Mathematical Statistics with Applications 7th Edition Miller Solutions Manual

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Chapter 1: What is Statistics?

1.1

a. <u>Population</u>: all tires manufactured by the company for the specific year. <u>Objective</u>: to estimate the proportion of tires with unsafe tread.

b. <u>Population</u>: all adult residents of the particular state. <u>Objective</u>: to estimate the proportion who favor a unicameral legislature.

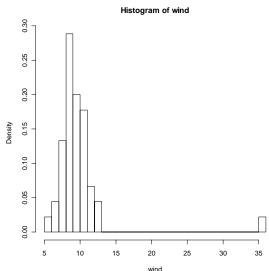
c. <u>Population</u>: times until recurrence for all people who have had a particular disease. <u>Objective</u>: to estimate the true average time until recurrence.

d. <u>Population</u>: lifetime measurements for all resistors of this type. <u>Objective</u>: to estimate the true mean lifetime (in hours).

e. <u>Population</u>: all generation X age US citizens (specifically, assign a '1' to those who want to start their own business and a '0' to those who do not, so that the population is the set of 1's and 0's). <u>Objective</u>: to estimate the proportion of generation X age US citizens who want to start their own business.

f. <u>Population</u>: all healthy adults in the US. <u>Objective</u>: to estimate the true mean body temperature

g. <u>Population</u>: single family dwelling units in the city. <u>Objective</u>: to estimate the true mean water consumption

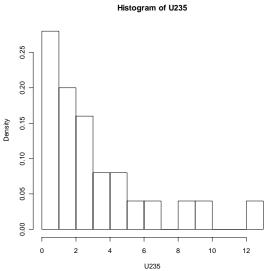


1.2 a. This histogram is above.

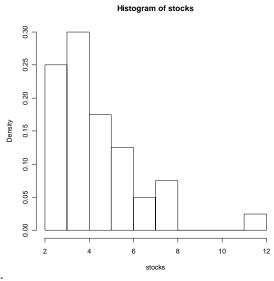
b. Yes, it is quite windy there.

c. 11/45, or approx. 24.4%

d. it is not especially windy in the overall sample.



1.3 The histogram is above.



- **a.** The histogram is above. **b.** 18/40 = 45% **c.** 29/40 = 72.5%
- **a.** The categories with the largest grouping of students are 2.45 to 2.65 and 2.65 to 2.85. (both have 7 students). **b.** 7/30 **c.** 7/30 + 3/30 + 3/30 + 3/30 = 16/30
- **1.6 a.** The modal category is 2 (quarts of milk). About 36% (9 people) of the 25 are in this category.

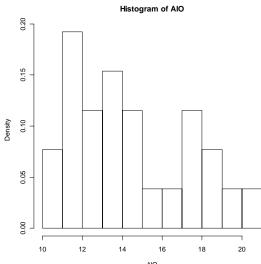
b. .2 + .12 + .04 = .36

c. Note that 8% purchased 0 while 4% purchased 5. Thus, 1 - .08 - .04 = .88 purchased between 1 and 4 quarts.

1.7 a. There is a possibility of bimodality in the distribution.

b. There is a dip in heights at 68 inches.

c. If all of the students are roughly the same age, the bimodality could be a result of the men/women distributions.



- **a.** The histogram is above. **b.** The data appears to be bimodal. Llanederyn and Caldicot have lower sample values than the other two.
- a. Note that 9.7 = 12 2.3 and 14.3 = 12 + 2.3. So, (9.7, 14.3) should contain approximately 68% of the values.
 b. Note that 7.4 = 12 2(2.3) and 16.6 = 12 + 2(2.3). So, (7.4, 16.6) should contain approximately 95% of the values.
 c. From parts (a) and (b) above, 95% 68% = 27% lie in both (14.3. 16.6) and (7.4, 9.7). By symmetry, 13.5% should lie in (14.3, 16.6) so that 68% + 13.5% = 81.5% are in (9.7, 16.6)
 d. Since 5.1 and 18.0 represent three standard deviations away from the mean the

d. Since 5.1 and 18.9 represent three standard deviations away from the mean, the proportion outside of these limits is approximately 0.

1.10 a. 14 - 17 = -3.

b. Since 68% lie within one standard deviation of the mean, 32% should lie outside. By symmetry, 16% should lie below one standard deviation from the mean.

c. If normally distributed, approximately 16% of people would spend less than -3 hours on the internet. Since this doesn't make sense, the population is not normal.

1.11 a.
$$\sum_{i=1}^{n} c = c + c + \dots + c = nc.$$

b. $\sum_{i=1}^{n} cy_i = c(y_1 + \dots + y_n) = c\sum_{i=1}^{n} y_i$
c. $\sum_{i=1}^{n} (x_i + y_i) = x_1 + y_1 + x_2 + y_2 + \dots + x_n + y_n = (x_1 + x_2 + \dots + x_n) + (y_1 + y_2 + \dots + y_n)$

= 1.21.

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Using the above, the numerator of
$$s^2$$
 is $\sum_{i=1}^n (y_i - \overline{y})^2 = \sum_{i=1}^n (y_i^2 - 2y_i\overline{y} + \overline{y}^2) = \sum_{i=1}^n y_i^2 - 2\overline{y}\sum_{i=1}^n y_i + n\overline{y}^2$ Since $n\overline{y} = \sum_{i=1}^n y_i$, we have $\sum_{i=1}^n (y_i - \overline{y})^2 = \sum_{i=1}^n y_i^2 - n\overline{y}^2$. Let $\overline{y} = \frac{1}{n}\sum_{i=1}^n y_i$ to get the result.

1.12 Using the data,
$$\sum_{i=1}^{6} y_i = 14$$
 and $\sum_{i=1}^{6} y_i^2 = 40$. So, $s^2 = (40 - 14^2/6)/5 = 1.47$. So, s

1.13 a. With $\sum_{i=1}^{45} y_i = 440.6$ and $\sum_{i=1}^{45} y_i^2 = 5067.38$, we have that $\overline{y} = 9.79$ and s = 4.14. b.

k	interval	frequency	Exp. frequency
1	5.65, 13.93	44	30.6
2	1.51, 18.07	44	42.75
3	-2.63, 22.21	44	45

1.14 a. With
$$\sum_{i=1}^{25} y_i = 80.63$$
 and $\sum_{i=1}^{25} y_i^2 = 500.7459$, we have that $\overline{y} = 3.23$ and $s = 3.17$.

b.

k	interval	frequency	Exp. frequency
1	0.063, 6.397	21	17
2	-3.104, 9.564	23	23.75
3	-6.271, 12.731	25	25

1.15 a. With
$$\sum_{i=1}^{40} y_i = 175.48$$
 and $\sum_{i=1}^{40} {y_i}^2 = 906.4118$, we have that $\overline{y} = 4.39$ and $s = 1.87$.

b.

k	interval	frequency	Exp. frequency
1	2.52, 6.26	35	27.2
2	0.65, 8.13	39	38
3	-1.22, 10	39	40

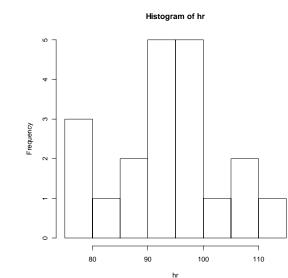
a. Without the extreme value, $\overline{y} = 4.19$ and s = 1.44. 1.16 **b.** These counts compare more favorably:

k	interval	frequency	Exp. frequency
1	2.75, 5.63	25	26.52
2	1.31, 7.07	36	37.05
3	-0.13, 8.51	39	39

- **1.18** The approximation is (800-200)/4 = 150.
- **1.19** One standard deviation below the mean is 34 53 = -19. The empirical rule suggests that 16% of all measurements should lie one standard deviation below the mean. Since chloroform measurements cannot be negative, this population cannot be normally distributed.
- **1.20** Since approximately 68% will fall between \$390 (\$420 \$30) to \$450 (\$420 + \$30), the proportion above \$450 is approximately 16%.
- **1.21** (Similar to exercise 1.20) Having a gain of more than 20 pounds represents all measurements greater than one standard deviation below the mean. By the empirical rule, the proportion above this value is approximately 84%, so the manufacturer is probably correct.

1.22 (See exercise 1.11)
$$\sum_{i=1}^{n} (y_i - \overline{y}) = \sum_{i=1}^{n} y_i - n\overline{y} = \sum_{i=1}^{n} y_i - \sum_{i=1}^{n} y_i = 0$$
.

- a. (Similar to exercise 1.20) 95 sec = 1 standard deviation above 75 sec, so this percentage is 16% by the empirical rule.
 b. (35 sec., 115 sec) represents an interval of 2 standard deviations about the mean, so approximately 95%
 c. 2 minutes = 120 sec = 2.5 standard deviations above the mean. This is unlikely.
- **1.24 a.** (112-78)/4 = 8.5



b. The histogram is above.

c. With
$$\sum_{i=1}^{20} y_i = 1874.0$$
 and $\sum_{i=1}^{20} y_i^2 = 117,328.0$, we have that $\overline{y} = 93.7$ and $s = 9.55$.

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d.

k	interval	frequency	Exp. frequency
1	84.1, 103.2	13	13.6
2	74.6, 112.8	20	19
3	65.0, 122.4	20	20

1.25 a. (716-8)/4 = 177 **b.** The figure is omitted.

c. With $\sum_{i=1}^{88} y_i = 18,550$ and $\sum_{i=1}^{88} y_i^2 = 6,198,356$, we have that $\overline{y} = 210.8$ and s = 162.17.

d.

k	interval	frequency	Exp. frequency
1	48.6, 373	63	59.84
2	-113.5, 535.1	82	83.6
3	-275.7, 697.3	87	88

- **1.26** For Ex. 1.12, 3/1.21 = 2.48. For Ex. 1.24, 34/9.55 = 3.56. For Ex. 1.25, 708/162.17 = 4.37. The ratio increases as the sample size increases.
- **1.27** (64, 80) is one standard deviation about the mean, so 68% of 340 or approx. 231 scores. (56, 88) is two standard deviations about the mean, so 95% of 340 or 323 scores.
- **1.28** (Similar to 1.23) 13 mg/L is one standard deviation below the mean, so 16%.
- **1.29** If the empirical rule is assumed, approximately 95% of all bearing should lie in (2.98, 3.02) this interval represents two standard deviations about the mean. So, approximately 5% will lie outside of this interval.
- **1.30** If $\mu = 0$ and $\sigma = 1.2$, we expect 34% to be between 0 and 0 + 1.2 = 1.2. Also, approximately 95%/2 = 47.5% will lie between 0 and 2.4. So, 47.5% 34% = 13.5% should lie between 1.2 and 2.4.
- **1.31** Assuming normality, approximately 95% will lie between 40 and 80 (the standard deviation is 10). The percent below 40 is approximately 2.5% which is relatively unlikely.
- **1.32** For a sample of size *n*, let *n'* denote the number of measurements that fall outside the interval $\overline{y} \pm ks$, so that (n n')/n is the fraction that falls inside the interval. To show this fraction is greater than or equal to $1 1/k^2$, note that

 $(n-1)s^{2} = \sum_{i \in A} (y_{i} - \overline{y})^{2} + \sum_{i \in b} (y_{i} - \overline{y})^{2}$, (both sums must be positive) where $A = \{i: |y_{i} - \overline{y}| \ge ks\}$ and $B = \{i: |y_{i} - \overline{y}| < ks\}$. We have that $\sum_{i \in A} (y_{i} - \overline{y})^{2} \ge \sum_{i \in A} k^{2}s^{2} = n'k^{2}s^{2}$, since if *i* is in *A*, $|y_{i} - \overline{y}| \ge ks$ and there are *n'* elements in *A*. Thus, we have that $s^{2} \ge k^{2}s^{2}n'/(n-1)$, or $1 \ge k^{2}n'/(n-1) \ge k^{2}n'/n$. Thus, $1/k^{2} \ge n'/n$ or $(n-n')/n \ge 1-1/k^{2}$.

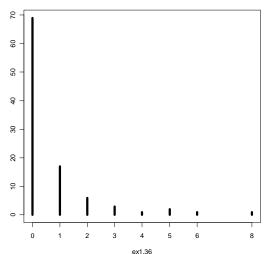
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- **1.33** With k = 2, at least 1 1/4 = 75% should lie within 2 standard deviations of the mean. The interval is (0.5, 10.5).
- **1.34** The point 13 is 13 5.5 = 7.5 units above the mean, or 7.5/2.5 = 3 standard deviations above the mean. By Tchebysheff's theorem, at least $1 1/3^2 = 8/9$ will lie within 3 standard deviations of the mean. Thus, at most 1/9 of the values will exceed 13.
- **1.35** a. (172 108)/4 = 16b. With $\sum_{i=1}^{15} y_i = 2041$ and $\sum_{i=1}^{15} y_i^2 = 281,807$ we have that $\overline{y} = 136.1$ and s = 17.1c. a = 136.1 - 2(17.1) = 101.9, b = 136.1 + 2(17.1) = 170.3. d. There are 14 observations contained in this interval, and 14/15 = 93.3%. 75% is a lower bound.



- **1.36 a.** The histogram is above. **b.** With $\sum_{i=1}^{100} y_i = 66$ and $\sum_{i=1}^{100} y_i^2 = 234$ we have that $\overline{y} = 0.66$ and s = 1.39. **c.** Within two standard deviations: 95, within three standard deviations: 96. The calculations agree with Tchebysheff's theorem.
- **1.37** Since the lead readings must be non negative, 0 (the smallest possible value) is only 0.33 standard deviations from the mean. This indicates that the distribution is skewed.
- **1.38** By Tchebysheff's theorem, at least 3/4 = 75% lie between (0, 140), at least 8/9 lie between (0, 193), and at least 15/16 lie between (0, 246). The lower bounds are all truncated a 0 since the measurement cannot be negative.