procedure	MATLAB M-File
Option Explicit	<pre>function Vol = tankvolume(R, d)</pre>
Function Vol(R, d)	if d < R
Dim V1 As Double, V2 As Double	Vol = pi * d ^ 3 / 3;
Dim pi As Double	elseif d <= 3 * R
pi = 4 * Atn(1)	V1 = pi * R ^ 3 / 3;
If d < R Then	V2 = pi * R ^ 2 * (d - R);
Vol = pi * d ^ 3 / 3	Vol = V1 + V2;
ElseIf d <= 3 * R Then	else
V1 = pi * R ^ 3 / 3	Vol = 'overtop';
V2 = pi * R ^ 2 * (d - R)	end
Vol = V1 + V2	
Else	
Vol = "overtop"	
End If	
End Function	

The results are:

R	d	Volume
1	0.5	0.1309
1	1.2	1.675516
1	3	7.330383
1	3.1	overtop

**2.14** Here is a flowchart for the algorithm:



Students could implement the function in any number of languages. The following MATLAB M-file is one option. Versions in other languages such as Fortran 90, Visual Basic, or C would have a similar structure.

```
function polar(x, y)
r = sqrt(x .^{2} + y .^{2});
n = length(x);
for i = 1:n
  if x(i) > 0
    th(i) = atan(y(i) / x(i));
  elseif x(i) < 0
    if y(i) > 0
      th(i) = atan(y(i) / x(i)) + pi;
    elseif y(i) < 0
      th(i) = atan(y(i) / x(i)) - pi;
    else
      th(i) = pi;
    end
  else
    if y(i) > 0
```

```
th(i) = pi / 2;
    elseif y(i) < 0
      th(i) = -pi / 2;
    else
      th(i) = 0;
    end
  end
  th(i) = th(i) * 180 / pi;
end
ou=[x;y;r;th];
fprintf('\n
                х
                         У
                                  radius
                                             angle\n');
fprintf('%8.2f %8.2f %10.4f %10.4f\n',ou);
```

This function can be used to evaluate the test cases.

```
>> x=[1 1 1 -1 -1 -1 0 0 0];
>> y=[1 -1 0 1 -1 0 1 -1 0];
>> polar(x,y)
                               angle
    х
                     radius
             У
    1.00
            1.00
                     1.4142
                               45.0000
   1.00
           -1.00
                     1.4142
                              -45.0000
            0.00
                               0.0000
   1.00
                     1.0000
   -1.00
           1.00
                     1.4142
                             135.0000
  -1.00
           -1.00
                     1.4142
                             -135.0000
   -1.00
           0.00
                     1.0000
                             180.0000
   0.00
           1.00
                     1.0000
                               90.0000
    0.00
           -1.00
                     1.0000
                              -90.0000
   0.00
            0.00
                     0.0000
                                0.0000
```

**2.15** Students could implement the function in any number of languages. The following VBA and MATLAB codes are two possible options.

VBA Function Procedure	MATLAB M-File
Function grade(s)	<pre>function grade = lettergrade(score)</pre>
If $s \ge 90$ Then	if score >= 90
grade = "A"	grade = 'A';
ElseIf s $\geq$ 80 Then	elseif score >= 80
grade = "B"	grade = 'B';
ElseIf s $\geq$ 70 Then	elseif score >= 70
grade = "C"	grade = 'C';
ElseIf s $\geq$ 60 Then	elseif score >= 60
grade = "D"	grade = 'D';
Else	else
grade = "F"	grade = 'F';
End If	end
End Function	

**2.16** Students could implement the functions in any number of languages. The following VBA and MATLAB codes are two possible options.

VBA Function Procedure	MATLAB M-File
(a) Factorial	
Function factor(n)	<pre>function fout = factor(n)</pre>
Dim x As Long, i As Integer	x = 1;
x = 1	for $i = 1:n$
For i = 1 To n	x = x * i;
x = x * i	end
Next i	fout = x;
factor = x	

```
End Function
(b) Minimum
Function min(x, n)
                                     function xm = xmin(x)
Dim i As Integer
                                     n = length(x);
                                     xm = x(1);
\min = x(1)
For i = 2 To n
                                     for i = 2:n
 If x(i) < \min Then \min = x(i)
                                      if x(i) < xm, xm = x(i); end
Next i
                                     end
End Function
(c) Average
                                     function xm = xmean(x)
Function mean(x, n)
Dim sum As Double
                                     n = length(x);
Dim i As Integer
                                     s = x(1);
sum = x(1)
                                     for i = 2:n
For i = 2 To n
                                      s = s + x(i);
 sum = sum + x(i)
                                     end
Next i
                                     xm = s / n;
mean = sum / n
End Function
```

**2.17** Students could implement the functions in any number of languages. The following VBA and MATLAB codes are two possible options.

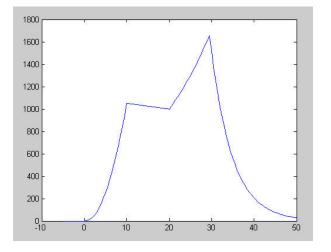
VBA Function Procedure	MATLAB M-File
(a) Square root sum of squares	
Function SSS(x, n, m)	function $s = SSS(x)$
Dim i As Integer, j As Integer	[n,m] = size(x);
SSS = 0	s = 0;
For i = 1 To n	for $i = 1:n$
For j = 1 To m	for $j = 1:m$
$SSS = SSS + x(i, j) ^ 2$	$s = s + x(i, j) ^ 2;$
Next j	end
Next i	end
SSS = Sqr(SSS)	s = sqrt(s);
End Function	
(b) Normalization	function of normal(m)
Sub normal(x, n, m, y)	<pre>function y = normal(x) [n,m] = size(x);</pre>
Dim i As Integer, j As Integer Dim max As Double	[n,m] = Size(x), for i = 1:n
For $i = 1$ To n	mx = abs(x(i, 1));
$\max = \operatorname{Abs}(x(i, 1))$	for $j = 2:m$
For $j = 2$ To m	if $abs(x(i, j)) > mx$
If $Abs(x(i, j)) > max$ Then	mx = x(i, j);
$\max = x(i, j)$	end
End If	end
Next j	for $j = 1:m$
For j = 1 To m	y(i, j) = x(i, j) / mx;
y(i, j) = x(i, j) / max	end
Next j	end
Next i	
End Sub	Alternate version:
	function $y = normal(x)$
	n = size(x);
	for i = 1:n
	y(i,:) = x(i,:)/max(x(i,:));
	end

2.18 The following MATLAB function implements the piecewise function:

```
function v = vpiece(t)
if t<0
    v = 0;
elseif t<10
    v = 11*t^2 - 5*t;
elseif t<20
    v = 1100 - 5*t;
elseif t<30
    v = 50*t + 2*(t - 20)^2;
else
    v = 1520*exp(-0.2*(t-30));
end</pre>
```

Here is a script that uses vpiece to generate the plot

```
k=0;
for i = -5:.5:50
    k=k+1;
    t(k)=i;
    v(k)=vpiece(t(k));
end
plot(t,v)
```



**2.19** The following MATLAB function implements the algorithm:

```
function nd = days(mo, da, leap)
nd = 0;
for m=1:mo-1
  switch m
    case {1, 3, 5, 7, 8, 10, 12}
    nday = 31;
    case {4, 6, 9, 11}
    nday = 30;
    case 2
    nday = 28+leap;
  end
  nd=nd+nday;
end
nd = nd + da;
```

**2.20** The following MATLAB function implements the algorithm:

```
function nd = days(mo, da, year)
leap = 0;
if year / 4 - fix(year / 4) == 0, leap = 1; end
nd = 0;
for m=1:mo-1
 switch m
   case {1, 3, 5, 7, 8, 10, 12}
     nday = 31;
    case {4, 6, 9, 11}
     nday = 30;
    case 2
     nday = 28+leap;
  end
 nd=nd+nday;
end
nd = nd + da;
>> days(1,1,1999)
ans =
    1
>> days(2,29,2000)
ans =
    60
>> days(3,1,2001)
ans =
   60
>> days(6,21,2002)
ans =
  172
>> days(12,31,2004)
ans =
  366
```

2.21 A MATLAB M-file can be written as

```
function Manning(A)
A(:,5)=sqrt(A(:,2))./A(:,1).*(A(:,3).*A(:,4)./(A(:,3)+2*A(:,4))).^(2/3);
fprintf('\n n S B H U\n');
fprintf('%8.3f %8.4f %10.2f %10.2f %10.4f\n',A');
```

This function can be run to create the table,

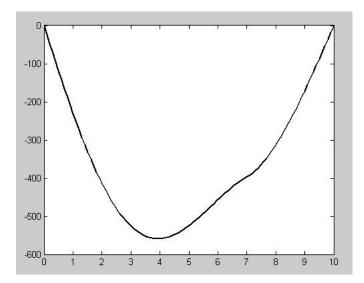
```
>> A=[.035 .0001 10 2
.020 .0002 8 1
.015 .001 20 1.5
.03 .0007 24 3
.022 .0003 15 2.5];
>> Manning(A)
              S
                         В
                                     Н
                                                 U
   n
   0.035
           0.0001
                        10.00
                                    2.00
                                              0.3624
   0.020
           0.0002
                         8.00
                                    1.00
                                              0.6094
   0.015
           0.0010
                        20.00
                                    1.50
                                              2.5167
                        24.00
   0.030
           0.0007
                                    3.00
                                              1.5809
                        15.00
                                    2.50
   0.022
           0.0003
                                              1.1971
```

#### 2.22 A MATLAB M-file can be written as

```
function beam(x)
xx = linspace(0,x);
n=length(xx);
for i=1:n
    uy(i) = -5/6.*(sing(xx(i),0,4)-sing(xx(i),5,4));
    uy(i) = uy(i) + 15/6.*sing(xx(i),8,3) + 75*sing(xx(i),7,2);
    uy(i) = uy(i) + 57/6.*xx(i)^3 - 238.25.*xx(i);
end
plot(xx,uy)
function s = sing(xxx,a,n)
if xxx > a
    s = (xxx - a).^n;
else
    s=0;
end
```

This function can be run to create the plot,

>> beam(10)



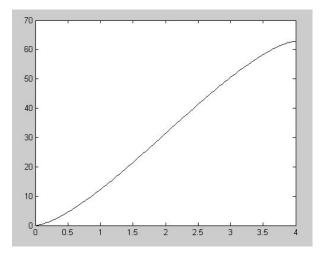
2.23 A MATLAB M-file can be written as

function cylinder(r, L)

h = linspace(0,2\*r); V = (r^2\*acos((r-h)./r)-(r-h).\*sqrt(2\*r\*h-h.^2))\*L; plot(h, V)

This function can be run to create the plot,

>> cylinder(2,5)



**2.24** Before the chute opens (t < 10), Euler's method can be implemented as

$$v(t + \Delta t) = v(t) + \left[9.8 - \frac{10}{80}v(t)\right]\Delta t$$

After the chute opens ( $t \ge 10$ ), the drag coefficient is changed and the implementation becomes

$$v(t + \Delta t) = v(t) + \left[9.8 - \frac{50}{80}v(t)\right]\Delta t$$

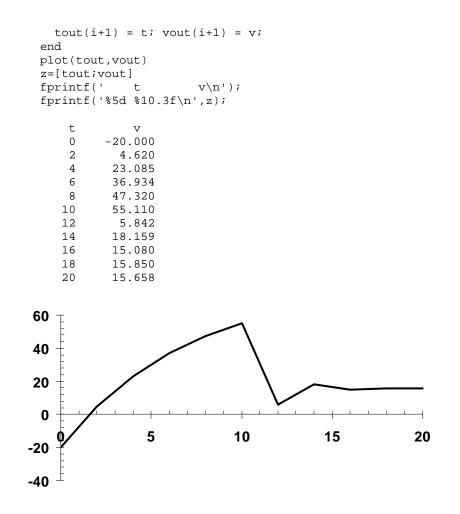
You can implement the subprogram in any number of languages. The following MATLAB M-file is one example. Notice that the results are inaccurate because the stepsize is too big. A smaller stepsize should be used to attain adequate accuracy.

```
function parachute
g = 9.81;
m = 80; c = 10;
ti = 0; tf = 20; dt = 2;
vi = -20;
tc = 10; cc = 50;
np = (tf - ti) / dt;
t = ti; v = vi;
tout(1) = t; vout(1) = v;
for i = 1:np
  if t < tc
    dvdt = g - c / m * v;
  else
    dvdt = g - cc / m * v;
  end
  v = v + dvdt * dt;
  t = t + dt;
```

## Numerical Methods for Engineers 6th Edition Chapra Solutions Manual

Full Download: http://alibabadownload.com/product/numerical-methods-for-engineers-6th-edition-chapra-solutions-manual/

16



**2.25** Students could implement the function in any number of languages. The following VBA and MATLAB codes are two possible options.

VBA/Excel	MATLAB
Option Explicit	
Function fac(n)	function $f = fac(n)$
Dim x As Long, i As Integer	
If $n \ge 0$ Then	if n >= 0
x = 1	x = 1;
For i = 1 To n	for $i = 1$ : n
x = x * i	x = x * i;
Next i	end
fac = x	f = x;
Else	else
MsgBox "value must be positive"	error 'value must be positive'
End	end
End If	
End Function	

**PROPRIETARY MATERIAL.** © The McGraw-Hill Companies, Inc. All rights reserved. <u>No part of this Manual</u> may be displayed, reproduced or distributed in any form or by any means, without the prior written permission of the publisher, or used beyond the limited distribution to teachers and educators permitted by McGraw-Hill for their individual course preparation. If you are a student using this Manual, you are using it without permission.

### This sample only, Download all chapters at: alibabadownload.com