

Exam

Name \_\_\_\_\_

**SHORT ANSWER.** Write the word or phrase that best completes each statement or answers the question.

**Perform the indicated elementary row operation.**

1) \_\_\_\_\_

$$\begin{cases} x - 5y = 4 \\ 2x + 2y = 5 \end{cases} \xrightarrow{R_2 + (-2)R_1}$$

**MULTIPLE CHOICE.** Choose the one alternative that best completes the statement or answers the question.

2) Find the result of performing the elementary row operation  $R_3 + (5) R_2$  on the system  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 1 & -3 & 2 \\ 0 & -5 & 4 & 1 \end{bmatrix}$ . 2) \_\_\_\_\_

A)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 0 & -3 & 2 \\ 0 & -5 & 4 & 1 \end{bmatrix}$  B)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 1 & -3 & 2 \\ 0 & 0 & -11 & 11 \end{bmatrix}$  C)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & -5 & -11 & 11 \\ 0 & -5 & 4 & 1 \end{bmatrix}$  D)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 1 & -3 & 2 \\ 10 & 5 & 14 & 11 \end{bmatrix}$

3) Find the result of performing the elementary row operation  $R_2 + (-1) R_3$  on the system  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 1 & -3 & 2 \\ 0 & -5 & 4 & 1 \end{bmatrix}$ . 3) \_\_\_\_\_

A)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 6 & -7 & 1 \\ 0 & -5 & 4 & 1 \end{bmatrix}$  B)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 1 & -3 & 2 \\ 0 & -7 & 2 & 0 \end{bmatrix}$  C)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & -1 & -3 & 2 \\ 0 & -4 & -7 & 1 \end{bmatrix}$  D)  $\begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & -7 & 2 & 0 \\ 0 & -5 & 4 & 1 \end{bmatrix}$

4) The system  $\begin{bmatrix} 1 & 0 & 0 & -2 \\ 0 & 1 & 3 & 5 \\ 1 & 1 & -3 & 4 \end{bmatrix}$  is equivalent to the system 4) \_\_\_\_\_

A)  $\begin{bmatrix} 1 & 0 & 0 & -2 \\ 0 & 1 & -3 & 5 \\ 0 & 1 & -3 & 4 \end{bmatrix}$  B)  $\begin{bmatrix} 1 & 0 & 0 & -2 \\ 0 & 1 & 3 & 5 \\ 0 & 1 & -3 & 6 \end{bmatrix}$  C)  $\begin{bmatrix} 1 & 0 & 0 & -2 \\ 0 & 3 & -9 & 5 \\ 1 & 1 & -3 & 4 \end{bmatrix}$  D)  $\begin{bmatrix} 1 & 0 & 0 & -2 \\ 0 & 1 & -3 & 5 \\ 0 & 0 & 0 & 4 \end{bmatrix}$

5) The system  $\begin{bmatrix} 1 & 0 & 1 & -1 \\ 3 & 1 & 3 & 7 \\ 2 & 1 & 4 & 4 \end{bmatrix}$  is equivalent to the system 5) \_\_\_\_\_

A)  $\begin{bmatrix} 1 & 0 & 1 & -1 \\ 3 & 1 & 3 & 7 \\ 0 & 1 & 3 & 2 \end{bmatrix}$  B)  $\begin{bmatrix} 1 & 0 & 1 & -1 \\ 0 & 1 & 0 & 7 \\ 2 & 1 & 4 & 4 \end{bmatrix}$  C)  $\begin{bmatrix} 1 & 0 & 1 & -1 \\ 3 & 1 & 3 & 7 \\ 0 & 1 & 2 & 2 \end{bmatrix}$  D)  $\begin{bmatrix} 1 & 0 & 1 & -1 \\ 3 & 1 & 3 & 7 \\ 0 & -1 & 2 & 2 \end{bmatrix}$

Use the indicated row operation to change the matrix.

6) Replace  $R_2$  by  $R_1 + (-1)R_2$ .

6) \_\_\_\_\_

$$\left[ \begin{array}{cc|c} 1 & -3 & 4 \\ 2 & 3 & 1 \end{array} \right]$$

A)  $\left[ \begin{array}{cc|c} 1 & -1 & 2 \\ 2 & 3 & 1 \end{array} \right]$

B)  $\left[ \begin{array}{cc|c} 1 & -1 & 2 \\ 1 & 4 & -1 \end{array} \right]$

C)  $\left[ \begin{array}{cc|c} 1 & -1 & 2 \\ 3 & 2 & 3 \end{array} \right]$

D)  $\left[ \begin{array}{cc|c} 1 & -3 & 4 \\ -1 & -6 & 3 \end{array} \right]$

7) Replace  $R_2$  by  $\frac{1}{2}R_1 + \frac{1}{2}R_2$ .

7) \_\_\_\_\_

$$\left[ \begin{array}{cc|c} 2 & 0 & 2 \\ -2 & 2 & 10 \end{array} \right]$$

A)  $\left[ \begin{array}{cc|c} 2 & 0 & 2 \\ 0 & 1 & 6 \end{array} \right]$

B)  $\left[ \begin{array}{cc|c} 2 & 0 & 2 \\ 0 & 0 & 6 \end{array} \right]$

C)  $\left[ \begin{array}{cc|c} 2 & 0 & 2 \\ 0 & 2 & 12 \end{array} \right]$

D)  $\left[ \begin{array}{cc|c} 2 & 0 & 2 \\ -1 & 1 & 5 \end{array} \right]$

8) Replace  $R_2$  by  $\frac{1}{3}R_1 + \frac{1}{2}R_2$ .

8) \_\_\_\_\_

$$\left[ \begin{array}{cc|c} 3 & 0 & 9 \\ -2 & 4 & 8 \end{array} \right]$$

A)  $\left[ \begin{array}{cc|c} 3 & 0 & 9 \\ 0 & 0 & 7 \end{array} \right]$

B)  $\left[ \begin{array}{cc|c} 3 & 0 & 9 \\ 0 & 2 & 7 \end{array} \right]$

C)  $\left[ \begin{array}{cc|c} 3 & 0 & 9 \\ 1 & 4 & 17 \end{array} \right]$

D)  $\left[ \begin{array}{cc|c} 3 & 0 & 9 \\ -1 & 2 & 4 \end{array} \right]$

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

State the next elementary row operation that should be performed to put the matrix into diagonal form.

9)

9) \_\_\_\_\_

$$\left[ \begin{array}{ccc|c} 1 & 2 & -4 & 5 \\ 0 & 0 & 3 & 6 \\ 0 & 1 & 4 & 1 \end{array} \right]$$

State and perform the next elementary row operation that should be performed to put the matrix in diagonal form.

10)

10) \_\_\_\_\_

$$\left[ \begin{array}{ccc|c} 1 & 0 & 3 & 9 \\ 0 & 1 & -3 & 2 \\ 0 & -5 & 4 & 1 \end{array} \right]$$

11)

11) \_\_\_\_\_

$$\left[ \begin{array}{ccc|c} 1 & 0 & 0 & -3 \\ 0 & 1 & -2 & -2 \\ 0 & 0 & 1 & 1 \end{array} \right]$$

12)

12) \_\_\_\_\_

$$\left[ \begin{array}{ccc|c} 1 & 2 & -3 & 3 \\ 0 & -4 & 6 & 7 \\ 2 & 6 & 5 & -1 \end{array} \right]$$

13) Is  $x = 2$ ,  $y = -1$ ,  $z = 4$  a solution of the system of equations shown below? Explain your answer.

13) \_\_\_\_\_

$$\begin{cases} x - y + z = 7 \\ 2x - z = 0 \\ 2y + 3z = 9 \end{cases}$$

14) Is  $x = 2, y = -1, z = 4$  a solution of the system of equations shown below? Explain your answer. 14) \_\_\_\_\_

$$\begin{cases} x - y + z = 7 \\ 2x - z = 0 \\ 2y + 3z = 10 \end{cases}$$

15) When you solve a system of equations, what set of values are you looking for? 15) \_\_\_\_\_

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

**Use the Gauss-Jordan method to solve the system of equations.**

16) 16) \_\_\_\_\_

$$\begin{cases} 2x + 3y = 7 \\ 3x - 2y = -22 \end{cases}$$

- A)  $x = -4, y = 5$       B)  $x = 5, y = -4$       C)  $x = -4, y = -5$       D) No solution

17) 17) \_\_\_\_\_

$$\begin{cases} 4x + 3y = 7 \\ 5x = -10 \end{cases}$$

- A)  $x = -2, y = -5$       B)  $x = 5, y = -2$       C)  $x = -2, y = 5$       D) No solution

18) 18) \_\_\_\_\_

$$\begin{cases} 5x + y = 15 \\ 6x + 4y = 4 \end{cases}$$

- A)  $x = -5, y = -4$       B)  $x = -5, y = 4$       C)  $x = 4, y = -5$       D) No solution

19) 19) \_\_\_\_\_

$$\begin{cases} x + y + z = 6 \\ x - y + 2z = -2 \\ 2x + y + z = 11 \end{cases}$$

- A)  $x = -2, y = 5, z = 3$       B)  $x = 5, y = 3, z = -2$   
C)  $x = -2, y = 3, z = 5$       D) No solution

20) 20) \_\_\_\_\_

$$\begin{cases} x - y + 5z = 11 \\ 5x + z = 3 \\ x + 3y + z = 15 \end{cases}$$

- A)  $x = 3, y = 0, z = 4$       B)  $x = 0, y = 4, z = 3$   
C)  $x = 3, y = 4, z = 0$       D) No solution

21) 21) \_\_\_\_\_

$$\begin{cases} x - y + z = 3 \\ x + y + z = -1 \\ x + y - z = -11 \end{cases}$$

- A)  $x = 5, y = -4, z = -2$       B)  $x = -4, y = -2, z = 5$   
C)  $x = -4, y = 5, z = -2$       D) No solution

22)

22) \_\_\_\_\_

$$\begin{cases} 5x - y + 5z = 11 \\ -6x - 8z = -26 \\ 3y + z = 28 \end{cases}$$

A)  $x = 3, y = 9, z = 1$

C)  $x = -3, y = 9, z = 6$

B)  $x = 3, y = 1, z = 9$

D) No solution

Fill in the missing numbers in the next step of the Gauss-Jordan elimination method.

23)

23) \_\_\_\_\_

$$\left[ \begin{array}{ccc|c} 1 & 8 & 4 & 5 \\ 3 & 1 & -2 & 6 \\ -2 & -4 & 5 & 0 \end{array} \right] \rightarrow \left[ \begin{array}{ccc|c} 1 & 8 & 4 & 5 \\ 0 & -23 & \square & \square \\ 0 & 12 & \square & \square \end{array} \right]$$

A)

$$\left[ \begin{array}{ccc|c} 1 & 8 & 4 & 5 \\ 0 & -23 & -6 & 1 \\ 0 & 12 & 1 & 9 \end{array} \right]$$

B)

$$\left[ \begin{array}{ccc|c} 1 & 8 & 4 & 5 \\ 0 & -23 & -13 & -7 \\ 0 & 12 & 12 & 11 \end{array} \right]$$

C)

$$\left[ \begin{array}{ccc|c} 1 & 8 & 4 & 5 \\ 0 & -23 & -16 & -10 \\ 0 & 12 & 16 & 10 \end{array} \right]$$

D)

$$\left[ \begin{array}{ccc|c} 1 & 8 & 4 & 5 \\ 0 & -23 & -14 & -9 \\ 0 & 12 & 13 & 10 \end{array} \right]$$

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Solve the problem.**

- 24) The sales division of a company purchased type A cell phones for \$95 each and type B cell phones for \$110 each. It purchased a total of 18 cell phones at a total cost of \$1815. How many type A cell phones did the division purchase? 24) \_\_\_\_\_

- 25) A marketing company wishes to conduct a \$15,000,000 advertising campaign in three media—radio, television, and newspaper. The company wants to spend twice as much money in television advertising as in radio and newspaper advertising combined. Also, the company wants to spend a total of \$13,000,000 in radio and television combined. Let  $x$ ,  $y$  and  $z$  represent the amount in millions of dollars spent in radio, television, and newspaper respectively. How much should the company spend in each medium? (Express the problem in terms of a system of linear equations and solve it using Gaussian elimination.) 25) \_\_\_\_\_

- 26) At a certain party, 72 people are invited. Only half of those invited come. Of those who come, twice as many are women as are men. How many men and how many women come? Let  $x$  be the number of women and  $y$  be the number of men. 26) \_\_\_\_\_

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

- 27) A waiter made a deposit of \$191. If his deposit consisted of 83 bills, some of them one-dollar bills and the rest five-dollar bills, how many one-dollar bills did he deposit? 27) \_\_\_\_\_  
 A) 46 one-dollar bills B) 56 one-dollar bills  
 C) 51 one-dollar bills D) 27 one-dollar bills

- 28) At a local zoo, adult visitors must pay \$3 and children pay \$1. On one day, the zoo collected a total of \$850. If the zoo had 470 visitors that day, how many adults and how many children visited? 28) \_\_\_\_\_  
 A) 212 adults and 258 children B) 280 adults and 190 children  
 C) 140 adults and 330 children D) 190 adults and 280 children

- 29) The annual salaries of a software engineer and a project supervisor total \$188,900. If the project supervisor makes \$14,900 more than the software engineer, find each of their salaries. 29) \_\_\_\_\_
- A) software engineer: \$72,100  
project supervisor: \$87,000  
C) software engineer: \$87,000  
project supervisor: \$101,900
- B) software engineer: \$72,100  
project supervisor: \$116,800  
D) software engineer: \$101,900  
project supervisor: \$116,800
- 30) A particular computer takes 66 nanoseconds (ns) to carry out 2 sums and 8 products, and 57 nanoseconds to perform 3 sums and 6 products. How long does the computer take to carry out one sum and one product? 30) \_\_\_\_\_
- A) one sum: 5 ns  
one product: 9 ns  
C) one sum: 5 ns  
one product: 7 ns
- B) one sum: 7 ns  
one product: 9 ns  
D) one sum: 7 ns  
one product: 5 ns
- 31) Barges from ports X and Y went to cities A and B. X sent 32 barges and Y sent 8. City A received 21 barges and B received 19. Shipping costs \$220 from X to A, \$300 from X to B, \$400 from Y to A, and \$180 from Y to B. \$9360 was spent. How many barges went where? 31) \_\_\_\_\_
- A) 17 from X to A, 17 from X to B, 4 from Y to A, and 4 from Y to B  
B) 16 from X to A, 16 from X to B, 6 from Y to A, and 2 from Y to B  
C) 21 from X to A, 11 from X to B, 0 from Y to A, and 8 from Y to B  
D) 19 from X to A, 13 from X to B, 2 from Y to A, and 6 from Y to B
- 32) Factories A and B sent rice to stores 1 and 2. A sent 13 loads and B sent 23. Store 1 received 19 loads and store 2 received 17. It cost \$200 to ship from A to 1, \$350 from A to 2, \$300 from B to 1, and \$250 from B to 2. \$8650 was spent. How many loads went where? 32) \_\_\_\_\_
- A) 11 from A to 1, 2 from A to 2, 8 from B to 1, and 15 from B to 2  
B) 13 from A to 1, 0 from A to 2, 6 from B to 1, and 17 from B to 2  
C) 0 from A to 1, 13 from A to 2, 17 from B to 1, and 6 from B to 2  
D) 12 from A to 1, 1 from A to 2, 7 from B to 1, and 4 from B to 2
- 33) Pivot the matrix  $\begin{bmatrix} 1 & 3 & 5 \\ 5 & 6 & 2 \end{bmatrix}$  about the element 6. 33) \_\_\_\_\_
- A)  $\begin{bmatrix} 1 & 3 & 5 \\ \frac{5}{6} & 1 & \frac{1}{3} \end{bmatrix}$
- B)  $\begin{bmatrix} 1 & 2 & -\frac{8}{3} \\ 0 & 1 & \frac{23}{9} \end{bmatrix}$
- C)  $\begin{bmatrix} -\frac{3}{2} & 0 & 4 \\ \frac{5}{6} & 1 & \frac{1}{3} \end{bmatrix}$
- D)  $\begin{bmatrix} 1 & 3 & 5 \\ 3 & 0 & -8 \end{bmatrix}$

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

- 34) Pivot the matrix  $\begin{bmatrix} 1 & 3 \\ 4 & -2 \end{bmatrix}$  about the element 3. 34) \_\_\_\_\_
- 35) Pivot the matrix  $\begin{bmatrix} 1 & 2 & 4 \\ 0 & \underline{1} & 2 \\ 0 & -5 & 3 \end{bmatrix}$  about the underlined element 1. 35) \_\_\_\_\_

36) Pivot the matrix  $\begin{bmatrix} 3 & 2 & -2 \\ 1 & \frac{1}{2} & -\frac{3}{2} \\ 0 & -1 & 9 \end{bmatrix}$  about the element  $\frac{1}{2}$ . 36) \_\_\_\_\_

**Solve the system of linear equations using the Gaussian elimination method. If there is no solution, state so; if there are infinitely many solutions, find two of them.**

37) 
$$\begin{cases} x - y + 2z = 2 \\ y - 2z = 1 \\ -3x + 5y - 10z = -4 \end{cases}$$
 37) \_\_\_\_\_

38) 
$$\begin{cases} x - 3y - 5z = 1 \\ -3x + 7y + 9z = 1 \\ x + 4z = -5 \end{cases}$$
 38) \_\_\_\_\_

39) 
$$\begin{cases} x - y - 2z = 2 \\ y - 2z = 1 \\ -3x + 5y - 10z = -4 \end{cases}$$
 39) \_\_\_\_\_

**Solve the linear system by using the Gauss-Jordan elimination method.**

40) 
$$\begin{cases} 3x + 6y = -6 \\ -2x - 7y = 1 \end{cases}$$
 40) \_\_\_\_\_

41) 
$$\begin{cases} x - 3y - 5z = 1 \\ -3x + 7y + 9z = 1 \\ x + 4z = -5 \end{cases}$$
 41) \_\_\_\_\_

**For the system of equations, state whether there is one, none, or infinitely many solutions. If there are one or more solutions, give all values of x, y, and z that satisfy the system.**

42) 
$$\begin{cases} x - y + 3z = 0 \\ z = 7 \end{cases}$$
 42) \_\_\_\_\_

43) 
$$\begin{cases} x + 3y + 2z = 4 \\ y - 3z = -1 \\ z = 17 \end{cases}$$
 43) \_\_\_\_\_

44) 
$$\begin{cases} x + y - z = 1 \\ y - 2z = 1 \\ x + y - z = 2 \end{cases}$$
 44) \_\_\_\_\_

- 45) When solving a system of linear equations with the unknowns  $x$ ,  $y$ , and  $z$  using the Gauss-Jordan elimination method, the following matrix was obtained. What can be concluded about the solution of the system?

$$\left[ \begin{array}{ccc|c} 1 & 0 & 0 & 4 \\ 0 & 1 & 1 & 3 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

45) \_\_\_\_\_

- 46) When solving a system of linear equations with the unknowns  $x$ ,  $y$ , and  $z$  using the Gauss-Jordan elimination method, the following matrix was obtained. What can be concluded about the general solution of the system?

$$\left[ \begin{array}{ccc|c} 1 & 0 & 2 & 4 \\ 0 & 1 & 1 & 3 \end{array} \right]$$

46) \_\_\_\_\_

- 47) When solving a system of linear equations with the unknowns  $x$ ,  $y$ , and  $z$  using the Gauss-Jordan elimination method, the following matrix was obtained. What can be concluded about the solution of the system?

$$\left[ \begin{array}{ccc|c} 1 & 0 & 0 & 4 \\ 0 & 1 & -1 & 3 \\ 0 & 0 & 0 & 2 \end{array} \right]$$

47) \_\_\_\_\_

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

- 48) Consider the system:  $\begin{cases} x - y = 7 \\ 2x - 2y = k \end{cases}$ . Which of the following statements is true?

48) \_\_\_\_\_

- A) If  $k = 14$ , the system has infinitely many solutions.
- B) If  $k \neq 14$ , the system has exactly one solution.
- C) If  $k = 14$ , the system has no solution.
- D) none of these

- 49) Consider the system:  $\begin{cases} x - y = 7 \\ 2x - 2y = k \end{cases}$ . Which of the following statements is true?

49) \_\_\_\_\_

- A) If  $k = 10$ , the system has infinitely many solutions.
- B) If  $k = 10$ , the system has no solution.
- C) If  $k \neq 10$ , the system has exactly one solution.
- D) none of these

- 50) Which of the following systems have infinitely many solutions?

50) \_\_\_\_\_

I.  $\begin{cases} x - 2y + 5z = 7 \\ y - 2z = 4 \end{cases}$

II.  $\begin{cases} x - y + 4z + 3w = 2 \\ z + 2w = 8 \\ w = 3 \end{cases}$

III.  $\begin{cases} x + y - z = 1 \\ y - 2z = 1 \\ 3y - 6z = 4 \end{cases}$

IV.  $\begin{cases} x + 2y - z = 2 \\ x - z = 3 \\ 2x - 2z = 6 \end{cases}$

- A) I, II, and III only
- B) I and II only
- C) III and IV only
- D) I, II, and IV only
- E) all of these

51) Which of the following systems has no solution?

51) \_\_\_\_\_

A)

$$\begin{cases} 2x + 4y = 10 \\ 3x + 6y = 15 \end{cases}$$

B)

$$\begin{cases} 2x + 4y = 10 \\ 3x + 6y = 20 \end{cases}$$

C)

$$\begin{cases} 2x + 4y = 10 \\ 4x + 8y = 20 \end{cases}$$

D)

$$\begin{cases} 2x + 4y = 10 \\ 2x + 6y = 10 \end{cases}$$

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

52) Suppose the line L has equation  $2x + 3y = 5$  and the line M has equation  $x + 4y = -5$ . Use Gauss-Jordan elimination method to determine whether L and M intersect in one point, are distinct but parallel, or coincide.

52) \_\_\_\_\_

53) Suppose line L has equation  $3x + 2y = 7$  and line H has equation  $9x + Ky = 14$ . Find the value for K so that L and M are parallel.

53) \_\_\_\_\_

54) If possible, find the general solution of the following system.

54) \_\_\_\_\_

$$\begin{cases} x + y + z = 1 \\ x + y + 2z = -1 \\ 2x + 2y + 3z = 0 \end{cases}$$

55) Find three solutions to  $\begin{cases} 8x + 2y - z = 7 \\ y = 2 \end{cases}$ .

55) \_\_\_\_\_

56) Find a value for K so that the following system of equations

56) \_\_\_\_\_

$$\begin{cases} 6x + 3y = 15 \\ Kx + y = 5 \end{cases} \text{ has infinitely many solutions.}$$

57) Find a value for K so that the following system of equations

57) \_\_\_\_\_

$$\begin{cases} 6x + 3y = 15 \\ Kx + y = 5 \end{cases} \text{ has exactly one solution.}$$

58) Find a specific solution to a system of linear equations whose general solution is

58) \_\_\_\_\_

$$\begin{aligned} y &= \text{any value} \\ w &= \text{any value} \\ x &= 3 - 6y \\ z &= 2 \end{aligned}$$

59) Find a specific solution to a system of linear equations whose general solution is

59) \_\_\_\_\_

$$\begin{aligned} y &= \text{any value} \\ w &= 2x - z \\ x &= 3 - 6y \\ z &= 2 \end{aligned}$$

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

60) The two lines  $-2x + y = 3$  and  $-3x + y = 2$

60) \_\_\_\_\_

- A) coincide.
- B) are parallel.
- C) intersect in exactly one point.
- D) are perpendicular.
- E) none of these



- 61) The two lines  $x + 5y = 3$  and  $5x - y = 6$   
 A) are parallel.  
 B) intersect in exactly one point.  
 C) are perpendicular.  
 D) coincide.  
 E) none of these

61) \_\_\_\_\_

Use the Gauss-Jordan method to solve the system of equations.

62)  $2x - 7y = -2$   
 $8x - 28y = 4$

62) \_\_\_\_\_

A) (4, 4)

B) (-2, 4)

C)  $\left(-1 + \frac{7}{2}y, y\right)$

D) No solution

63)  $-3x - 6y = 9$   
 $-12x - 24y = 36$

63) \_\_\_\_\_

A)  $(-3 - 2y, y)$

B) (1, -2)

C)  $(-3 + 2y, y)$

D) No solution

64)  $-4x - 3y = -5$   
 $8x + 6y = 8$

64) \_\_\_\_\_

A)  $\left(\frac{3}{5}x + \frac{4}{5}y, y\right)$

B) (-2, -2)

C) (-5, 8)

D) No solution

A matrix,  $A$ , corresponding to a system of linear equations and the matrix  $\text{rref}(A)$  obtained after the Gauss-Jordan elimination method is applied to  $A$ , are given. Write the system of linear equations corresponding to  $A$ , and use  $\text{rref}(A)$  to give all solutions of the system of linear equations.

65)  $A = \left[ \begin{array}{ccc|c} 1 & 6 & -7 & 13 \\ -3 & -14 & 13 & -35 \end{array} \right]; \text{rref}(A) = \left[ \begin{array}{ccc|c} 1 & 0 & 5 & 7 \\ 0 & 1 & -2 & 1 \end{array} \right]$

65) \_\_\_\_\_

A)

$$\begin{cases} x + 6y - 7z = 7 \\ -3x - 14y + 13z = 1 \end{cases}$$

$z = \text{any value}, y = 1 - 2z, x = 7 + 5z$

B)

$$\begin{cases} x + 6y - 7z = 7 \\ -3x - 14y + 13z = 1 \end{cases}$$

$z = \text{any value}, y = -2, x = 5$

C)

$$\begin{cases} x + 6y - 7z = 13 \\ -3x - 14y + 13z = -35 \end{cases}$$

$z = \text{any value}, y = 1 + 2z, x = 7 - 5z$

D)

$$\begin{cases} x + 5z = 7 \\ y - 2z = 1 \end{cases}$$

$z = \text{any value}, y = 1 + 2z, x = 7 - 5z$

$$66) A = \left[ \begin{array}{ccc|c} 1 & 3 & 10 & 12 \\ -2 & -5 & -16 & -19 \\ 2 & 5 & 16 & 19 \end{array} \right]; \text{ rref}(A) = \left[ \begin{array}{ccc|c} 1 & 0 & -2 & -3 \\ 0 & 1 & 4 & 5 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

66) \_\_\_\_\_

A)

$$\begin{cases} x - 2z = -3 \\ y + 4z = 5 \end{cases}$$

$z = \text{any value}, y = 5 - 4z, x = -3 + 2z$

B)

$$\begin{cases} x + 3y + 10z = 12 \\ -2x - 5y - 16z = -19 \\ 2x + 5y + 16z = 19 \end{cases}$$

$z = \text{any value}, y = 5 - 4z, x = -3 + 2z$

C)

$$\begin{cases} x + 3y + 10z = 12 \\ -2x - 5y - 16z = -19 \\ 2x + 5y + 16z = 19 \end{cases}$$

$z = 0, y = 5, x = -3$

D)

$$\begin{cases} x + 3y + 10z = -3 \\ -2x - 5y - 16z = 5 \\ 2x + 5y + 16z = 0 \end{cases}$$

$z = \text{any value}, y = 5 + 4z, x = 3 - 2z$

### Solve the problem.

- 67) Janet is planning to visit Arizona, New Mexico, and California on a 26-day vacation. If she plans to spend as much time in New Mexico as she does in the other two states combined, how can she allot her time in the three states? (Let  $x$  denote the number of days in Arizona,  $y$  the number of days in New Mexico, and  $z$  the number of days in California. Let  $z$  be the parameter.) 67) \_\_\_\_\_

- A)  $x = 13 - z, y = 13, 0 \leq z \leq 13$   
 B)  $x = 13, y = 13 - z, 0 \leq z \leq 13$   
 C)  $x = 13, y = z - 13, 0 \leq z \leq 13$   
 D)  $x = z - 13, y = 13, 0 \leq z \leq 13$

- 68) A company is introducing a new soft drink and is planning to have 48 advertisements distributed among TV ads, radio ads, and newspaper ads. If the cost of TV ads is \$500 each, the cost of radio ads is \$200 each, and the cost of newspaper ads is \$200 each, how can the ads be distributed among the three types if the company has \$13,800 to spend for advertising? (Let  $x$  denote the number of TV ads,  $y$  the number of radio ads, and  $z$  the number of newspaper ads. Let  $z$  be the parameter.) 68) \_\_\_\_\_

- A)  $x = 34 - z, y = 14, 0 \leq z \leq 34$   
 B)  $x = 14, y = z - 34, 0 \leq z \leq 34$   
 C)  $x = z - 34, y = 14, 0 \leq z \leq 34$   
 D)  $x = 14, y = 34 - z, 0 \leq z \leq 34$

- 69) An investor has \$300,000 to invest in stocks, bonds, and commodities. If he plans to put three times as much into stocks as in bonds, how can he distribute his money among the three types of investments? (Let  $x$  denote the amount put into stocks,  $y$  the amount put into bonds, and  $z$  the amount put into commodities. Let all amounts be in dollars, and let  $z$  be the parameter.) 69) \_\_\_\_\_

- A)  $x = 75,000 - 3z/4, y = 225,000 - z/4, 0 \leq z \leq 300,000$   
 B)  $x = 75,000 - z/2, y = 225,000 - z/2, 0 \leq z \leq 300,000$   
 C)  $x = 225,000 - 3z/4, y = 75,000 - z/4, 0 \leq z \leq 300,000$   
 D)  $x = 225,000 - z/2, y = 75,000 - z/2, 0 \leq z \leq 300,000$

- 70) A company has 144 sales representatives, each to be assigned to one of four marketing teams. If the first team is to have three times as many members as the second team and the third team is to have twice as many members as the fourth team, how can the members be distributed among the teams? (Let  $x$  denote the number of members assigned to the first team,  $y$  the number assigned to the second team,  $z$  the number assigned to the third team, and  $w$  the number assigned to the fourth team. Let  $w$  be the parameter.) 70) \_\_\_\_\_

- A)  $x = 144 - 3w, y = 48 - w, z = 3w - 48, 0 \leq w \leq 48$   
 B)  $x = 36 - 3w/4, y = 12 - w/4, z = 2w, 0 \leq w \leq 24$   
 C)  $x = 72 - 3w, y = 24 - w, z = 48 + 3w, 0 \leq w \leq 24$   
 D)  $x = 108 - 9w/4, y = 36 - 3w/4, z = 2w, 0 \leq w \leq 48$

- 71) A school library has \$24,000 to spend on new books among the four categories of biology, chemistry, physics, and mathematics. If the amount spent on biology books is to be the same as the amount spent on chemistry books and if the amount spent on mathematics books is to be the same as the total spent on chemistry and physics books, how can the money be distributed among the four types of books? (Let  $x$  denote the amount spent on biology books,  $y$  the amount spent on chemistry books,  $z$  the amount spent on physics books, and  $w$  the amount spent on mathematics books. Let all amounts be in dollars, and let  $w$  be the parameter.) 71) \_\_\_\_\_
- A)  $x = 24,000 - 2w$ ,  $y = 24,000 - 2w$ ,  $z = 3w - 24,000$ ,  $8000 \leq w \leq 12,000$   
 B)  $x = 24,000 - w$ ,  $y = 24,000 - w$ ,  $z = 2w - 24,000$ ,  $4000 \leq w \leq 8000$   
 C)  $x = 24,000 + w$ ,  $y = 24,000 + w$ ,  $z = w - 24,000$ ,  $4000 \leq w \leq 12,000$   
 D)  $x = 24,000 - 3w$ ,  $y = 24,000 - 3w$ ,  $z = 4w - 24,000$ ,  $8000 \leq w \leq 16,000$
- 72) A recording company is to release 120 new CDs in the categories of rock, country, jazz, and classical. If twice the number of rock CDs is to equal three times the number of country CDs and if the number of jazz CDs is to equal the number of classical CDs, how can the CDs be distributed among the four types? (Let  $x$  be the number of rock CDs,  $y$  the number of country CDs,  $z$  the number of jazz CDs, and  $w$  the number of classical CDs. Let  $w$  be the parameter.) 72) \_\_\_\_\_
- A)  $x = 60 - 3w/5$ ,  $y = 40 - 2w/5$ ,  $z = w$ ,  $0 \leq w \leq 52$   
 B)  $x = 60 - 2w$ ,  $y = 60 - 2w/5$ ,  $z = w$ ,  $0 \leq w \leq 60$   
 C)  $x = 72 - w$ ,  $y = 32 - w$ ,  $z = w$ ,  $0 \leq w \leq 40$   
 D)  $x = 72 - 6w/5$ ,  $y = 48 - 4w/5$ ,  $z = w$ ,  $0 \leq w \leq 60$
- 73) A politician is planning to spend a total of 36 hours on a campaign swing through the southern states of Arkansas, Louisiana, Mississippi, Alabama, and Georgia. Assume that he spends the same amount of time in Mississippi as in Alabama; half the amount of time in Georgia as in Arkansas; and the same amount of time in Mississippi, Alabama, and Georgia (combined) as in Arkansas and Louisiana (combined). How can he distribute his time among the five states? (Let  $a$  be the hours spent in Arkansas,  $b$  the hours spent in Louisiana,  $c$  the hours spent in Mississippi,  $d$  the hours spent in Alabama, and  $e$  the hours spent in Georgia. Let  $e$  be the parameter.) 73) \_\_\_\_\_
- A)  $a = 2e$ ,  $b = 18 - e$ ,  $c = 9 - e/2$ ,  $d = 9 - e/2$ ,  $0 \leq e \leq 9$   
 B)  $a = e$ ,  $b = 18 - e/2$ ,  $c = 9 - e/4$ ,  $d = 9 - e/4$ ,  $0 \leq e \leq 18$   
 C)  $a = 2e$ ,  $b = 18 - e$ ,  $c = 9 - e$ ,  $d = 9 - e$ ,  $0 \leq e \leq 18$   
 D)  $a = 2e$ ,  $b = 18 - 2e$ ,  $c = 9 - e/2$ ,  $d = 9 - e/2$ ,  $0 \leq e \leq 9$
- 74) Which of the following calculations can be performed? 74) \_\_\_\_\_
- I.  $\begin{bmatrix} 4 & 0 & 2 \end{bmatrix} + \begin{bmatrix} 1 \\ 3 \\ 5 \end{bmatrix}$     II.  $\begin{bmatrix} 6 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$     III.  $\begin{bmatrix} 5 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$     IV.  $\begin{bmatrix} 2 & 1 & 2 \\ 4 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix}$
- A) III and IV only  
 B) IV only  
 C) I and II only  
 D) III only  
 E) all of these
- 75) What is the identity matrix of size 3? 75) \_\_\_\_\_
- A)  $\begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$     B)  $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$     C)  $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$     D)  $\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$

76) If B is a  $1 \times 6$  matrix and A is a  $6 \times 1$  matrix, determine the size of AB.

76) \_\_\_\_\_

- A)  $6 \times 1$
- B)  $1 \times 1$
- C)  $1 \times 6$
- D)  $6 \times 6$
- E) none of these

77) If B is a  $4 \times 2$  matrix and A is a  $3 \times 4$  matrix, determine the size of AB.

77) \_\_\_\_\_

- A)  $3 \times 4$
- B)  $2 \times 3$
- C)  $3 \times 2$
- D)  $4 \times 4$
- E) none of these

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Determine the values of x and y, if any, that make  $A = B$ .**

78)  $A = \begin{bmatrix} 5 & 3 & -2 \\ x & 4 & 0 \end{bmatrix}$  and  $B = \begin{bmatrix} 5 & y & -2 \\ 8 & 4 & 0 \end{bmatrix}$  78) \_\_\_\_\_

79)  $A = \begin{bmatrix} x & 1 \\ 2 & 3 \\ 4 & y \end{bmatrix}$  and  $B = \begin{bmatrix} 5 & 2 & 4 \\ 1 & 3 & -2 \end{bmatrix}$  79) \_\_\_\_\_

80) In each case below, give an example of a matrix that meets the specified condition.

80) \_\_\_\_\_

- (a) A and B so that AB is not defined
- (b) a  $2 \times 2$  matrix that has no inverse
- (c) C and D so that CD is defined but DC is not defined

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

**Provide an appropriate response.**

81) Which choice best describes the following matrix?

81) \_\_\_\_\_

$$\begin{bmatrix} 23 \\ 27 \\ 20 \\ 17 \\ 18 \end{bmatrix}$$

- A) Row matrix      B)  $1 \times 5$  matrix      C) Square matrix      D) Column matrix

**Answer the question about the  $2 \times 3$  matrix A.**

82) Find  $a_{12}$  and  $a_{23}$ .

82) \_\_\_\_\_

$$A = \begin{bmatrix} -4 & 8 & 1 \\ -6 & 0 & 7 \end{bmatrix}$$

- A) 8, 7      B) -6, 7      C) 8, -4      D) -6, 1

83) For what values of i and j does  $a_{ij} = 9$ ?

83) \_\_\_\_\_

$$A = \begin{bmatrix} -4 & 9 & 2 \\ -1 & 0 & 6 \end{bmatrix}$$

- A)  $i = 1, j = 2$       B)  $i = 1, j = 1$       C)  $i = 2, j = 1$       D)  $i = 2, j = 2$

84) 
$$\begin{bmatrix} -5 & -5 \\ -4 & -9 \\ -1 & -8 \end{bmatrix} + \begin{bmatrix} -2 & -2 \\ -7 & 5 \\ 3 & -5 \end{bmatrix} =$$

A) 
$$\begin{bmatrix} -7 & -7 \\ -11 & -4 \\ 2 & -13 \end{bmatrix}$$
 B) 
$$\begin{bmatrix} -7 & -7 \\ 11 & -9 \\ 2 & 13 \end{bmatrix}$$
 C) 
$$\begin{bmatrix} -3 & -3 \\ 3 & -14 \\ -4 & -2 \end{bmatrix}$$
 D) 
$$\begin{bmatrix} -7 & -9 \\ -11 & -4 \\ 2 & -13 \end{bmatrix}$$

84) \_\_\_\_\_

85) 
$$\begin{bmatrix} -1 & 0 \\ 6 & 3 \end{bmatrix} - \begin{bmatrix} -1 & 6 \\ 3 & 1 \end{bmatrix} =$$

A) 
$$\begin{bmatrix} 0 & -6 \\ 3 & 2 \end{bmatrix}$$
 B) 
$$\begin{bmatrix} -2 & 6 \\ 9 & 4 \end{bmatrix}$$
 C) 
$$[-1]$$
 D) 
$$\begin{bmatrix} 0 & 6 \\ -3 & -2 \end{bmatrix}$$

85) \_\_\_\_\_

**Perform the indicated operation, where possible.**

86) 
$$\begin{bmatrix} -7 & 1 \\ 2 & 5 \end{bmatrix} + \begin{bmatrix} 6 & 2 \\ 4 & 1 \end{bmatrix}$$

A) 
$$\begin{bmatrix} 3 & 4 \\ 2 & 6 \end{bmatrix}$$
 B) 
$$\begin{bmatrix} -1 & -5 \\ -3 & -6 \end{bmatrix}$$
 C) 
$$\begin{bmatrix} -1 & 3 \\ 6 & 6 \end{bmatrix}$$
 D) Not possible

86) \_\_\_\_\_

87) 
$$\begin{bmatrix} 6 & 4 \end{bmatrix} + \begin{bmatrix} -2 \\ 9 \end{bmatrix}$$

A) 
$$\begin{bmatrix} 6 & -2 \\ 4 & 9 \end{bmatrix}$$
 B) 
$$\begin{bmatrix} 4 \\ 13 \end{bmatrix}$$
 C) 
$$\begin{bmatrix} 4 & 13 \end{bmatrix}$$
 D) Not possible

87) \_\_\_\_\_

88) 
$$\begin{bmatrix} -5 & 9 & 1 \end{bmatrix} - \begin{bmatrix} 4 & 3 \end{bmatrix}$$

A) 
$$\begin{bmatrix} -9 & 6 & 1 \end{bmatrix}$$
 B) 
$$\begin{bmatrix} -9 & 9 & -2 \end{bmatrix}$$
 C) 
$$\begin{bmatrix} -9 & 6 & -2 \end{bmatrix}$$
 D) Not possible

88) \_\_\_\_\_

89) 
$$\begin{bmatrix} 3 \\ -3 \\ -4 \end{bmatrix} + \begin{bmatrix} -5 \\ 4 \\ 7 \end{bmatrix}$$

A) 
$$\begin{bmatrix} 2 \\ 3 \\ 4 \end{bmatrix}$$
 B) 
$$\begin{bmatrix} 3 & -5 \\ -3 & 4 \\ -4 & 7 \end{bmatrix}$$
 C) 
$$\begin{bmatrix} -2 & 1 & 3 \end{bmatrix}$$
 D) 
$$\begin{bmatrix} -2 \\ 1 \\ 3 \end{bmatrix}$$

89) \_\_\_\_\_

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Let A, B, and C be the following matrices:**

$$A = \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix} \quad B = \begin{bmatrix} 2 & 0 & -2 \\ 0 & 2 & 3 \end{bmatrix} \quad C = \begin{bmatrix} -2 & 3 & 1 \\ 5 & 6 & -3 \end{bmatrix}$$

**State whether or not each of the following calculations is possible. If possible, perform the calculation.**

90)  $A + B$  90) \_\_\_\_\_

91)  $B - C$  91) \_\_\_\_\_

92)  $2A - B$  92) \_\_\_\_\_

93)  $2C + B$

93) \_\_\_\_\_

**State whether the calculation is possible. If possible, perform the calculation.**

94)

$$\begin{bmatrix} 4 & 2 \\ -3 & 1 \end{bmatrix} + \begin{bmatrix} 1 & -1 \\ \frac{1}{2} & 0 \end{bmatrix} - \begin{bmatrix} 6 & 6 \\ 1 & 2 \end{bmatrix}$$

94) \_\_\_\_\_

95)

$$\begin{bmatrix} 3 \\ 30 \\ 17 \end{bmatrix} + \begin{bmatrix} 14 \\ 0 \\ 8 \end{bmatrix}$$

95) \_\_\_\_\_

96)

$$[6] + \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

96) \_\_\_\_\_

97)

$$\begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix} + [4 \quad 0 \quad 6]$$

97) \_\_\_\_\_

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

98)  $[4 \quad 0 \quad 6] \begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix} =$

98) \_\_\_\_\_

A)

$$\begin{bmatrix} 4 & 0 & 6 \\ 12 & 0 & 18 \\ -8 & 0 & -12 \end{bmatrix}$$

B)

$$\begin{bmatrix} 4 & 12 & -8 \\ 0 & 0 & 0 \\ 6 & 18 & -12 \end{bmatrix}$$

C)

$$\begin{bmatrix} 4 \\ 0 \\ -12 \end{bmatrix}$$

D)

$$[4 \quad 0 \quad -12]$$

E)

$$[-8]$$

99)  $\begin{bmatrix} 1 \\ 3 \\ -2 \end{bmatrix} [4 \ 0 \ 6] =$

99) \_\_\_\_\_

A)

$$\begin{bmatrix} 4 & 0 & 6 \\ 12 & 0 & 18 \\ -8 & 0 & -12 \end{bmatrix}$$

B)

$$\begin{bmatrix} 4 \\ 0 \\ -12 \end{bmatrix}$$

C)

$$[-8]$$

D)

$$[4 \ 0 \ -12]$$

E)

$$\begin{bmatrix} 4 & 12 & -8 \\ 0 & 0 & 0 \\ 6 & 18 & -12 \end{bmatrix}$$

100) Let  $A = \begin{bmatrix} -2 & 1 & 3 \\ 1 & 0 & 5 \\ 0 & 4 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & 1 & -3 \\ 1 & 3 & -4 \\ 3 & 0 & 1 \end{bmatrix}$ . Find the second row of  $AB$ .

100) \_\_\_\_\_

A)  $[15 \ -1 \ 2]$

B)  $[18 \ -1 \ 2]$

C)  $[18 \ 1 \ 2]$

D)  $[15 \ 1 \ 2]$

E) none of these

101) Let  $A = \begin{bmatrix} 3 & 2 & 7 \\ 1 & 0 & 3 \\ 1 & 4 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 5 & 2 \\ 7 & 1 & 3 \end{bmatrix}$ . Find the third row of  $AB$ .

101) \_\_\_\_\_

A)  $[25 \ 18 \ 58]$

B)  $[18 \ 23 \ 16]$

C)  $[7 \ 4 \ 6]$

D)  $[31 \ 11 \ 16]$

E) none of these

102) Let  $A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$  and  $B = \begin{bmatrix} 3 & -2 \\ 4 & 6 \end{bmatrix}$ . Find the entry in the second row, first column of  $AB$ .

102) \_\_\_\_\_

A) 18

B) 22

C) 8

D) 34

E) 6

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**State whether the calculation is possible. If possible, perform the calculation.**

103) \_\_\_\_\_

$$\begin{bmatrix} 2 & 1 & 0 \\ 3 & 0 & 2 \end{bmatrix} \begin{bmatrix} 7 & -1 \\ 1 & 0 \\ 5 & 2 \end{bmatrix}$$

104) \_\_\_\_\_

$$\begin{bmatrix} 1 \\ 2 \\ -5 \end{bmatrix} [4 \ 0 \ 3]$$

105) \_\_\_\_\_

$$\begin{bmatrix} 3 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} 2 & 7 \\ 6 & 4 \\ 1 & 6 \end{bmatrix}$$

106) \_\_\_\_\_

$$\begin{bmatrix} 1 & 0 & -2 \\ 2 & 4 & 3 \end{bmatrix} \begin{bmatrix} 2 & 1 & -1 \\ 5 & 0 & 1 \end{bmatrix}$$

107) \_\_\_\_\_

$$\begin{bmatrix} 2 & 1 & 3 \\ 4 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$$

108) If  $A = \begin{bmatrix} 6 & -2 \\ -2 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} \frac{1}{2} & 1 \\ 1 & 3 \end{bmatrix}$ , find  $AB$  and  $BA$ . \_\_\_\_\_

109) If  $A = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix}$ , does  $AB = BA$ ? Explain. \_\_\_\_\_

110) Find  $a$  and  $b$  so that  $\begin{bmatrix} 1 & 6 & -3 \\ 7 & 7 & 4 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a & b & 0 \\ 2 & 6 & 1 \\ 4 & 2 & 2 \end{bmatrix} = \begin{bmatrix} -4 & 28 & 0 \\ 2 & 36 & 15 \\ 4 & 2 & 2 \end{bmatrix}$  \_\_\_\_\_

111) If  $A^4 = \begin{bmatrix} -3 & 4 \\ -4 & 5 \end{bmatrix}$  and  $A^5 = \begin{bmatrix} 4 & -5 \\ 5 & -6 \end{bmatrix}$ , what is  $A$ ? \_\_\_\_\_

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

**The sizes of two matrices  $A$  and  $B$  are given. Find the sizes of the product  $AB$  and the product  $BA$ , whenever these products exist.**

112)  $A$  is  $2 \times 2$ , and  $B$  is  $2 \times 2$ . \_\_\_\_\_

A)  $2 \times 4$ ;  $2 \times 4$       B)  $1 \times 1$ ;  $1 \times 1$       C)  $4 \times 2$ ;  $4 \times 2$       D)  $2 \times 2$ ;  $2 \times 2$



113) A is  $1 \times 3$ , and B is  $3 \times 1$ .

- A) AB does not exist;  $3 \times 3$   
C)  $1 \times 1$ ; BA does not exist.

- B)  $3 \times 3$ ;  $1 \times 1$   
D)  $1 \times 1$ ;  $3 \times 3$

113) \_\_\_\_\_

114) A is  $2 \times 1$ , and B is  $2 \times 1$ .

- A) AB does not exist; BA does not exist.  
C)  $2 \times 2$ ;  $1 \times 1$

- B)  $2 \times 1$ ;  $1 \times 2$   
D)  $1 \times 2$ ;  $2 \times 1$

114) \_\_\_\_\_

**Find the matrix product, if possible.**

115)  $\begin{bmatrix} -2 & 3 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} -2 & 0 \\ -1 & 3 \end{bmatrix}$

A)  $\begin{bmatrix} 9 & 1 \\ 6 & -6 \end{bmatrix}$

B)  $\begin{bmatrix} 4 & -6 \\ -2 & 3 \end{bmatrix}$

C)  $\begin{bmatrix} 4 & 0 \\ -2 & 6 \end{bmatrix}$

D)  $\begin{bmatrix} 1 & 9 \\ -6 & 6 \end{bmatrix}$

115) \_\_\_\_\_

116)  $\begin{bmatrix} -1 & 3 \\ 5 & 4 \end{bmatrix} \begin{bmatrix} 0 & -2 & 5 \\ 1 & -3 & 2 \end{bmatrix}$

A)  $\begin{bmatrix} 3 & 4 & -7 \\ -22 & 1 & 33 \end{bmatrix}$

B)  $\begin{bmatrix} 3 & -7 & 1 \\ 4 & -22 & 33 \end{bmatrix}$

C)  $\begin{bmatrix} 0 & -6 \\ 15 & 5 \\ -12 & 8 \end{bmatrix}$

D) Does not exist

116) \_\_\_\_\_

117)  $\begin{bmatrix} 3 & -2 & 1 \\ 0 & 4 & -3 \end{bmatrix} \begin{bmatrix} 5 & 0 \\ -2 & 3 \end{bmatrix}$

A)  $\begin{bmatrix} 15 & -10 & 5 \\ -6 & 16 & -11 \end{bmatrix}$

B)  $\begin{bmatrix} 15 & 0 \\ 0 & 12 \end{bmatrix}$

C)  $\begin{bmatrix} 15 & -6 \\ -10 & 16 \\ 5 & -11 \end{bmatrix}$

D) Does not exist

117) \_\_\_\_\_

118)  $\begin{bmatrix} 1 & 3 & -2 \\ 4 & 0 & 5 \end{bmatrix} \begin{bmatrix} 3 & 0 \\ -2 & 1 \\ 0 & 5 \end{bmatrix}$

A)  $\begin{bmatrix} -3 & -7 \\ 12 & 25 \end{bmatrix}$

B)  $\begin{bmatrix} 3 & -6 & 0 \\ 0 & 0 & 25 \end{bmatrix}$

C)  $\begin{bmatrix} -7 & -3 \\ 25 & 12 \end{bmatrix}$

D) Does not exist

118) \_\_\_\_\_

119) Find the system of equations that is equivalent to the matrix equation,  $\begin{bmatrix} -2 & 5 \\ 1 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 6 \end{bmatrix}$ .

A)  $\begin{cases} -2x + 5y = 3 \\ y + 4y = 6 \end{cases}$

B)  $\begin{cases} -2x + 5y = 3 \\ x + 4y = 6 \end{cases}$

C)  $\begin{cases} -2x + y = 3 \\ 5y + 4y = 6 \end{cases}$

D)  $\begin{cases} -2x + y = 3 \\ 5x + 4y = 6 \end{cases}$

119) \_\_\_\_\_

120) Find the matrix equation that is equivalent to the system of equations,  $\begin{cases} x - 2y + z = 4 \\ 3x + y + z = 1 \\ x + y + 2z = 0 \end{cases}$ . 120) \_\_\_\_\_

A)  $\begin{bmatrix} 1 & -2 & 1 \\ 3 & 1 & 1 \\ 1 & 1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 0 \end{bmatrix}$ .

B)  $\begin{bmatrix} x \\ y \\ z \end{bmatrix} \begin{bmatrix} 1 & -2 & 1 \\ 3 & 1 & 1 \\ 1 & 1 & 2 \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 0 \end{bmatrix}$ .

C)  $\begin{bmatrix} 1 & 3 & 1 \\ -2 & 1 & 1 \\ 1 & 1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 0 \end{bmatrix}$ .

D)  $\begin{bmatrix} x \\ y \\ z \end{bmatrix} \begin{bmatrix} 1 & 3 & 1 \\ -2 & 1 & 1 \\ 1 & 1 & 2 \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 0 \end{bmatrix}$ .

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

121) Write the system of linear equations as a matrix equation. 121) \_\_\_\_\_  
 $\begin{cases} x + 3y = 6 \\ 2x - y = 3 \end{cases}$

122) Write the system of linear equations as a matrix equation. 122) \_\_\_\_\_  
 $\begin{cases} x + 2y + 3z = 4 \\ 6y + 7z = 8 \\ x = 5 \end{cases}$

123) Write the system of linear equations as a matrix equation. 123) \_\_\_\_\_  
 $\begin{cases} x + y + 4z = 3 \\ 4x + y - 2z = -6 \\ -3x + 2z = 1 \end{cases}$

124) Give the system of linear equations that is equivalent to the matrix equation: 124) \_\_\_\_\_  
 $\begin{bmatrix} 3 & 1 & 2 \\ -1 & 0 & 2 \\ 0 & 4 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ -1 \end{bmatrix}$

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

**Write the matrix equation as a system of linear equations without matrices.**

125) 125) \_\_\_\_\_  
 $\begin{bmatrix} 2 & 0 \\ 1 & 1 \\ 2 & -5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -8 \\ 6 \\ 2 \end{bmatrix}$

A)  $2x_1 + x_2 = -8$   
 $x_1 + 6x_2 = 6$   
 $2x_1 - 5x_2 = 2$

B)  $2x_1 + x_2 + x_3 = -8$   
 $x_1 - 5x_2 = 6$

C)  $2x_1 = -8$   
 $x_1 + x_2 = 6$   
 $2x_1 - 5x_2 = 2$

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Solve the problem.**

- 126) In a certain state legislature the percentage of legislators voting for or against lowering the legal drinking age by various party affiliations is summarized by this matrix. 126) \_\_\_\_\_

$$\begin{array}{c} \text{For} \quad \text{Against} \\ \text{Democrat} \\ \text{Republican} \\ \text{Independent} \end{array} \begin{bmatrix} 0.6 & 0.4 \\ 0.3 & 0.7 \\ 1 & 0 \end{bmatrix} = A$$

There are 60 Democratic, 30 Republicans, and 10 Independents in the legislature. Use a matrix calculation to determine how many legislators voted for lowering the drinking age and how many voted against lowering the drinking age.

- 127) A company has three factories I, II, and III. Each factory employs both skilled and unskilled worker. The break down of the number of workers by type in the three factories is summarized by matrix A below. The hourly wage of the skilled worker is \$15 and that of the unskilled worker is \$10. Multiply appropriate matrices and compute the total hourly pay at each factory. 127) \_\_\_\_\_

$$A = \begin{array}{c} \text{skilled} \\ \text{unskilled} \end{array} \begin{array}{ccc} \text{I} & \text{II} & \text{III} \\ \begin{bmatrix} 25 & 34 & 24 \\ 42 & 53 & 62 \end{bmatrix} \end{array}$$

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

- 128) Suppose one hour's output (measured in bottles) in a brewery is described by the following matrix: 128) \_\_\_\_\_

$$\begin{array}{c} \text{Production line 1} \quad \text{Production line 2} \\ \text{Regular Beer} \\ \text{Light Beer} \\ \text{Malt Beer} \end{array} \begin{bmatrix} 300 & 200 \\ 400 & 100 \\ 100 & 50 \end{bmatrix} = A$$

Let  $H = \begin{bmatrix} x \\ y \end{bmatrix}$  where x represents the number of hours Production line 1 is in operation in a day and y represents the number of hours Production line 2 is in operation in a day. Then the entry in the second row, first column of AH, represents

- A) the total number of bottles of regular beer produced in a day.
- B) the total number of bottles of light beer produced in a day.
- C) the total number of hours in a day spent producing light beer.
- D) the total number of hours in a day spent producing regular beer.
- E) none of these

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

- 129) Two hundred students are registered in a certain mathematics course. Experience suggests that if  $x$  and  $y$  represent the number of students who earn a grade of C or better on Exam I and the number of students who earn a grade of D or F on Exam I, respectively, and if  $p$  and  $n$  represent the number of students who earn a grade of C or better on Exam II and the number of students who earn a grade of D or F on Exam II, respectively, then \_\_\_\_\_
- $$0.9x + 0.3y = p$$
- $$0.1x + 0.7y = n$$
- (a) Write the system of equations in matrix form.
- (b) Solve the resulting matrix equation for  $X = \begin{bmatrix} x \\ y \end{bmatrix}$ .
- (c) Suppose 120 students earn a grade of C or better on Exam II. How many students earned a grade of D or F on Exam I?

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

- 130) Barnes and Able sell life, health, and auto insurance. Their sales, in dollars, for May and June are given in the following matrices. \_\_\_\_\_

$$\text{May: } \begin{array}{ccccc} & \text{Life} & \text{Health} & \text{Auto} & \\ \begin{bmatrix} 20,000 & 15,000 & 6,000 \\ 30,000 & 0 & 17,000 \end{bmatrix} & \text{Able} & & & \\ & & & & \text{Barnes} \end{array}$$

$$\text{June: } \begin{array}{ccccc} & \text{Life} & \text{Health} & \text{Auto} & \\ \begin{bmatrix} 70,000 & 0 & 30,000 \\ 20,000 & 21,000 & 32,000 \end{bmatrix} & \text{Able} & & & \\ & & & & \text{Barnes} \end{array}$$

Find a matrix that gives total sales, in dollars, of each type of insurance by each salesman for the two-month period.

- A)  $\begin{bmatrix} 140,000 & 21,000 & 49,000 \end{bmatrix}$
- B)  $\begin{bmatrix} 90,000 & 15,000 & 36,000 \\ 50,000 & 21,000 & 49,000 \end{bmatrix}$
- C)  $\begin{bmatrix} 90,000 & 0 & 36,000 \\ 50,000 & 0 & 49,000 \end{bmatrix}$
- D)  $\begin{bmatrix} 90,000 & 15,000 & 36,000 \\ 50,000 & 21,000 & 32,000 \end{bmatrix}$

- 131) The matrices give points and rebounds for five starting players in two games. Find the matrix that gives the totals. 131) \_\_\_\_\_

$$F = \begin{array}{c} \text{Points} \quad \text{Rebounds} \\ \left[ \begin{array}{cc} 19 & 3 \\ 16 & 5 \\ 8 & 12 \\ 6 & 11 \\ 10 & 2 \end{array} \right] \end{array}$$

$$S = \begin{array}{c} \text{Points} \quad \text{Rebounds} \\ \left[ \begin{array}{cc} 18 & 4 \\ 14 & 3 \\ 12 & 9 \\ 4 & 10 \\ 10 & 3 \end{array} \right] \end{array}$$

A)

$$\left[ \begin{array}{cc} 37 & 7 \\ 30 & 8 \\ 20 & 21 \\ 10 & 21 \\ 20 & 5 \end{array} \right]$$

B)

$$\left[ \begin{array}{cc} 62 & 5 \end{array} \right]$$

C)

$$\left[ \begin{array}{cc} 7 & 37 \\ 30 & 8 \\ 21 & 20 \\ 21 & 10 \\ 5 & 20 \end{array} \right]$$

D)

$$\left[ \begin{array}{cc} 5 & 62 \end{array} \right]$$

- 132) Find the inverse of the matrix  $\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ . 132) \_\_\_\_\_

A)

$$\left[ \begin{array}{cc} \frac{1}{2} & -\frac{3}{2} \\ -1 & 2 \end{array} \right]$$

B)

$$\left[ \begin{array}{cc} 1 & \frac{1}{2} \\ \frac{1}{3} & \frac{1}{4} \end{array} \right]$$

C) not defined

D)

$$\left[ \begin{array}{cc} -2 & 1 \\ \frac{3}{2} & -\frac{1}{2} \end{array} \right]$$

E) none of these

133) Find the inverse of the matrix  $\begin{bmatrix} 1 & -1 \\ -3 & 4 \end{bmatrix}$ .

133) \_\_\_\_\_

A) not defined

B)

$$\begin{bmatrix} 4 & 1 \\ -3 & 1 \end{bmatrix}$$

C)

$$\begin{bmatrix} 4 & 1 \\ 3 & 1 \end{bmatrix}$$

D)

$$\begin{bmatrix} 4 & -1 \\ -3 & 1 \end{bmatrix}$$

E) none of these

134) The matrix  $\begin{bmatrix} 3 & x \\ 4 & 36 \end{bmatrix}$  has no inverse if x is

134) \_\_\_\_\_

A) 0.

B) 3.

C)  $\frac{1}{3}$ .

D) 27.

E) 48.

135) The matrix  $\begin{bmatrix} 3 & 12 \\ x & 36 \end{bmatrix}$  has no inverse if x is

135) \_\_\_\_\_

A) 3.

B) 12.

C) 48.

D) 9.

E) 27.

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Find the inverse of the matrix, if it exists.**

136)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

136) \_\_\_\_\_

137)  $\begin{bmatrix} 3 & 1 \\ 6 & 2 \end{bmatrix}$

137) \_\_\_\_\_

138)  $\begin{bmatrix} 2 & -1 \\ -6 & 8 \end{bmatrix}$

138) \_\_\_\_\_

139)  $\begin{bmatrix} 0.6 & 0.1 \\ 0.4 & 0.9 \end{bmatrix}$

139) \_\_\_\_\_

140)  $\begin{bmatrix} 3 & 2 \\ 0 & 1 \end{bmatrix}$

140) \_\_\_\_\_

141)  $\begin{bmatrix} 3 & 1 \\ 0 & 0 \end{bmatrix}$

141) \_\_\_\_\_

142) [6]

142) \_\_\_\_\_

143) [0.4]

143) \_\_\_\_\_

144) Two  $n \times n$  matrices A and B are called inverses of each other if both products AB and BA equal  $I_n$ . Are the following matrices inverses of each other? 144) \_\_\_\_\_

$$A = \begin{bmatrix} 7 & 4 \\ 5 & 3 \end{bmatrix}, B = \begin{bmatrix} 3 & -4 \\ -5 & 7 \end{bmatrix}$$

145) Are the following matrices inverses of each other? 145) \_\_\_\_\_

$$A = \begin{bmatrix} 1 & 4 \\ 8 & 3 \end{bmatrix}, B = \begin{bmatrix} -1 & 8 \\ 3 & -2 \end{bmatrix}$$

146) Given that  $\begin{bmatrix} 2 & -2 & -1 \\ -5 & 3 & 4 \\ -6 & 5 & 4 \end{bmatrix}$  and  $\begin{bmatrix} 8 & -3 & 5 \\ 4 & -2 & 3 \\ 7 & -2 & 4 \end{bmatrix}$  are inverses of each other, 146) \_\_\_\_\_

$$\text{find A so that } (A - I)^{-1} = \begin{bmatrix} 8 & -3 & 5 \\ 4 & -2 & 3 \\ 7 & -2 & 4 \end{bmatrix}.$$

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

147) 147) \_\_\_\_\_

$$\text{Let } A = \begin{bmatrix} 1 & 2 & 0 \\ 3 & 1 & 0 \\ 0 & 0 & 2 \end{bmatrix} \text{ and } B = \begin{bmatrix} x & y & 0 \\ \frac{3}{5} & -\frac{1}{5} & 0 \\ 0 & 0 & \frac{1}{2} \end{bmatrix}$$

In order for A and B to be inverses, x and y must be

A)  $x = -\frac{1}{5}, y = \frac{2}{5}$ .

B)  $x = 1, y = \frac{1}{2}$ .

C)  $x = -5, y = \frac{5}{3}$ .

D)  $x = 1, y = 0$ .

E) none of these

148) 148) \_\_\_\_\_

$$\text{Let } A = \begin{bmatrix} -4 & 1 & 2 \\ 7 & -1 & -4 \\ -\frac{1}{2} & 0 & \frac{1}{2} \end{bmatrix} \text{ and } B = \begin{bmatrix} x & y & 4 \\ 3 & 2 & 4 \\ 1 & 1 & 6 \end{bmatrix}$$

In order for A and B to be inverses, x and y must be

A)  $x = 1, y = -1$ .

B)  $x = -1, y = -1$ .

C)  $x = -1, y = 1$ .

D)  $x = 1, y = 1$ .

E) none of these

Find the inverse, if it exists, for the matrix.

149)  $\begin{bmatrix} -2 & 4 \\ 4 & -4 \end{bmatrix}$

149) \_\_\_\_\_

A)

$$\begin{bmatrix} \frac{1}{2} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{4} \end{bmatrix}$$

B)

$$\begin{bmatrix} \frac{1}{4} & \frac{1}{2} \\ \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

C)

$$\begin{bmatrix} \frac{1}{2} & -\frac{1}{2} \\ -\frac{1}{2} & \frac{1}{4} \end{bmatrix}$$

D)

$$\begin{bmatrix} \frac{1}{2} & \frac{1}{4} \\ \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

150)  $\begin{bmatrix} 0 & -2 \\ -4 & -5 \end{bmatrix}$

150) \_\_\_\_\_

A)

$$\begin{bmatrix} -\frac{1}{2} & 0 \\ \frac{5}{8} & -\frac{1}{4} \end{bmatrix}$$

B)

$$\begin{bmatrix} 0 & -\frac{1}{4} \\ -\frac{1}{2} & \frac{5}{8} \end{bmatrix}$$

C)

$$\begin{bmatrix} \frac{5}{8} & \frac{1}{4} \\ \frac{1}{2} & 0 \end{bmatrix}$$

D)

$$\begin{bmatrix} \frac{5}{8} & -\frac{1}{4} \\ -\frac{1}{2} & 0 \end{bmatrix}$$

151)  $\begin{bmatrix} -3 & -6 \\ -7 & -7 \end{bmatrix}$

151) \_\_\_\_\_

A)

$$\begin{bmatrix} -7 & 6 \\ 7 & -3 \end{bmatrix}$$

B)

$$\begin{bmatrix} \frac{7}{31} & \frac{6}{31} \\ \frac{7}{31} & \frac{3}{31} \end{bmatrix}$$

C)

$$\begin{bmatrix} \frac{7}{31} & -\frac{6}{31} \\ -\frac{7}{31} & \frac{3}{31} \end{bmatrix}$$

D) No inverse

152)  $\begin{bmatrix} 6 & 6 \\ 0 & 4 \end{bmatrix}$

152) \_\_\_\_\_

A)

$$\begin{bmatrix} 0 & \frac{1}{4} \\ \frac{1}{6} & -\frac{1}{4} \end{bmatrix}$$

B)

$$\begin{bmatrix} \frac{1}{6} & -\frac{1}{4} \\ 0 & \frac{1}{4} \end{bmatrix}$$

C)

$$\begin{bmatrix} \frac{1}{6} & \frac{1}{4} \\ 0 & \frac{1}{4} \end{bmatrix}$$

D)

$$\begin{bmatrix} \frac{1}{4} & -\frac{1}{4} \\ 0 & \frac{1}{6} \end{bmatrix}$$

153) Given that the matrices  $A = \begin{bmatrix} 1 & 2 & 2 \\ 1 & 3 & 2 \\ 1 & 2 & 3 \end{bmatrix}$  and  $B = \begin{bmatrix} 5 & -2 & -2 \\ -1 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix}$  are inverses of each other, find the

153) \_\_\_\_\_

solution  $\begin{bmatrix} x \\ y \\ z \end{bmatrix}$  of the system  $\begin{cases} -5x - 2y - 2z = 1 \\ -x + y = 2 \\ -x + z = -3 \end{cases}$ .

A)

$$\begin{bmatrix} 5 & -2 & -2 \\ -1 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix}.$$

B)

$$\begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix} \begin{bmatrix} 5 & -2 & -2 \\ -1 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix}.$$

C)

$$\begin{bmatrix} 1 & 2 & 2 \\ 1 & 3 & 2 \\ 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix}.$$

D)

$$\begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix} \begin{bmatrix} 1 & 2 & 2 \\ 1 & 3 & 2 \\ 1 & 2 & 3 \end{bmatrix}.$$



**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

154) Solve the system  $\begin{cases} x + y = 2 \\ 2x + y = -1 \end{cases}$  by using the inverse of an appropriate matrix. 154) \_\_\_\_\_

155) The matrices  $\begin{bmatrix} 5 & -2 & -2 \\ -1 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix}$  and  $\begin{bmatrix} 1 & 2 & 2 \\ 1 & 3 & 2 \\ 1 & 2 & 3 \end{bmatrix}$  are inverses of each other. 155) \_\_\_\_\_

Use this fact to solve the system  $\begin{cases} x + 2y + 2z = 1 \\ x + 3y + 2z = -1 \\ x + 2y + 3z = -1 \end{cases}$ .

156) The matrices  $\begin{bmatrix} 5 & 2 & -2 \\ 2 & 1 & -1 \\ -3 & -1 & 2 \end{bmatrix}$  and  $\begin{bmatrix} 1 & -2 & 0 \\ -1 & 4 & 1 \\ 1 & -1 & 1 \end{bmatrix}$  are inverses of each other. 156) \_\_\_\_\_

Use this fact to solve the system  $\begin{cases} x - 2y = 5 \\ -x + 4y + z = 1 \\ x - y + z = 2 \end{cases}$ .

157) Use the fact that 157) \_\_\_\_\_

$$\begin{bmatrix} 3 & 0 & -6 & 0 \\ 1 & 1 & 1 & 4 \\ 0 & 2 & 1 & 6 \\ 1 & 0 & 0 & 2 \end{bmatrix}^{-1} = \begin{bmatrix} \frac{1}{9} & \frac{4}{3} & -\frac{2}{3} & -\frac{2}{3} \\ \frac{2}{9} & \frac{5}{3} & -\frac{1}{3} & -\frac{7}{3} \\ -\frac{1}{9} & \frac{2}{3} & -\frac{1}{3} & -\frac{1}{3} \\ -\frac{1}{18} & -\frac{2}{3} & \frac{1}{3} & \frac{5}{6} \end{bmatrix}$$

to solve the system

$$\begin{cases} 3x - 6z = 0 \\ x + y + z + 4w = 2 \\ 2y + z + 6w = 1 \\ x + 2w = 0 \end{cases}$$

158) Consider the system  $\begin{cases} 3x + 2y = 7 \\ y = 8 \end{cases}$  158) \_\_\_\_\_

- Rewrite it in the form  $AX = B$ , where A, B, and X are appropriate matrices.
- Find the inverse of A.
- Solve the system by computing  $A^{-1}B$ .

159) Consider the system  $\begin{cases} 2x + 3y = 4 \\ -2x - y = 8 \end{cases}$  159) \_\_\_\_\_

- Rewrite it in the form  $AX = B$ , where A, B, and X are appropriate matrices.
- Find the inverse of A.
- Solve the system by computing  $A^{-1}B$ .

- 160) Consider the system  $\begin{cases} 0.7x + 0.2y = 3 \\ 0.3x + 0.8y = 2 \end{cases}$  160) \_\_\_\_\_
- (a) Rewrite it in the form  $AX = B$  where, A, B, and X are appropriate matrices.
- (b) Find the inverse of A.
- (c) Solve the system by computing  $A^{-1}B$ .
- 161) (a) Find the inverse of the matrix  $\begin{bmatrix} 2 & 1 \\ 3 & 1 \end{bmatrix}$ . 161) \_\_\_\_\_
- (b) Use the result from (a) to solve the system  $\begin{cases} 2x + y = 2 \\ 3x + y = -1 \end{cases}$ .
- 162) Find the  $2 \times 2$  matrix C such that  $AC = B$ , where  $A = \begin{bmatrix} 3 & 2 \\ 7 & 5 \end{bmatrix}$  and  $B = \begin{bmatrix} 4 & 1 \\ 2 & -3 \end{bmatrix}$ . 162) \_\_\_\_\_
- 163) Find the  $3 \times 3$  matrix C such that  $AC = B$ , where  $A = \begin{bmatrix} 1 & 1 & 0 \\ 0 & -1 & 0 \\ 3 & 0 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$ . 163) \_\_\_\_\_
- 164) Solve the equation  $AX = B$ , where  $A = \begin{bmatrix} 13 & -5 \\ -5 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$ . 164) \_\_\_\_\_
- 165) Let A and B be  $n \times n$  invertible matrices and C be an  $n \times 1$  column vector. 165) \_\_\_\_\_
- Solve  $AX + BY = C$  for X.

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

**Solve the system of equations by using the inverse of the coefficient matrix if it exists and by the echelon method if the inverse doesn't exist.**

- 166)  $2x - 6y = -6$  166) \_\_\_\_\_  
 $3x + 2y = 13$   
 A)  $x = 2, y = 3$       B)  $x = -3, y = -2$       C)  $x = -2, y = -3$       D)  $x = 3, y = 2$
- 167)  $6x + 5y = 1$  167) \_\_\_\_\_  
 $3x + 5y = 13$   
 A)  $x = -4, y = 5$       B)  $x = 5, y = -4$   
 C) No inverse, no solution for system      D)  $x = -4, y = -5$
- 168)  $6x + y = 32$  168) \_\_\_\_\_  
 $4x + 2y = 16$   
 A)  $x = 6, y = -4$       B)  $x = -4, y = -6$   
 C)  $x = -4, y = 6$       D) No inverse, no solution for system

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

**Solve the problem.**

- 169) A charitable organization estimates that 60% of the people in a certain area who make a contribution in one year will also contribute the next year, and that 10% of those who do not contribute one year will contribute the next. Let  $x$  and  $y$  denote the number of people who contribute in one year respectively, and let  $u$  and  $v$  be the corresponding numbers for the following year. 169) \_\_\_\_\_
- (a) Write a matrix equation relating  $\begin{bmatrix} x \\ y \end{bmatrix}$  to  $\begin{bmatrix} u \\ v \end{bmatrix}$ .
- (b) Solve the equation for  $\begin{bmatrix} x \\ y \end{bmatrix}$ .
- (c) Suppose that out of 10,000 people, 1500 made a contribution this year. How many made a contribution last year?

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

- 170) A bakery sells three types of cakes, each requiring the amount of ingredients shown. 170) \_\_\_\_\_

	Cake I	Cake II	Cake III
flour (cups)	2	4	2
sugar (cups)	2	1	2
eggs	2	1	3

To fill its orders for these cakes, the bakery used 72 cups of flour, 48 cups of sugar, and 55 eggs. How many cakes of each type were made?

- A) 37 cake I, 8 cake II, 12 cake III  
 B) 15 cake I, 8 cake II, 7 cake III  
 C) 7 cake I, 8 cake II, 13 cake III  
 D) 13 cake I, 8 cake II, 7 cake III

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

- 171) Use the Gauss–Jordan method to compute the inverse of the matrix  $\begin{bmatrix} 3 & 1 \\ 2 & 1 \end{bmatrix}$ . 171) \_\_\_\_\_
- 172) Use the Gauss–Jordan method to find the inverse of the matrix  $A$ , where  $A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 2 \\ 4 & 5 & 5 \end{bmatrix}$ . 172) \_\_\_\_\_
- 173) Use the Gauss–Jordan method to compute the inverse of the matrix, if it exists.  $\begin{bmatrix} -1 & 2 \\ -3 & 7 \end{bmatrix}$  173) \_\_\_\_\_
- 174) Use the Gauss–Jordan method to explain why the matrix  $\begin{bmatrix} 1 & 2 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix}$  has no inverse. 174) \_\_\_\_\_
- 175) Use the Gauss–Jordan method to compute  $\begin{bmatrix} -1 & 2 & -4 \\ 1 & -1 & 3 \\ 0 & 0 & 1 \end{bmatrix}^{-1}$ . 175) \_\_\_\_\_

176) Use the Gauss-Jordan method to compute the inverse of the matrix, if it exists.

176) \_\_\_\_\_

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}$$

177) Use the Gauss-Jordan method to compute the inverse of the matrix, if it exists.

177) \_\_\_\_\_

$$\begin{bmatrix} 2 & 6 & 0 \\ -1 & -3 & 0 \\ 7 & 7 & 1 \end{bmatrix}$$

178) If  $A^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ -2 & 0 & 1 \\ 3 & 1 & 5 \end{bmatrix}$ , find A.

178) \_\_\_\_\_

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

**Find the inverse, if it exists, of the given matrix.**

179)  $A = \begin{bmatrix} 5 & -6 & 0 & 4 \\ 15 & -12 & 0 & 8 \\ 6 & -24 & 0 & 12 \\ 0 & 0 & -3 & 0 \end{bmatrix}$

179) \_\_\_\_\_

A)

$$\begin{bmatrix} \frac{1}{5} & -\frac{1}{6} & 0 & \frac{1}{4} \\ \frac{1}{15} & -\frac{1}{12} & 0 & \frac{1}{8} \\ \frac{1}{6} & -\frac{1}{24} & 0 & \frac{1}{12} \\ 0 & 0 & -\frac{1}{3} & 0 \end{bmatrix}$$

C)

$$\begin{bmatrix} -\frac{2}{5} & \frac{11}{10} & 0 & \frac{12}{5} \\ \frac{1}{5} & -\frac{3}{10} & 0 & -\frac{7}{10} \\ 0 & -\frac{1}{6} & 0 & -\frac{1}{4} \\ 0 & 0 & -\frac{1}{3} & 0 \end{bmatrix}$$

B)

$$\begin{bmatrix} -\frac{2}{5} & \frac{1}{5} & 0 & 0 \\ \frac{11}{10} & -\frac{3}{10} & -\frac{1}{6} & 0 \\ 0 & 0 & 0 & -\frac{1}{3} \\ \frac{12}{5} & -\frac{7}{10} & -\frac{1}{4} & 0 \end{bmatrix}$$

D) No inverse

180)  $A = \begin{bmatrix} 0 & 5 & 5 \\ -5 & 0 & 5 \\ 0 & 7 & 0 \end{bmatrix}$

180) \_\_\_\_\_

A)

$$\begin{bmatrix} \frac{1}{5} & 0 & \frac{1}{5} \\ -\frac{1}{5} & 0 & 0 \\ -\frac{1}{7} & \frac{1}{7} & -\frac{1}{7} \end{bmatrix}$$

C) Does not exist

B)

$$\begin{bmatrix} -\frac{1}{5} & -\frac{1}{5} & -\frac{1}{7} \\ -\frac{1}{7} & 0 & \frac{1}{7} \\ \frac{1}{5} & 0 & 0 \end{bmatrix}$$

D)

$$\begin{bmatrix} \frac{1}{5} & -\frac{1}{5} & -\frac{1}{7} \\ 0 & 0 & \frac{1}{7} \\ \frac{1}{5} & 0 & -\frac{1}{7} \end{bmatrix}$$

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

181) Use matrix inversion to solve the system of linear equations.

181) \_\_\_\_\_

$$\begin{cases} 5x + 2y - 2z = 5 \\ 2x + y - z = 1 \\ -3x - y + 2z = 2 \end{cases}$$

182) Use matrix inversion to solve the system of linear equations.

182) \_\_\_\_\_

$$\begin{cases} x + y + 3z = 10 \\ 2x + y - z = 0 \\ -x - y + 2z = 5 \end{cases}$$

183) Use matrix inversion to solve the system of linear equations.

183) \_\_\_\_\_

$$\begin{cases} x + y + z = 6 \\ x - y + z = 3 \\ x - y - z = 0 \end{cases}$$

184) (a) Using the Gauss-Jordan method, find the inverse of the matrix  $\begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & -4 \\ 0 & 0 & 2 \end{bmatrix}$ .

184) \_\_\_\_\_

(b) Based on your answer to (a), solve the system  $\begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & -4 \\ 0 & 0 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$ .

185) (a) Using the Gauss-Jordan method, find the inverse of the matrix  $\begin{bmatrix} -2 & 2 & -1 \\ 3 & -5 & 4 \\ 5 & -6 & 4 \end{bmatrix}$ .

185) \_\_\_\_\_

(b) Based on your answer to (a), solve the system  $\begin{bmatrix} -2 & 2 & -1 \\ 3 & -5 & 4 \\ 5 & -6 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 3 \end{bmatrix}$ .

186) (a) Using the Gauss-Jordan method, find the inverse of the matrix  $\begin{bmatrix} 1 & 0 & 1 \\ 2 & 1 & 0 \\ 0 & 1 & -1 \end{bmatrix}$ . 186) \_\_\_\_\_

(b) Based on your answer to (a), solve the following system.

$$\begin{cases} x + z = 2 \\ 2x + y = 3 \\ y - z = 4 \end{cases}$$

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

**Solve the system of equations by using the inverse of the coefficient matrix.**

187)  $x + y + z = 4$  187) \_\_\_\_\_

$$x - y + 5z = -18$$

$$3x + y + z = 8$$

A)  $x = -3, y = 5, z = 2$

B)  $x = -3, y = 2, z = 5$

C)  $x = 2, y = 5, z = -3$

D) No inverse, no solution for system

188)  $x - y + 2z = 8$  188) \_\_\_\_\_

$$3x + z = 2$$

$$x + 4y + z = -14$$

A)  $x = 2, y = 0, z = -4$

B)  $x = 0, y = -4, z = 2$

C)  $x = 2, y = -4, z = 0$

D) No inverse, no solution for system

189)  $x - y + z = -1$  189) \_\_\_\_\_

$$x + y + z = -11$$

$$x + y - z = -7$$

A)  $x = -2, y = -4, z = -5$

B)  $x = -4, y = -5, z = -2$

C)  $x = -4, y = -2, z = -5$

D) No inverse, no solution for system

190)  $x - y + 2z = 5$  190) \_\_\_\_\_

$$3x + z = 0$$

$$x + 4y + z = -20$$

A)  $x = 0, y = -5, z = 5$

B)  $x = 0, y = -5, z = 0$

C)  $x = 0, y = 0, z = -5$

D) No inverse, no solution for system

**Solve the problem.**

191) A company makes 3 types of cable. Cable A requires 3 black wires, 3 white wires, and 2 red wires. 191) \_\_\_\_\_

Cable B requires 1 black, 2 white, and 1 red. Cable C requires 2 black, 1 white, and 2 red. If 100 black wires, 110 white wires, and 90 red wires were used, then how many of each cable were made?

A) 20 cable A, 30 cable B, 10 cable C

B) 10 cable A, 30 cable B, 93 cable C

C) 10 cable A, 103 cable B, 20 cable C

D) 10 cable A, 30 cable B, 20 cable C

192) A company makes 3 types of cable. Cable A requires 3 black wires, 3 white wires, and 2 red wires. 192) \_\_\_\_\_

Cable B requires 1 black, 2 white, and 1 red. Cable C requires 2 black, 1 white, and 2 red. If 95 black wires, 100 white wires, and 90 red wires were used, then how many of each cable were made?

A) 58 cable A, 30 cable B, 22 cable C

B) 5 cable A, 18 cable B, 25 cable C

C) 30 cable A, 5 cable B, 25 cable C

D) 5 cable A, 30 cable B, 25 cable C

- 193) A basketball fieldhouse seats 15,000. Courtside seats cost \$10, endzone seats cost \$6, and balcony seats cost \$5. The total revenue for a sellout is \$92,000. If half the courtside seats, half the balcony seats, and all the endzone seats are sold; then the total revenue is \$52,000. How many of each type of seat are there? 193) \_\_\_\_\_
- A) 4000 courtside, 3000 endzone, 8000 balcony  
 B) 3200 courtside, 1800 endzone, 10,000 balcony  
 C) 3000 courtside, 4000 endzone, 8000 balcony  
 D) 3000 courtside, 2000 endzone, 10,000 balcony

- 194) The economy of a small country can be regarded as consisting of three industries, I, II, and III, whose input-output matrix is 194) \_\_\_\_\_

$$A = \begin{matrix} & \begin{matrix} \text{I} & \text{II} & \text{III} \end{matrix} \\ \begin{matrix} \text{I} \\ \text{II} \\ \text{III} \end{matrix} & \begin{bmatrix} 0.20 & 0.01 & 0.30 \\ 0.30 & 0.10 & 0.02 \\ 0.05 & 0.40 & 0.10 \end{bmatrix} \end{matrix}$$

The entry in the third row, second column of matrix A means that

- A) industry II uses 40% of industry III's output.  
 B) industry III uses 40% of industry II's output.  
 C) to make \$1 worth of output, industry III needs \$0.40 worth of input from industry II.  
 D) to make \$1 worth of output, industry II needs \$0.40 worth of input from industry III.  
 E) none of these

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

- 195) Solve the following matrix equation for X:  $AX = BX + C$ . 195) \_\_\_\_\_

- 196) Solve the matrix equation for  $AX = BX + C$  for  $X = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$  196) \_\_\_\_\_

where  $A = \begin{bmatrix} 6 & 0 \\ 15 & 1 \end{bmatrix}$ ,  $B = \begin{bmatrix} -1 & -2 \\ 4 & -2 \end{bmatrix}$ , and  $C = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$ .

- 197) If A is given by  $A = \begin{bmatrix} 0.6 & 0.4 \\ 0.2 & 0.3 \end{bmatrix}$ , find  $I - A$ . 197) \_\_\_\_\_

- 198) Let  $A = \begin{bmatrix} 3 & 6 \\ 2 & 4 \end{bmatrix}$ . Find  $(I - A)^{-1}$ . 198) \_\_\_\_\_

- 199) If A is given by  $A = \begin{bmatrix} 0.6 & 0.4 \\ 0.2 & 0.3 \end{bmatrix}$ , find  $(I - A)^{-1}$  199) \_\_\_\_\_

- 200) Solve the matrix equation  $X = AX + D$  for the unknown matrix  $X = \begin{bmatrix} x \\ y \end{bmatrix}$ , where  $A = \begin{bmatrix} 9 & 3 \\ 2 & 3 \end{bmatrix}$ ,  $D = \begin{bmatrix} 30 \\ 40 \end{bmatrix}$ . 200) \_\_\_\_\_

- 201) Let  $A = \begin{bmatrix} 0.3 & 0.5 & 0 \\ 0 & 0.2 & 0.4 \\ 0.1 & 0.1 & 0.2 \end{bmatrix}$ ,  $X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ , and  $D = \begin{bmatrix} 10 \\ 20 \\ 30 \end{bmatrix}$ . Solve the matrix equation  $(I - A)X = D$ . 201) \_\_\_\_\_

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

202) Find the solution  $X$  for the matrix equation  $X - AX = D$ .

202) \_\_\_\_\_

- A)  $X = D(I - A)^{-1}$
- B)  $X = D(A - I)^{-1}$
- C)  $X = (A - I)^{-1} D$
- D)  $X = (I - A)^{-1} D$
- E) none of these

203) Find the solution  $X$  for the matrix equation  $XA + XB = C$ .

203) \_\_\_\_\_

- A)  $X = (B + A)^{-1} C$
- B)  $X = (A + B)^{-1} C$
- C)  $X = C(A + B)^{-1}$
- D)  $X = C(B + A)^{-1}$
- E) none of these

**Solve the problem.**

204) The economy of a small country can be regarded as consisting of three industries, I, II, and III, whose input-output matrix is

204) \_\_\_\_\_

$$A = \begin{matrix} & \begin{matrix} \text{I} & \text{II} & \text{III} \end{matrix} \\ \begin{matrix} \text{I} \\ \text{II} \\ \text{III} \end{matrix} & \begin{bmatrix} 0.20 & 0.01 & 0.30 \\ 0.30 & 0.10 & 0.02 \\ 0.05 & 0.40 & 0.10 \end{bmatrix} \end{matrix}$$

Suppose  $x$ ,  $y$ , and  $z$  represent the output of industries I, II, and III, respectively. An algebraic expression for the amount of output from industry III that can be exported is

- A)  $z - (0.05x + 0.40y + 0.10z)$ .
- B)  $z + (0.05x + 0.40y + 0.10z)$ .
- C)  $z - (0.30x + 0.02y + 0.10z)$ .
- D)  $z + (0.30x + 0.02y + 0.10z)$ .
- E) none of these

**SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.**

205) An economy consists of steel and coal. The steel industry consumes \$ 0.25 of coal and \$ 0.02 of steel to produce \$1 of steel. The coal industry requires \$0.04 of coal and \$0.01 of steel to produce \$1 of coal.

205) \_\_\_\_\_

(a) If the total production in millions of dollars of steel and coal is given by the matrix  $X =$

$$\begin{bmatrix} 2 \\ 3 \end{bmatrix}, \text{ find the amounts of steel and coal used in production.}$$

(b) Compute the amounts of steel and coal available which can be consumed or exported.



- 206) A large insurance company has a data processing division and an actuarial division. For each \$1 worth of output the data processing division needs \$0.20 worth of data processing and \$0.40 worth of actuarial science. For each \$1 worth of output, the actuarial division needs \$0.30 worth of data processing and \$0.10 of actuarial science.
- (a) Write the input-output matrix for the insurance company.
- (b) The company estimates a demand of 5 million dollars for the data processing division and 2 million for the actuarial division. Let  $x$  be the production level of the data processing division and let  $y$  be the production level of the actuarial division. Write a matrix equation to fit this problem.
- (c) At what levels should each division produce to meet the demand?
- 206) \_\_\_\_\_

- 207) The economy of Mongovia is composed of three industries: I, II, and III. Suppose that in order to produce \$1 worth of industry I, it takes \$0.02 worth of I, \$0.20 worth of II and \$0.30 worth of III. To produce \$1 worth of industry II, it takes \$0.05 worth of I, \$0.02 worth of II, and \$0.20 worth of III. To produce \$1 worth of industry III, it takes \$0.10 worth of I, \$0.15 worth of II, and \$0.02 worth of III.
- (a) Write the input-output matrix for this economy.
- (b) How much should each industry produce to allow for consumption at these levels: \$3 million for I, \$2 million for II, and \$3 million for III?
- 207) \_\_\_\_\_

- 208) An economy consists of steel and coal. The steel industry consumes \$ 0.25 of coal and \$ 0.02 of steel to produce \$1 of steel. The coal industry requires \$0.04 coal and \$0.01 steel to produce \$1 coal.
- (a) What is the input-output matrix for this economy?
- (b) What is the amount of coal needed for a steel production level of \$30 million?
- 208) \_\_\_\_\_

- 209) The economy of a small country can be regarded as consisting of three industries, I, II, III, whose input-output matrix is
- $$A = \begin{matrix} & \begin{matrix} \text{I} & \text{II} & \text{III} \end{matrix} \\ \begin{matrix} \text{I} \\ \text{II} \\ \text{III} \end{matrix} & \begin{bmatrix} 0.2 & 0.3 & 0.05 \\ 0.01 & 0.1 & 0.4 \\ 0.3 & 0.02 & 0.1 \end{bmatrix} \end{matrix}$$
- 209) \_\_\_\_\_

If  $x$ ,  $y$ , and  $z$  represent the outputs of industries I, II, and III respectively, write an algebraic expression for the amount of output from industry II that can be exported.

- 210) An economy consisting of agriculture (I) and manufacturing (II) has the following input-output matrix.
- $$A = \begin{matrix} & \begin{matrix} \text{I} & \text{II} \end{matrix} \\ \begin{matrix} \text{I} \\ \text{II} \end{matrix} & \begin{bmatrix} 0.1 & 0.3 \\ 0.3 & 0.4 \end{bmatrix} \end{matrix}$$
- 210) \_\_\_\_\_

How many units of agriculture and manufacturing should be produced in order to meet a demand for 15 units from I and 9 units from II?

**MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.**

- 211) Suppose the following matrix represents the input–output matrix of a primitive economy that depends on two basic goods, yams and pigs. How much of each commodity should be produced to get 1 bushels of yams and 14 pigs? (It is not necessary to round to a whole–number quantity of pigs.) 211) \_\_\_\_\_

$$\begin{array}{c} \text{yams pigs} \\ \text{yams} \begin{bmatrix} 1/4 & 1/6 \end{bmatrix} \\ \text{pigs} \begin{bmatrix} 1/2 & 0 \end{bmatrix} \end{array}$$

- A) 5 bushels of yams and 16.88 pigs  
B) 12 bushels of yams and 16 pigs  
C) 17.25 bushels of yams and 16 pigs  
D) 5 bushels of yams and 16.5 pigs

- 212) Suppose the following matrix represents the input–output matrix of a simplified economy that involves just three commodity categories: manufacturing, agriculture, and transportation. How many units of each commodity should be produced to satisfy a demand of 800 units for each commodity? 212) \_\_\_\_\_

$$\begin{array}{c} \text{Mfg Agri Trans} \\ \text{Mfg} \begin{bmatrix} 0 & 1/4 & 1/3 \end{bmatrix} \\ \text{Agri} \begin{bmatrix} 1/2 & 0 & 1/4 \end{bmatrix} \\ \text{Trans} \begin{bmatrix} 1/4 & 1/4 & 0 \end{bmatrix} \end{array}$$

- A) 2240 units of manufacturing, 1864 units of agriculture, and 2008 units of transportation  
B) 2008 units of manufacturing, 2240 units of agriculture, and 1864 units of transportation  
C) 2008 units of manufacturing, 1864 units of agriculture, and 1992 units of transportation  
D) 1992 units of manufacturing, 2256 units of agriculture, and 1864 units of transportation

- 213) Suppose the following matrix represents the input–output matrix of a primitive economy that depends on two basic goods, yams and pigs. How much of each commodity should be produced to satisfy a demand for 96 bushels of yams and 64 pigs? (It is not necessary to round to a whole–number quantity of pigs.) 213) \_\_\_\_\_

$$\begin{array}{c} \text{yams pigs} \\ \text{yams} \begin{bmatrix} 1/4 & 1/6 \end{bmatrix} \\ \text{pigs} \begin{bmatrix} 1/2 & 0 \end{bmatrix} \end{array}$$

- A) 192 bushels of yams and 96 pigs  
B) 160 bushels of yams and 180 pigs  
C) 160 bushels of yams and 144 pigs  
D) 216 bushels of yams and 96 pigs

- 214) Suppose the following matrix represents the input–output matrix of a simplified economy with just three sectors: manufacturing, agriculture, and transportation.

214) \_\_\_\_\_

$$\begin{array}{c} \text{Mfg} \quad \text{Agri} \quad \text{Trans} \\ \text{Mfg} \begin{bmatrix} 0 & 0.25 & 0.33 \\ 0.50 & 0 & 0.25 \\ 0.25 & 0.25 & 0 \end{bmatrix} \\ \text{Agri} \\ \text{Trans} \end{array}$$

Suppose also that the demand matrix is as follows:

$$D = \begin{bmatrix} 530 \\ 270 \\ 108 \end{bmatrix}$$

Find the amount of each commodity that should be produced.

- A) 937 units of manufacturing, 1055 units of agriculture, and 562 units of transportation
- B) 1124 units of manufacturing, 1055 units of agriculture, and 674 units of transportation
- C) 937 units of manufacturing, 879 units of agriculture, and 562 units of transportation
- D) 714 units of manufacturing, 631 units of agriculture, and 48 units of transportation

- 215) Suppose the following matrix represents the input–output matrix,  $T$ , of a simplified economy.

215) \_\_\_\_\_

$$\begin{array}{c} \text{Manufacturing} \quad \text{Agriculture} \quad \text{Transportation} \\ \text{Manufacturing} \begin{bmatrix} 0 & 1/4 & 1/3 \\ 1/2 & 0 & 1/4 \\ 1/4 & 1/4 & 0 \end{bmatrix} \\ \text{Agriculture} \\ \text{Transportation} \end{array}$$

The demand matrix is

$$D = \begin{bmatrix} 1500 \\ 1500 \\ 1500 \end{bmatrix}$$

Find the amount of each commodity that should be produced.

- A) 3765 units of manufacturing, 3495 units of agriculture, and 3720 units of transportation.
- B) 3765 units of manufacturing, 4200 units of agriculture, and 3489 units of transportation.
- C) 3720 units of manufacturing, 4233 units of agriculture, and 3489 units of transportation.
- D) 4200 units of manufacturing, 3495 units of agriculture, and 3765 units of transportation.

- 216) A simplified economy is based on agriculture, manufacturing, and transportation. Each unit of agricultural output requires 0.3 unit of its own output, 0.5 of manufacturing, and 0.2 unit of transportation output. Each unit of manufacturing output requires 0.3 unit of its own output, 0.1 of agricultural, and 0.4 unit of transportation output. Each unit of transportation output requires 0.4 unit of its own output, 0.2 of agricultural, and 0.1 of manufacturing output. There is demand for 15 units of agricultural, 70 units of manufacturing, and 50 units of transportation output. How many units should each segment of the economy produce?

216) \_\_\_\_\_

- A) Agriculture: 218; manufacturing: 265; transportation: 272
- B) Agriculture: 265; manufacturing: 272; transportation: 218
- C) Agriculture: 272; manufacturing: 265; transportation: 218
- D) Agriculture: 272; manufacturing: 218; transportation: 265

# Answer Key

Testname: UNTITLED2

1) 
$$\begin{cases} x - 5y = 4 \\ 12y = -3 \end{cases}$$

2) B

3) A

4) B

5) D

6) D

7) A

8) B

9)  $R_2 \leftrightarrow R_3$

10)

$$\xrightarrow{R_3 + 5R_2} \begin{bmatrix} 1 & 0 & 3 & 9 \\ 0 & 1 & -3 & 2 \\ 0 & 0 & -11 & 11 \end{bmatrix}$$

11)

$$\xrightarrow{R_2 + 2R_3} \begin{bmatrix} 1 & 0 & 0 & -3 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

12)

$$\xrightarrow{R_3 + (-2)R_1} \begin{bmatrix} 1 & 2 & -3 & 3 \\ 0 & -4 & 6 & 7 \\ 0 & 2 & 11 & -7 \end{bmatrix}$$

13)  $x = 2, y = -1, z = 4$  is not a solution because these values do not satisfy the third equation.

14)  $x = 2, y = -1, z = 4$  is a solution because these values satisfy every equation.

15) The solution to a system of equations is the set of all values such that each value satisfies every equation in the system.

16) A

17) C

18) C

19) B

20) B

21) B

22) A

23) D

24) 11 type A cell phones

25)

$$\begin{cases} x + y + z = 15 \\ -2x + y - 2z = 0 \\ x + y = 13 \end{cases}$$

$x = 3, y = 10, z = 2$ ; The company should spend \$3,000,000 in radio advertising, \$10,000,000 in television advertising, and \$2,000,000 in newspaper advertising.

26)  $x = 24$  = number of women;  $y = 12$  = number of men

27) B

28) D

29) C

30) C

31) C

32) B

33) C

## Answer Key

Testname: UNTITLED2

34)

$$\begin{bmatrix} \frac{1}{3} & 1 \\ \frac{14}{3} & 0 \end{bmatrix}$$

35)

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 13 \end{bmatrix}$$

36)

$$\begin{bmatrix} -1 & 0 & 4 \\ 2 & 1 & -3 \\ 2 & 0 & 6 \end{bmatrix}$$

37)  $z = \text{any value}, x = 3, y = 2z + 1;$

two possible solutions:  $x = 3, y = 1, z = 0$  and  $x = 3, y = 3, z = 1$

38)  $z = \text{any value}, x = -4z - 5, y = -3z - 2;$

two possible solutions:  $x = -5, y = -2, z = 0$  and  $x = -9, y = -5, z = 1$

39) unique solution;  $x = 3, y = 1, z = 0$

40)  $x = -4, y = 1$

41)  $z = \text{any value}, x = -4z - 5, y = -3z - 2$

42) infinitely many solutions:  $y = \text{any value}, x = y - 21, z = 7$

43) one solution:  $x = -180, y = 50, z = 17$

44) no solution

45) The system has infinitely many solutions; the general solution is:

$z = \text{any value}, x = 4, y = 3 - z.$

46) The system has infinitely many solutions; the general solution is:

$z = \text{any value}, x = 4 - 2z, y = 3 - z.$

47) The system has no solution.

48) A

49) B

50) D

51) B

52) L and M intersect in one point:  $(7, -3).$

53)  $K = 6$

54)  $z = -2, x + y = 3;$  the general solution is:  $x = \text{any value}, y = 3 - x, z = -2.$

55) Answers will vary. Solutions are of the form:  $x = \text{any value}, y = 2, z = 8x - 3.$

Three possible solutions are:

$x = 0, y = 2, z = -3$

$x = 1, y = 2, z = 5$

$x = 2, y = 2, z = 13$

56)  $K = 2$

57)  $K \neq 2$

58) One possible solution is  $x = 3, y = 0, z = 2, w = 1.$

59) One possible solution is  $x = 3, y = 0, z = 2, w = 4.$

60) C

61) C

62) D

63) A

64) D

## Answer Key

Testname: UNTITLED2

65) C

66) B

67) A

68) D

69) C

70) D

71) A

72) D

73) D

74) B

75) C

76) D

77) C

78)  $x = 8, y = 3$

79) There are no values of  $x$  and  $y$  that make  $A = B$ .

80) Answers will vary.

(a) Possible solutions: any two matrices such that the number of columns in  $A$  is not the same as the number of rows in  $B$ .

One possible example is  $A = \begin{bmatrix} 2 & 4 \\ 3 & 1 \end{bmatrix}$  and  $B = \begin{bmatrix} 5 \\ 1 \\ 7 \end{bmatrix}$ .

(b) Possible solution: any  $2 \times 2$  matrix such that  $\Delta = 0$ , or having a row of zeros.

Possible examples:  $\begin{bmatrix} 6 & 4 \\ 3 & 2 \end{bmatrix}$  or  $\begin{bmatrix} 0 & 1 \\ 0 & 0 \end{bmatrix}$ .

(c) Possible solutions: any two matrices such that the number of columns in  $C$  is the same as the number of rows in  $D$ , but the number of rows in  $C$  is not equal to the number of columns in  $D$ .

One possible example is  $C = \begin{bmatrix} 3 & 2 & 1 \\ 1 & -2 & 0 \end{bmatrix}$  and  $D = \begin{bmatrix} 4 \\ 8 \\ -2 \end{bmatrix}$ .

81) D

82) A

83) A

84) A

85) A

86) C

87) D

88) D

89) D

90) The calculation is not possible.

91)

$$\begin{bmatrix} 4 & -3 & -3 \\ -5 & -4 & 6 \end{bmatrix}$$

92) The calculation is not possible.

93)

$$\begin{bmatrix} -2 & 6 & 0 \\ 10 & 14 & -3 \end{bmatrix}$$

94)

$$\begin{bmatrix} -1 & -5 \\ -\frac{7}{2} & -1 \end{bmatrix}$$

## Answer Key

Testname: UNTITLED2

95)

$$\begin{bmatrix} 17 \\ 30 \\ 25 \end{bmatrix}$$

96) The calculation is not possible.

97) The calculation is not possible.

98) E

99) A

100) D

101) B

102) A

103)

$$\begin{bmatrix} 15 & -2 \\ 31 & 1 \end{bmatrix}$$

104)

$$\begin{bmatrix} 4 & 0 & 3 \\ 8 & 0 & 6 \\ -20 & 0 & -15 \end{bmatrix}$$

105) The calculation is not possible.

106) The calculation is not possible.

107)

$$\begin{bmatrix} 6 \\ 5 \end{bmatrix}$$

108)  $AB = BA = I_2$

109) No.

$$AB = \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix} = \begin{bmatrix} 17 & 14 \\ 14 & 13 \end{bmatrix}$$

$$BA = \begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} 1 & 4 \\ 2 & 3 \end{bmatrix} = \begin{bmatrix} 5 & 10 \\ 10 & 25 \end{bmatrix}$$

110)  $a = -4$ ,  $b = -2$

$$111) A = \begin{bmatrix} 0 & -1 \\ 1 & -2 \end{bmatrix}$$

112) D

113) D

114) A

115) D

116) B

117) D

118) A

119) B

120) A

121)

$$\begin{bmatrix} 1 & 3 \\ 2 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 6 \\ 3 \end{bmatrix}$$

122)

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 6 & 7 \\ 1 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 4 \\ 8 \\ 5 \end{bmatrix}$$

# Answer Key

Testname: UNTITLED2

123)

$$\begin{bmatrix} 1 & 1 & 4 \\ 4 & 1 & -2 \\ -3 & 0 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ -6 \\ 1 \end{bmatrix}$$

124)

$$\begin{cases} 3x + y + 2z = 1 \\ -x + 2z = 2 \\ 4y + z = -1 \end{cases}$$

125) C

126) Let  $B = \begin{bmatrix} 60 & 30 & 10 \end{bmatrix}$

$$BA = \begin{bmatrix} 60 & 30 & 10 \end{bmatrix} \begin{bmatrix} 0.6 & 0.4 \\ 0.3 & 0.7 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} 55 & 45 \end{bmatrix}$$

The vote is 55 in favor, 45 against.

127) Let  $B = \begin{bmatrix} 15 & 10 \end{bmatrix}$ . Then  $BA = \begin{bmatrix} 795 & 1040 & 980 \end{bmatrix}$ .

Therefore, the total hourly pay for factory I = \$795, for II = \$1,040, and for III = \$980.

128) B

129) (a)

$$\begin{bmatrix} 0.9 & 0.3 \\ 0.1 & 0.7 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} p \\ n \end{bmatrix}$$

(b)

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} \frac{7}{6} & -\frac{1}{2} \\ -\frac{1}{6} & \frac{3}{2} \end{bmatrix} \begin{bmatrix} p \\ n \end{bmatrix}$$

$$(c) \quad y = -\frac{1}{6}(120) + \frac{3}{2}(80) = 100$$

130) B

131) A

132) D

133) C

134) D

135) D

$$136) \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

137) Inverse does not exist.

$$138) \begin{bmatrix} 0.8 & 0.1 \\ 0.6 & 0.2 \end{bmatrix}$$

$$139) \begin{bmatrix} 1.8 & -0.2 \\ -0.8 & 1.2 \end{bmatrix}$$

$$140) \begin{bmatrix} \frac{1}{3} & -\frac{2}{3} \\ 0 & 1 \end{bmatrix}$$

141) Inverse does not exist.

$$142) \begin{bmatrix} 1 \\ 6 \end{bmatrix}$$

$$143) [2.5]$$



## Answer Key

Testname: UNTITLED2

144) Yes

145) No.

146)

$$A = \begin{bmatrix} 3 & -2 & -1 \\ -5 & 4 & 4 \\ -6 & 5 & 5 \end{bmatrix}$$

147) A

148) D

149) A

150) D

151) D

152) B

153) C

154)  $x = -3, y = 5$

155)  $x = 9, y = -2, z = -2$

156)  $x = 23, y = 9, z = -12$

157)  $x = 2, y = 3, z = 1, w = -1$

158) (a)

$$\begin{bmatrix} 3 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ 8 \end{bmatrix}$$

(b)

$$\begin{bmatrix} \frac{1}{3} & -\frac{2}{3} \\ 0 & 1 \end{bmatrix}$$

(c)  $x = -3, y = 8$

159) (a)

$$\begin{bmatrix} 2 & 3 \\ -2 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ 8 \end{bmatrix}$$

(b)

$$\begin{bmatrix} -\frac{1}{4} & -\frac{3}{4} \\ \frac{1}{2} & \frac{1}{2} \end{bmatrix}$$

(c)  $x = -7, y = 6$

160) (a)

$$\begin{bmatrix} 0.7 & 0.2 \\ 0.3 & 0.8 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$$

(b)

$$\begin{bmatrix} 1.6 & -0.4 \\ -0.6 & 1.4 \end{bmatrix}$$

(c)  $x = 4, y = 1$

161) (a)  $\begin{bmatrix} -1 & 1 \\ 3 & -2 \end{bmatrix}$  (b)  $x = -3, y = 8$

# Answer Key

Testname: UNTITLED2

162)

$$C = \begin{bmatrix} 16 & 11 \\ -22 & -16 \end{bmatrix}$$

163)

$$C = \begin{bmatrix} 5 & 7 & 9 \\ -4 & -5 & -6 \\ -8 & -13 & -18 \end{bmatrix}$$

164)

$$X = \begin{bmatrix} 12 \\ 31 \end{bmatrix}$$

165)  $X = A^{-1} (C - BY)$

166) D

167) A

168) A

169) (a)

$$\begin{bmatrix} 0.6 & 0.1 \\ 0.4 & 0.9 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} u \\ v \end{bmatrix}.$$

(b)

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1.8 & -0.2 \\ -0.8 & 1.2 \end{bmatrix} \begin{bmatrix} u \\ v \end{bmatrix}$$

(c) 1000

170) D

171)  $\left[ \begin{array}{cc|cc} 3 & 1 & 1 & 0 \\ 2 & 1 & 0 & 1 \end{array} \right], \left[ \begin{array}{cc|cc} 1 & \frac{1}{3} & \frac{1}{3} & 0 \\ 2 & 1 & 0 & 1 \end{array} \right], \left[ \begin{array}{cc|cc} 1 & \frac{1}{3} & \frac{1}{3} & 1 \\ 0 & \frac{1}{3} & -\frac{2}{3} & 1 \end{array} \right], \left[ \begin{array}{cc|cc} 1 & \frac{1}{3} & \frac{1}{3} & 0 \\ 0 & 1 & -2 & 3 \end{array} \right], \left[ \begin{array}{cc|cc} 1 & 0 & 1 & -1 \\ 0 & 1 & -2 & 3 \end{array} \right]$

$$\begin{bmatrix} 3 & 1 \\ 2 & 1 \end{bmatrix}^{-1} = \begin{bmatrix} 1 & -1 \\ -2 & 3 \end{bmatrix}$$

172)

$$A^{-1} = \begin{bmatrix} 5 & 0 & -1 \\ -3 & -1 & 1 \\ -1 & 1 & 0 \end{bmatrix}$$

173)

$$\begin{bmatrix} -7 & 2 \\ -3 & 1 \end{bmatrix}$$

174) Row reduction of the original matrix results in a matrix with a row of zeros.

175)

$$\begin{bmatrix} 1 & 2 & -2 \\ 1 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

176) Inverse does not exist.

177) Inverse does not exist.

178)

$$\begin{bmatrix} 1 & 0 & 0 \\ -13 & -5 & 1 \\ 2 & 1 & 0 \end{bmatrix}$$

## Answer Key

Testname: UNTITLED2

179) B

180) D

181)  $x = 3, y = -1, z = 6$

182)  $x = 2, y = -1, z = 3$

183)  $x = 3, y = \frac{3}{2}, z = \frac{3}{2}$

184) (a)

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 2 \\ 0 & 0 & \frac{1}{2} \end{bmatrix}$$

(b)  $x = -2, y = 8, z = \frac{3}{2}$

185) (a)

$$\begin{bmatrix} 4 & -2 & 3 \\ 8 & -3 & 5 \\ 7 & -2 & 4 \end{bmatrix}$$

(b)  $x = 13, y = 23, z = 19$

186) (a)

$$\begin{bmatrix} -1 & 1 & -1 \\ 2 & -1 & 2 \\ 2 & -1 & 1 \end{bmatrix}$$

(b)  $x = -3, y = 9, z = 5$

187) C

188) B

189) B

190) B

191) D

192) D

193) D

194) D

195)  $X = (A - B)^{-1}C$

196)  $X = \begin{bmatrix} 1 \\ -3 \end{bmatrix}$

197)

$$\begin{bmatrix} 0.4 & -0.4 \\ -0.2 & 0.7 \end{bmatrix}$$

198)

$$\begin{bmatrix} \frac{1}{2} & -1 \\ -\frac{1}{3} & \frac{1}{3} \end{bmatrix}$$

199)

$$\begin{bmatrix} 3.5 & 2 \\ 1 & 2 \end{bmatrix}$$

200)  $x = 6, y = -26$

Answer Key

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201)

$$I - A = \begin{bmatrix} 0.7 & -0.5 & 0 \\ 0 & 0.8 & -0.4 \\ -0.1 & -0.1 & 0.8 \end{bmatrix}, (I - A)^{-1} = \begin{bmatrix} 1.5 & 1 & 0.5 \\ 0.1 & 1.4 & 0.7 \\ 0.2 & 0.3 & 1.4 \end{bmatrix}, X = \begin{bmatrix} 50 \\ 50 \\ 50 \end{bmatrix}$$

202) D

203) C

204) A

205) (a)  $\begin{bmatrix} 0.02 & 0.01 \\ 0.25 & 0.04 \end{bmatrix} \begin{bmatrix} 2 \\ 3 \end{bmatrix} = \begin{bmatrix} 0.07 \\ 0.62 \end{bmatrix}$ , that is \$70,000 steel, \$620,000 coal.

(b) \$1.93 million steel, \$2.38 million coal

206) (a)

	DPD	AD
DPD	$\begin{bmatrix} 0.20 & 0.30 \end{bmatrix}$	
AD	$\begin{bmatrix} 0.40 & 0.10 \end{bmatrix}$	

(b)  $\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0.20 & 0.30 \\ 0.40 & 0.10 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} 5 \\ 2 \end{bmatrix}$

(c) data processing division should produce \$8.5 million, actuarial division should produce \$6 million

207) (a)

	I	II	III
I	$\begin{bmatrix} 0.02 & 0.05 & 0.10 \end{bmatrix}$		
II	$\begin{bmatrix} 0.20 & 0.02 & 0.15 \end{bmatrix}$		
III	$\begin{bmatrix} 0.30 & 0.20 & 0.02 \end{bmatrix}$		

(b) \$3.75 million worth of industry I, \$3.56 million worth of industry II, \$4.93 million worth of industry III.

208) (a)

	steel	coal
steel	$\begin{bmatrix} 0.02 & 0.01 \end{bmatrix}$	
coal	$\begin{bmatrix} 0.25 & 0.04 \end{bmatrix}$	

(b) \$7.5 million

209)  $y - (0.01x + 0.1y + 0.4z)$

210) 26 units of agriculture and 28 of manufacturing

211) D

212) D

213) C

214) C

215) C

216) C