

	A	B	C	D	E	F	G	H	I	J
1	<b>BOND PRICING</b>	<b>Annual Payments</b>								
2										
3										
4										
5										
6										
7	<b>Inputs</b>									
8	Number of Periods to Maturity (T)	8	8							
9	Face Value (PAR)	\$1,000	20							
10										
11										
12	Discount Rate / Period (r)	3.25%	6							
13	Coupon Payment (PMT)	\$35.00	7							
14										
15	<b>Bond Price using a Timeline</b>									
16	Period	0	1	2	3	4	5	6	7	8
17										
18	Cash Flows		\$35.00	\$35.00	\$35.00	\$35.00	\$35.00	\$35.00	\$35.00	\$1,035.00
19	Present Value of Cash Flows		\$33.80	\$32.83	\$31.80	\$30.80	\$29.83	\$28.89	\$27.98	\$801.35
20	Bond Price	\$1,017.37								
21										
22	<b>Bond Price using the Formula</b>									
23	Bond Price (P)	\$1,017.37								
24										
25	<b>Bond Price using the PV Function</b>									
26	Bond Price	\$1,017.37								
27										
28										
29										
30										
31										
32										
33										
34										
35										
36										

1. Input Payment  
Enter =PMT (Rate, Nper, PV, FV, Type)  
Enter =PMT(0.0325/2, 8, 1000, 0, 0)

2. Input Payment = Face Value \*  
Enter =1000\*0.0325

3. (Cash Flow \* (1 - Discount Rate / Period)  
Enter =1000\*(1 - 0.0325/2) + 0.0325/2

4. Input the Present Value of Cash Flows  
Enter =PV(0.0325/2, 8, 35, 1035, 0)

5. The Bond Price Formula

$$P = \frac{PMT \cdot \left(1 - \left(\frac{1}{(1+r)^T}\right)\right)}{r} + \frac{PAR}{(1+r)^T}$$

Enter =35\*(1 - 1/(1+0.0325/2)^8)/(0.0325/2) + 1000/(1+0.0325/2)^8



# BOND PRICING

# Duration and Convexity

Currency:

## Inputs

Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2	Annual Percentage Rate
Annual Coupon Rate	4.00%	8	
Yield to Maturity (Annualized)	1.74%	3	
Number of Payments / Year	2	2	
Number of Periods to Maturity (T)	8	8	
Face Value (PAR)	\$1,000	20	

## Outputs

Discount Rate / Period (r)	0.9%
Coupon Payment (PMT)	\$20

## Bond Duration using a Timeline

Period	0	1	2	3	4	5
Time (Years)	0.0	0.5	1.0	1.5	2.0	2.5
Cash Flows		\$20.00	\$20.00	\$20.00	\$20.00	\$20.00
Present Value of Cash Flows		\$19.83	\$19.66	\$19.49	\$19.32	\$19.15
Bond Price using a Timeline	\$1,086.96					
Weight		1.8%	1.8%	1.8%	1.8%	1.8%
Weight * Time		0.01	0.02	0.03	0.04	0.04
Duration using a Timeline	3.75					
Modified Duration using a Timeline	3.72					

## Bond Duration using a Formula

Duration (D) using a Formula	3.75
Modified Duration using a Formula	3.72

## Bond Duration using a Function (under APR)

Duration using a Function	3.75
Modified Duration using a Function	3.72

(7) DURATION (Settlement Date, Maturity Date, Annual Coupon Rate, Yield to Maturity, Number of Periods)  
Enter =IF(\$C\$4=1,"",DURATION(DATE(2000,1,1), DATE(2000+B8/B7,1,1),B5,B6,B7))

(8) MDURATION (Settlement Date, Maturity Date, Annual Coupon Rate, Yield to Maturity, Number of Periods)  
Enter =IF(\$C\$4=1,"",MDURATION(DATE(2000,1,1), DATE(2000+B8/B7,1,1),B5,B6,B7))

(2) PV of Cash Flow on Date t / Total  
Enter =C19/\$B\$20 and copy across

(3) Weight \* Time  
Enter =C21\*C17 and copy across

(4) Sum of all the Weight \* Times  
Enter =SUM(C22:J22)

(5) Duration / (1+(Discount Rate / Period)  
Enter =B23/(1+\$B\$12) and copy across

(6) The Duration Formula is:  

$$D = \frac{1+r}{r \cdot NOP} - \frac{1+r+T \cdot (CR \cdot ((1+r)^T - 1))}{CR \cdot ((1+r)^T - 1)}$$
 Enter =(1+B12)/(B12\*B7)-(1+B12)/(B5\*((1+B12)^B8-1)+B12\*B7)

## Bond Convexity

Weight * (Time^2+Time)	0.01	0.04	0.07	0.11	0.15
Convexity using a Timeline	18.08				
Convexity using a Formula	18.08				

(9) Weight \* (Time^2 + Time)  
Enter =C21\*(C17^2+C17) and copy across

(10) (Sum of Weight \* (Time ^ 2 + Time) / ((1 + Yield to Maturity / Number of Periods)^Time))  
Enter =SUM(C43:J43)/((1+B6/B7)^B8)

(11) The Convexity Formula is:

$$\frac{\left( CR \cdot (1+r)^{1+T} \cdot (r \cdot (NOP+1) + 2) \right.}{r^2 \cdot NOP^2 \cdot \left( CR \cdot (1+r)^T - CR + r \cdot NOP \right)}$$

Enter =((B5\*((1+B12)^(1+B8))\*(B12\*(B7+1)+2)-B5\*(B12^2\*(B7+B8+1)\*(B8+1)+B12\*(B7+2\*B8+3)-

/((B12^2\*B7^2\*(B5\*(1+B12)^B8-B5+B12\*B7)))/((1+B12)^2))

US Dollar      Exch Rate  
\$1.00 = \$1.00

Currency Number 4  
(Select from below)

1 = Chinese Yuan      ¥ 7.3790  
2 = European Euro      € 0.6805  
3 = Indian Rupee      IDR 39.30  
4 = US Dollar      \$1.00

previous sheet  
ious sheet to B12

6	7	8
3.0	3.5	4.0
\$20.00	\$20.00	\$1,020.00
\$18.99	\$18.82	\$951.71
1.7%	1.7%	87.6%
0.05	0.06	3.50

al PV of all Cash Flows  
oss

ss

eriod))  
y to cell B28

$$\frac{1}{NOP - r}$$
  

$$1) + r \cdot NOP$$
  

$$+ B8 * (B5 / B7 - B12))$$
  

$$B7)$$

0.21      0.27      17.51

opy across

ime))  
r of Payments) ^ 2)  
)^2)

$$\frac{)}{\div ((1+r)^2)}$$

$$+2)+B12^3*B7*B8*(B7+B8))$$

# BOND PRICING

# Price Sensitivity

## Inputs

Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2
Annual Coupon Rate (CR)	3.00%	6
Yield to Maturity (Annualized)	1.74%	3
Number of Payments / Year (NOP)	2	2
Number of Periods to Maturity (T)	8	8
Face Value	\$1,000	20

## Outputs

Discount Rate / Period (r)	0.9%
Coupon Payment	\$15

(1) If Rate Convention = EAR,  
Then  $(1 + \text{Yield To Maturity})^{(1 / (\text{Number of Payments / Year})) - 1}$   
Else  $(\text{Yield To Maturity} / \text{Number of Payment / Year})$   
Enter =IF(\$C\$4=1,((1+B21)^(1/\$B\$7))-1,B21/\$B\$7)  
and copy across

## Chart Outputs

Yield to Maturity (Annualized)	0.50%	1.00%	1.50%	2.00%	2.50%
Discount Rate / Period	0.3%	0.5%	0.8%	1.0%	1.3%
Change in Yield to Maturity	-1.2%	-0.7%	-0.2%	0.3%	0.8%
Actual Bond Price	\$1,099	\$1,078	\$1,058	\$1,038	\$1,019
Current Bond Price	\$1,048	\$1,048	\$1,048	\$1,048	\$1,048
Actual Percent Change in Price	4.8%	2.8%	0.9%	-1.0%	-2.8%
Modified Duration	3.77	3.77	3.77	3.77	3.77
Duration Approximation	4.7%	2.8%	0.9%	-1.0%	-2.9%
Convexity	18.41	18.41	18.41	18.41	18.41
Duration and Convexity Approx.	4.8%	2.8%	0.9%	-1.0%	-2.8%

(5) (Actual Bond Price  
- Current Bond Price)  
/ Current Bond Price  
Enter =(B24-B25)/B25  
and copy across

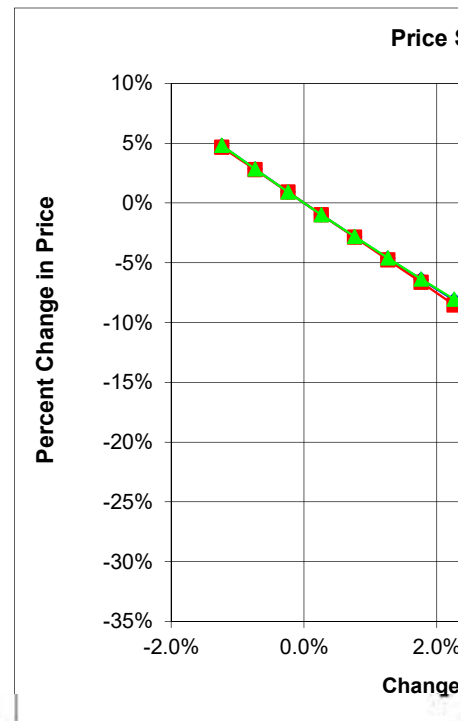
(6) The Modified Duration Formula is:

$$D^* = \left( \frac{1+r}{r \cdot NOP} - \frac{1+r+T \cdot (CR / NOP - r)}{CR \cdot ((1+r)^T - 1) + r \cdot NOP} \right) \div (1+r)$$

Enter =((1+\$B\$12)/(\$B\$12\*\$B\$7)  
-(1+\$B\$12+\$B\$8\*(\$B\$5/\$B\$7-\$B\$12))  
/(\$B\$5\*((1+\$B\$12)^\$B\$8-1)+\$B\$12\*\$B\$7))/(1+\$B\$12)  
and copy across

(9) Duration Approximation  
+ (1/2) \* Convexity \* (Change in YTM)^2  
Enter =B28+(1/2)\*B29\*B23^2 and copy across

(8) The Convexity Formula is:



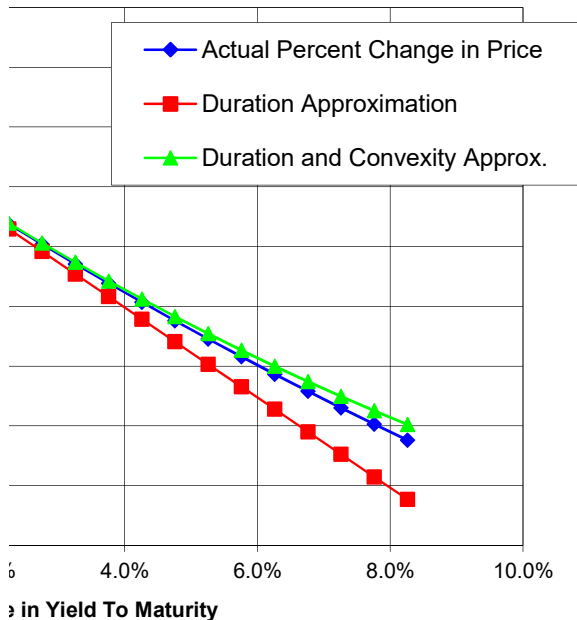
(b) The Convexity Formula is:

$$\frac{\left( CR \cdot (1+r)^{1+T} \cdot (r \cdot (NOP+1) + 2) - CR \cdot (r^2 \cdot (NOP+T+1) \cdot (T+1) + r \cdot (NOP+2 \cdot T+3) + 2) + r^3 \cdot NOP \cdot T \cdot (NOP+T) \right)}{r^2 \cdot NOP^2 \cdot \left( CR \cdot (1+r)^T - CR + r \cdot NOP \right)} \div \left( (1+r)^2 \right)$$

Enter =((B5\*((1+B12)^(1+B8))\*(B12\*(B7+1)+2)-B5\*(B12^2\*(B7+B8+1)\*(B8+B12\*(B7+2\*B8+3)+2)+B12^3\*B7\*B8\*(B7+B8)))/(B12^2\*B7^2\*(B5\*(1+B12)^B8-B5+B12\*B7)))/((1+B12)^2) and copy across

Currency: US Dollar      Exch Rate  
\$1.00 = \$1.00

Sensitivity



Currency Number **4**  
(Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

3.00%	3.50%	4.00%	4.50%	5.00%	5.50%	6.00%	6.50%
1.5%	1.8%	2.0%	2.3%	2.5%	2.8%	3.0%	3.3%
1.3%	1.8%	2.3%	2.8%	3.3%	3.8%	4.3%	4.8%
\$1,000	\$981	\$963	\$946	\$928	\$911	\$895	\$878
\$1,048	\$1,048	\$1,048	\$1,048	\$1,048	\$1,048	\$1,048	\$1,048
-4.6%	-6.4%	-8.1%	-9.8%	-11.5%	-13.1%	-14.7%	-16.2%
3.77	3.77	3.77	3.77	3.77	3.77	3.77	3.77
-4.8%	-6.6%	-8.5%	-10.4%	-12.3%	-14.2%	-16.1%	-18.0%
18.41	18.41	18.41	18.41	18.41	18.41	18.41	18.41
-4.6%	-6.4%	-8.1%	-9.7%	-11.3%	-12.9%	-14.4%	-15.9%

(2) New YTM - Current YTM  
Enter =B21-\$B\$6 and copy across

PV(Actual Discount Rate / Period,  
Number of Periods to Maturity,  
Coupon Payment, Face Value)  
Enter =-PV(B22,\$B\$8,\$B\$13,\$B\$9)  
and copy across

/(Current Discount Rate / Period,  
Number of Periods to Maturity,  
Coupon Payment, Face Value)  
Enter =-PV(\$B\$12,\$B\$8,\$B\$13,\$B\$9)  
and copy across

ified Duration  
ange in YTM  
=-B27\*B23  
copy across

$$+r)^2)$$

$$+1$$

7.00%	7.50%	8.00%	8.50%	9.00%	9.50%	10.00%
3.5%	3.8%	4.0%	4.3%	4.5%	4.8%	5.0%
5.3%	5.8%	6.3%	6.8%	7.3%	7.8%	8.3%
\$863	\$847	\$832	\$817	\$802	\$788	\$774
\$1,048	\$1,048	\$1,048	\$1,048	\$1,048	\$1,048	\$1,048
-17.7%	-19.2%	-20.7%	-22.1%	-23.5%	-24.9%	-26.2%
3.77	3.77	3.77	3.77	3.77	3.77	3.77
-19.8%	-21.7%	-23.6%	-25.5%	-27.4%	-29.3%	-31.2%
18.41	18.41	18.41	18.41	18.41	18.41	18.41
-17.3%	-18.7%	-20.0%	-21.3%	-22.5%	-23.7%	-24.9%



# BOND PRICING

# Immunization

## Inputs

Rate Convention

☐ EAR ☒ APR

2

Annual Percentage Rate

Yield to Maturity (Annualized)

1.74%

Number of Payments / Year

2

	Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
Bond 1	1.50%	4	\$1,000	1,783
Bond 2	2.00%	8	\$1,000	2,042
Bond 3	0.90%	2	\$1,000	0
Bond 4	1.50%	4	\$1,000	0
Bond 5	1.90%	6	\$1,000	0
Bond 6	2.30%	8	\$1,000	0
Bond 7	1.90%	6	\$1,000	0
Bond 8	2.30%	8	\$1,000	0

## Outputs

Discount Rate / Period (r)

0.9%

## Bond Present Value, Duration, and Convexity using a Timeline

Period	0	1	2	3
Time (Years)	0.0	0.5	1.0	1.5
Liabilities		\$0	\$0	\$0
Present Value of Liabilities		\$0	\$0	\$0
Total Present Value of Liabilities	\$3,797,413			
Weight		0.0%	0.0%	0.0%
Weight * Time		0.00	0.00	0.00
Duration of Liabilities	3.00			
Modified Duration of Liabilities	2.97			
Weight * (Time^2+Time)		0.00	0.00	0.00
Convexity of Liabilities	11.79			

## Assets

Bond 1	\$13,371	\$13,371	\$13,371
Bond 2	\$15,313	\$15,313	\$15,313
Bond 3	\$0	\$0	\$0
Bond 4	\$0	\$0	\$0
Bond 5	\$0	\$0	\$0
Bond 6	\$0	\$0	\$0
Bond 7	\$0	\$0	\$0
Bond 8	\$0	\$0	\$0
Total Assets	\$28,685	\$28,685	\$28,685
Present Value of Assets	\$28,437	\$28,192	\$27,949
Total Present Value of Assets	\$3,797,413		
Weight	0.7%	0.7%	0.7%
Weight * Time	0.00	0.01	0.01
Duration of Assets	2.97		
Modified Duration of Assets	2.93		
Weight * (Time^2+Time)	0.01	0.01	0.03

(3) Copy the Present Value & Duration  
Copy the range B19:J24 from the

(5) (Sum of Weight \* (Time ^ 2 + Time))  
/ ((1 + Yield to Maturity / Number of Payments)  
Enter =SUM(C30:J30)/((1+B18)^2)

## Differences

Total Assets - Liabilities

PV of Assets - PV of Liabilities

Duration of Assets - Duration of Liab

Convexity of Assets - Convexity of Liab

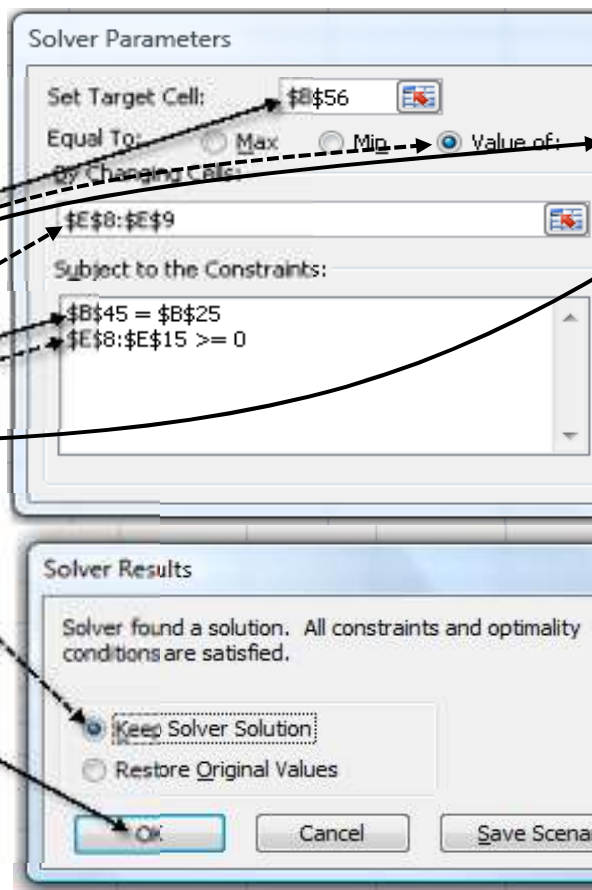
(6) Copy the Present Value,  
Copy the range B24:J31

(7) Total Assets - Liabilities  
Enter =C43-C23 and copy

(8) Compute the differences between Assets &  
Enter =B45-B25 in B55, =B48-B28 in B56,

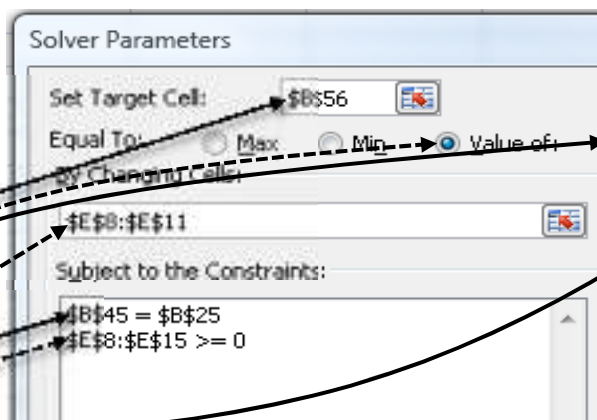
To solve the first problem  
when there is a single liability to immunize

(9a) Use Solver to determine the number of both Treasury bonds.  
 \* Click on **Data | Analysis | Solver**  
 \* enter B56 in Set Target Cell  
 \* click on the **Value Of** button  
 \* enter 0 in the adjacent box,  
 \* enter E8:E9 in By Changing Cells,  
 \* click on **Add** and enter B45 = B25,  
 \* click **Add** and enter E8:E15 >=0  
 \* and click on **Solve**  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution** button  
 \* and click on **OK**

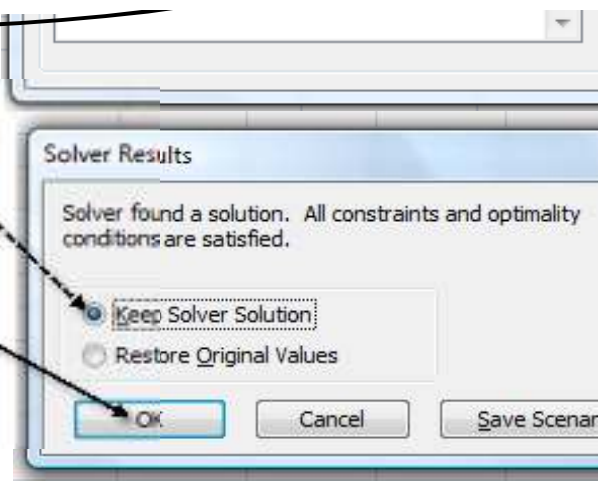


To solve the second problem  
when there is a series of liabilities to immunize

(9b) Use Solver to determine the number of all four Treasury bonds.  
 \* Click on **Data | Analysis | Solver**  
 \* enter B56 in Set Target Cell,  
 \* click on the **Value Of** button  
 \* enter 0 in the adjacent box,  
 \* enter E8:E11 in By Changing Cells,  
 \* click on **Add** and enter B45 = B25,  
 \* click **Add** and enter E8:E15 >=0

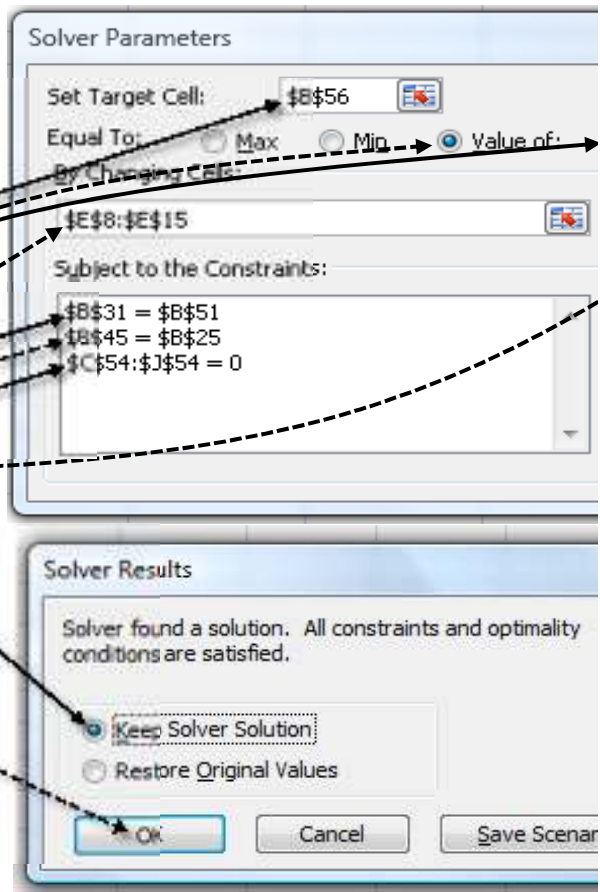


\* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



To solve the third problem  
 when there is a series of liabilities to immunize  
 with cash flow matching

(9c) Use Solver to determine the  
 number of all four Treasury bonds.  
 \* Click on **Data | Analysis | Solver**  
 \* enter **B56** in Set Target Cell,  
 \* click on the **Value Of** button  
 \* enter **0** in the adjacent box,  
 \* enter **E8:E15** in By Changing Cells,  
 \* click on **Add** and enter **B45 = B25**,  
 \* click **Add** and enter **E8:E15 >= 0**,  
 \* click **Add** and enter **C54:J54 = 0**  
 \* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



Currency: US Dollar

Exch Rate  
\$1.00 = \$1.00

Coupon  
Payment (PMT)

\$8  
\$10  
\$5  
\$8  
\$10  
\$12  
\$10  
\$12

(1) Coupon Rate \* Face Value / (Number of Payments / Year)  
Enter =B8\*D8/\$B\$6 and copy down

(2) If Rate Convention = EAR,  
Then  $(1 + \text{Yield To Maturity})^{(1 / (\text{Number of Payments / Year}))} - 1$   
Else  $(\text{Yield To Maturity}) / \text{Number of Payment / Year}$   
Enter =IF(C4=1,((1+B5)^(1/B6))-1,B5/B6)

on formulas from the Duration and Convexity sheet  
Duration and Convexity sheet to B24

4	5	6	7	8
2.0	2.5	3.0	3.5	4.0
\$0	\$0	\$4,000,000	\$0	\$0
\$0	\$0	\$3,797,413	\$0	\$0
0.0%	0.0%	100.0%	0.0%	0.0%
0.00	0.00	3.00	0.00	0.00

0.00 0.00 12.00 0.00 0.00

ents) ^ 2)

(4) Weight \* (Time^2 + Time)  
Enter =C26\*(C22^2+C22) and copy across

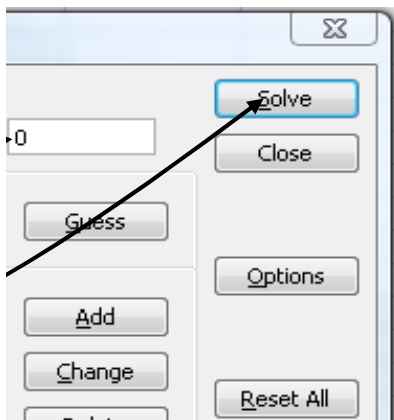
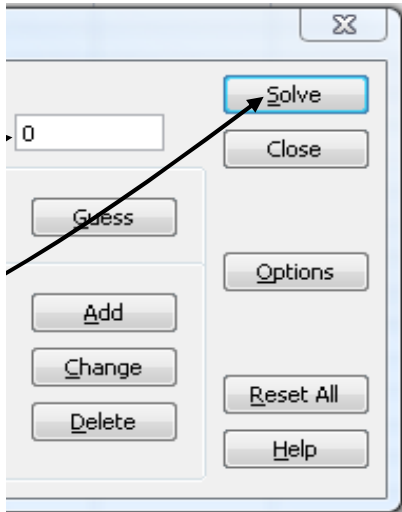
\$1,796,227	\$0	\$0	\$0	\$0
\$15,313	\$15,313	\$15,313	\$15,313	\$2,057,101
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$1,811,540	\$15,313	\$15,313	\$15,313	\$2,057,101
\$1,749,846	\$14,664	\$14,538	\$14,412	\$1,919,374
46.1%	0.4%	0.4%	0.4%	50.5%
0.92	0.01	0.01	0.01	2.02
2.76	0.03	0.05	0.06	10.11

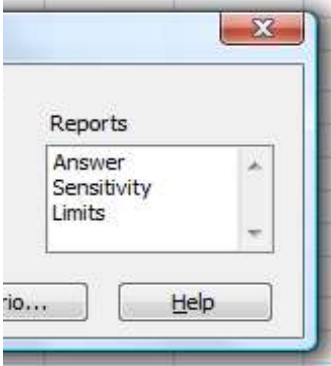
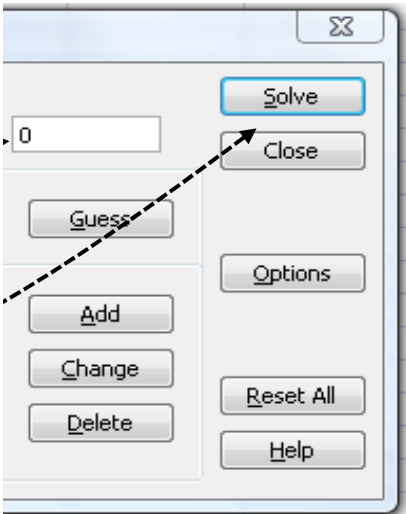
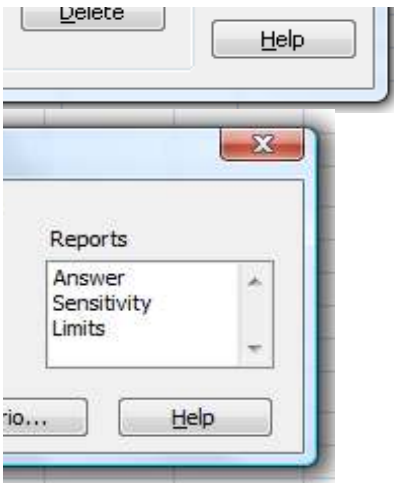
Duration, and Convexity formulas from above  
to B44

\$1,811,540	\$15,313	(\$3,984,687)	\$15,313	\$2,057,101
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by across

and Liabilities in Present Value, Duration, and Convexity  
and =B51-B31 in B57





Currency Number 4  
 (Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
1.50%	4	\$1,000	1,783
2.00%	8	\$1,000	2,042
0.90%	2	\$1,000	6,038
1.50%	4	\$1,000	5,937
1.90%	6	\$1,000	7,017
2.30%	8	\$1,000	8,068

0	1	2	3
0.0	0.5	1.0	1.5
	\$0	\$0	\$0
	\$2,000,000	\$2,200,000	\$2,500,000





Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
0.00%	1	\$1,000	2,000
0.00%	2	\$1,000	2,200
0.00%	3	\$1,000	2,500
0.00%	4	\$1,000	3,200
0.00%	5	\$1,000	3,700
0.00%	6	\$1,000	4,300
0.00%	7	\$1,000	4,700
0.00%	8	\$1,000	5,100

4 2.0	5 2.5	6 3.0	7 3.5	8 4.0
\$0	\$0	\$4,000,000	\$0	\$0
\$3,200,000	\$3,700,000	\$4,300,000	\$4,700,000	\$5,100,000





	A	B	C	D	E	F	G	H	I	J
1	<b>BOND PRICING</b>	<b>System of Five Bond Variables</b>					Currency: US Dollar	Exch Rate \$1.00 =	\$1.00	
2										
3	<b>Inputs</b>	<b>Annual Percentage Rate</b>								
4	Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2							
5	Annual Coupon Rate	4.00%								
6	Yield to Maturity (Annualized)	1.74%								
7	Number of Payments / Year	2								
8	(1) Number of Periods to Maturity (T)	11								
9	(2) Face Value (PAR)	\$1,000								
10	(3) Discount Rate / Period (r)	0.87%								
11	(4) Coupon Payment (PMT)	\$20.00								
12	(5) Bond Price (P)	\$1,086.66								
13										
14	(1) Number of Periods to Maturity (T) from the other four variables									
15	Number of Periods to Maturity using NPER Function	11								
16										
17	(2) Face Value (PAR) from the other four variables									
18	Face Value using the FV Function	\$1,000.00								
19	Face Value using the Formula	\$1,000.00								
20										
21	(3) Discount Rate / Period (r) from the other four variables									
22	Discount Rate / Period using the RATE Function	0.8714%								
23										
24	(4) Coupon Payment (PMT) from the other four variables									
25	Coupon Payment using the PMT Function	\$20.00								
26	Coupon Payment using the Formula	\$20.00								
27										
28	(5) Bond Price (P) from the other four variables									
29	Bond Price using the PV Function	\$1,086.66								
30	Bond Price using the Formula	\$1,086.66								
31										
32										
33										
34	(5) The Bond Price Formula is									
35	$P = \frac{PMT \cdot \left(1 - (1+r)^{-T}\right)}{r} + \frac{PAR}{(1+r)^T}$									
36	Enter =B11*(1-(1+B10^(-B8)))/B10 + B10/(1+B10^B8)									
37										
38										
39										
40										
41										
42										

(1) NPER(Discount Rate / Period, Coupon Payment, -Bond Price, Face Value)  
Enter =NPER(B10,B11,B12,B9)

(2) FV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price)  
Enter =FV(B10,B11,B11,B12)

(3) The Face Value Formula is  
$$PAR = P \cdot (1+r)^T - \frac{PMT \cdot \left( \left( (1+r)^T \right) - 1 \right)}{r}$$
  
Enter =B12\*(1+B10^B11)-B11\*(1+B10^B11-1)/B10

(4) RATE(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price, Face Value)  
Enter =RATE(B10,B11,B12,B9)

(5) PMT(Discount Rate / Period, Number of Periods to Maturity, Bond Price, Face Value)  
Enter =PMT(B10,B8,B12,B9)

(6) The Coupon Payment Formula is  
$$PMT = \frac{P - PAR / (1+r)^T}{\left( 1 - (1+r)^{-T} \right) / r}$$
  
Enter =B12-B9/(1+B10^B11)-B10/(1+B10^B11-1)/B10

(7) PV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, Face Value)  
Enter =PV(B10,B11,B11,B9)

	A	B	C	D	E	F	G	H	I	J
1	<b>BOND PRICING</b>	<b>Annual Payments</b>								
2										
3										
4										
5										
6										
7	<b>Inputs</b>									
8	Number of Periods to Maturity (T)	8	8							
9	Face Value (PAR)	\$1,000	20							
10										
11										
12	Discount Rate / Period (r)	4.37%	8							
13	Coupon Payment (PMT)	\$12.00	2							
14										
15	<b>Bond Price using a Timeline</b>									
16	Period	0	1	2	3	4	5	6	7	8
17										
18	Cash Flows		\$12.00	\$12.00	\$12.00	\$12.00	\$12.00	\$12.00	\$12.00	\$1,012.00
19	Present Value of Cash Flows		\$11.50	\$11.02	\$10.55	\$10.11	\$9.69	\$9.28	\$8.90	\$718.75
20	Bond Price	\$789.60								
21										
22	<b>Bond Price using the Formula</b>									
23	Bond Price (P)	\$789.60								
24										
25	<b>Bond Price using the PV Function</b>									
26	Bond Price	\$789.60								
27										
28										
29										
30										
31										
32										
33										
34										
35										
36										

1. Input Payment  
Enter =PMT and copy across cells

2. Input Payment = Face Value  
Enter =1000

3. (Cash Flow + PV of Cash Flow + PV of Face Value)  
Enter =11.50+11.02+10.55+10.11+9.69+9.28+8.90

4. Input the Period of Value of Cash Flow  
Enter =1,1,2,3,4,5,6,7,8

5. Use the Bond Price Formula

$$P = \frac{PMT \cdot \left(1 - \left((1+r)^{-T}\right)\right)}{r} + \frac{PAR}{(1+r)^T}$$

Enter = 12\* (1-(1+0.0437)^-8)/0.0437 + 1000/(1+0.0437)^8

[illegible]



# BOND PRICING

# Duration and Convexity

Currency:

## Inputs

Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2	Annual Percentage Rate
Annual Coupon Rate	3.20%	6	
Yield to Maturity (Annualized)	2.53%	5	
Number of Payments / Year	2	2	
Number of Periods to Maturity (T)	8	8	
Face Value (PAR)	\$1,000	20	

## Outputs

Discount Rate / Period (r)	1.3%
Coupon Payment (PMT)	\$16

## Bond Duration using a Timeline

Period	0	1	2	3	4	5
Time (Years)	0.0	0.5	1.0	1.5	2.0	2.5
Cash Flows		\$16.00	\$16.00	\$16.00	\$16.00	\$16.00
Present Value of Cash Flows		\$15.80	\$15.60	\$15.41	\$15.22	\$15.03
Bond Price using a Timeline	\$1,025.34					
Weight		1.5%	1.5%	1.5%	1.5%	1.5%
Weight * Time		0.01	0.02	0.02	0.03	0.04
Duration using a Timeline	3.79					
Modified Duration using a Timeline	3.74					

## Bond Duration using a Formula

Duration (D) using a Formula	3.79
Modified Duration using a Formula	3.74

## Bond Duration using a Function (under APR)

Duration using a Function	3.79
Modified Duration using a Function	3.74

(7) DURATION (Settlement Date, Maturity Date, Annual Coupon Rate, Yield to Maturity, Number of Periods)  
Enter =IF(\$C\$4=1,"",DURATION(DATE(2000,1,1), DATE(2000+B8/B7,1,1),B5,B6,B7))

(8) MDURATION (Settlement Date, Maturity Date, Annual Coupon Rate, Yield to Maturity, Number of Periods)  
Enter =IF(\$C\$4=1,"",MDURATION(DATE(2000,1,1), DATE(2000+B8/B7,1,1),B5,B6,B7))

(2) PV of Cash Flow on Date t / Total  
Enter =C19/\$B\$20 and copy across

(3) Weight \* Time  
Enter =C21\*C17 and copy across

(4) Sum of all the Weight \* Times  
Enter =SUM(C22:J22)

(5) Duration / (1+(Discount Rate / Period)  
Enter =B23/(1+\$B\$12) and copy across

(6) The Duration Formula is:  

$$D = \frac{1+r}{r \cdot NOP} - \frac{1+r+T \cdot (CR \cdot ((1+r)^T - 1))}{CR \cdot ((1+r)^T - 1)}$$
 Enter =(1+B12)/(B12\*B7)-(1+B12)/(B5\*((1+B12)^B8-1)+B12\*B7)

## Bond Convexity

Weight * (Time^2+Time)	0.01	0.03	0.06	0.09	0.13
Convexity using a Timeline	18.17				
Convexity using a Formula	18.17				

(9) Weight \* (Time^2 + Time)  
Enter =C21\*(C17^2+C17) and copy across

(10) (Sum of Weight \* (Time ^ 2 + Time) / ((1 + Yield to Maturity / Number of Periods)  
Enter =SUM(C43:J43)/((1+B6/B7)^B8)

(11) The Convexity Formula is:

$$\frac{\left( CR \cdot (1+r)^{1+T} \cdot (r \cdot (NOP+1) + 2) \right.}{r^2 \cdot NOP^2 \cdot \left( CR \cdot (1+r)^T - CR + r \cdot NOP \right)}$$

Enter =((B5\*((1+B12)^(1+B8))\*(B12\*(B7+1)+2)-B5\*(B12^2\*(B7+B8+1)\*(B8+1)+B12\*(B7+2\*B8+3)-

/((B12^2\*B7^2\*(B5\*(1+B12)^B8-B5+B12\*B7)))/((1+B12)^2))

US Dollar      Exch Rate  
\$1.00 = \$1.00

Currency Number 4  
(Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

previous sheet  
ious sheet to B12

6	7	8
3.0	3.5	4.0
\$16.00	\$16.00	\$1,016.00
\$14.84	\$14.65	\$918.80
1.4%	1.4%	89.6%
0.04	0.05	3.58

al PV of all Cash Flows  
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$$\frac{1}{NOP - r}$$
  

$$1) + r \cdot NOP$$
  

$$+ B8 * (B5 / B7 - B12))$$
  

$$B7)$$

0.17      0.23      17.92

opy across

ime))  
r of Payments) ^ 2)  
)^2)

$$\frac{)}{\div ((1+r)^2)}$$

$$+2)+B12^3*B7*B8*(B7+B8))$$

# BOND PRICING

# Duration and Convexity

Currency:

## Inputs

Rate Convention	<input checked="" type="radio"/> EAR <input type="radio"/> APR	1	Effective Annual Rate
Annual Coupon Rate	3.20%	6	
Yield to Maturity (Annualized)	2.53%	5	
Number of Payments / Year	2	2	
Number of Periods to Maturity (T)	8	8	
Face Value (PAR)	\$1,000	20	

## Outputs

Discount Rate / Period (r)	1.3%
Coupon Payment (PMT)	\$16

## Bond Duration using a Timeline

Period	0	1	2	3	4	5
Time (Years)	0.0	0.5	1.0	1.5	2.0	2.5
Cash Flows		\$16.00	\$16.00	\$16.00	\$16.00	\$16.00
Present Value of Cash Flows		\$15.80	\$15.61	\$15.41	\$15.22	\$15.03
Bond Price using a Timeline	\$1,025.94					
Weight		1.5%	1.5%	1.5%	1.5%	1.5%
Weight * Time		0.01	0.02	0.02	0.03	0.04
Duration using a Timeline	3.79					
Modified Duration using a Timeline	3.74					

## Bond Duration using a Formula

Duration (D) using a Formula	3.79
Modified Duration using a Formula	3.74

## Bond Duration using a Function (under APR)

Duration using a Function	
Modified Duration using a Function	

(7) DURATION (Settlement Date, Maturity Date, Annual Coupon Rate, Yield to Maturity, Number of Periods)  
Enter =IF(\$C\$4=1,"",DURATION(DATE(2000,1,1), DATE(2000+B8/B7,1,1),B5,B6,B7))

(8) MDURATION (Settlement Date, Maturity Date, Annual Coupon Rate, Yield to Maturity, Number of Periods)  
Enter =IF(\$C\$4=1,"",MDURATION(DATE(2000,1,1), DATE(2000+B8/B7,1,1),B5,B6,B7))

(2) PV of Cash Flow on Date t / Total  
Enter =C19/\$B\$20 and copy across

(3) Weight \* Time  
Enter =C21\*C17 and copy across

(4) Sum of all the Weight \* Times  
Enter =SUM(C22:J22)

(5) Duration / (1+(Discount Rate / Period)  
Enter =B23/(1+\$B\$12) and copy across

(6) The Duration Formula is:  

$$D = \frac{1+r}{r \cdot NOP} - \frac{1+r+T \cdot (CR)}{CR \cdot ((1+r)^T - 1)}$$
 Enter =(1+B12)/(B12\*B7)-(1+B12)/(B5\*((1+B12)^B8-1)+B12\*B7)

## Bond Convexity

Weight * (Time^2+Time)	0.01	0.03	0.06	0.09	0.13
Convexity using a Timeline	18.17				
Convexity using a Formula	18.18				

(9) Weight \* (Time^2 + Time)  
Enter =C21\*(C17^2+C17) and copy across

(10) (Sum of Weight \* (Time ^ 2 + Time) / ((1 + Yield to Maturity / Number of Periods)^Time - 1))  
Enter =SUM(C43:J43)/((1+B6/B7)^B8-1)

(11) The Convexity Formula is:

$$\frac{\left( CR \cdot (1+r)^{1+T} \cdot (r \cdot (NOP+1) + 2) \right.}{r^2 \cdot NOP^2 \cdot \left( CR \cdot (1+r)^T - CR + r \cdot NOP \right)}$$

Enter =((B5\*((1+B12)^(1+B8))\*(B12\*(B7+1)+2)-B5\*(B12^2\*(B7+B8+1)\*(B8+1)+B12\*(B7+2\*B8+3)-

/((B12^2\*B7^2\*(B5\*(1+B12)^B8-B5+B12\*B7)))/((1+B12)^2))

US Dollar      Exch Rate  
\$1.00 = \$1.00

Currency Number 4  
(Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

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6	7	8
3.0	3.5	4.0
\$16.00	\$16.00	\$1,016.00
\$14.84	\$14.66	\$919.37
1.4%	1.4%	89.6%
0.04	0.05	3.58

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$$\frac{1}{NOP - r}$$
  

$$1) + r \cdot NOP$$
  

$$+ B8 * (B5 / B7 - B12))$$
  

$$B7)$$

0.17      0.23      17.92

opy across

ime))  
r of Payments) ^ 2)  
)^2)

$$\frac{)}{\div ((1+r)^2)}$$

$$+2)+B12^3*B7*B8*(B7+B8))$$

# BOND PRICING

# Price Sensitivity

## Inputs

Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2
Annual Coupon Rate (CR)	5.80%	11
Yield to Maturity (Annualized)	4.29%	8
Number of Payments / Year (NOP)	2	2
Number of Periods to Maturity (T)	8	8
Face Value	\$1,000	20

## Outputs

Discount Rate / Period (r)	2.1%
Coupon Payment	\$29

(1) If Rate Convention = EAR,  
Then  $(1 + \text{Yield To Maturity})^{(1 / (\text{Number of Payments / Year})) - 1}$   
Else  $(\text{Yield To Maturity} / \text{Number of Payment / Year})$   
Enter =IF(\$C\$4=1,((1+B21)^(1/\$B\$7))-1,B21/\$B\$7)  
and copy across

## Chart Outputs

Yield to Maturity (Annualized)	0.50%	1.00%	1.50%	2.00%	2.50%
Discount Rate / Period	0.3%	0.5%	0.8%	1.0%	1.3%
Change in Yield to Maturity	-3.8%	-3.3%	-2.8%	-2.3%	-1.8%
Actual Bond Price	\$1,210	\$1,188	\$1,166	\$1,145	\$1,125
Current Bond Price	\$1,055	\$1,055	\$1,055	\$1,055	\$1,055
Actual Percent Change in Price	14.7%	12.6%	10.6%	8.6%	6.6%
Modified Duration	3.56	3.56	3.56	3.56	3.56
Duration Approximation	13.5%	11.7%	9.9%	8.2%	6.4%
Convexity	16.93	16.93	16.93	16.93	16.93
Duration and Convexity Approx.	14.7%	12.6%	10.6%	8.6%	6.6%

(5)  $(\text{Actual Bond Price} - \text{Current Bond Price}) / \text{Current Bond Price}$   
Enter =(B24-B25)/B25  
and copy across

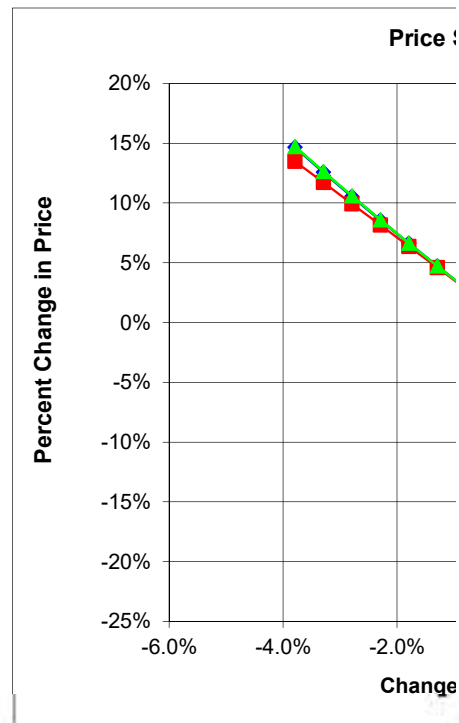
(6) The Modified Duration Formula is:

$$D^* = \left( \frac{1+r}{r \cdot NOP} - \frac{1+r+T \cdot (CR / NOP - r)}{CR \cdot ((1+r)^T - 1) + r \cdot NOP} \right) \div (1+r)$$

Enter =((1+\$B\$12)/(\$B\$12\*\$B\$7) - (1+\$B\$12+\$B\$8\*(\$B\$5/\$B\$7-\$B\$12)) / (\$B\$5\*((1+\$B\$12)^\$B\$8-1)+\$B\$12\*\$B\$7))/(1+\$B\$12)  
and copy across

(9) Duration Approximation  
+ (1/2) \* Convexity \* (Change in YTM)^2  
Enter =B28+(1/2)\*B29\*B23^2 and copy across

(8) The Convexity Formula is:



(8) The Convexity Formula is:

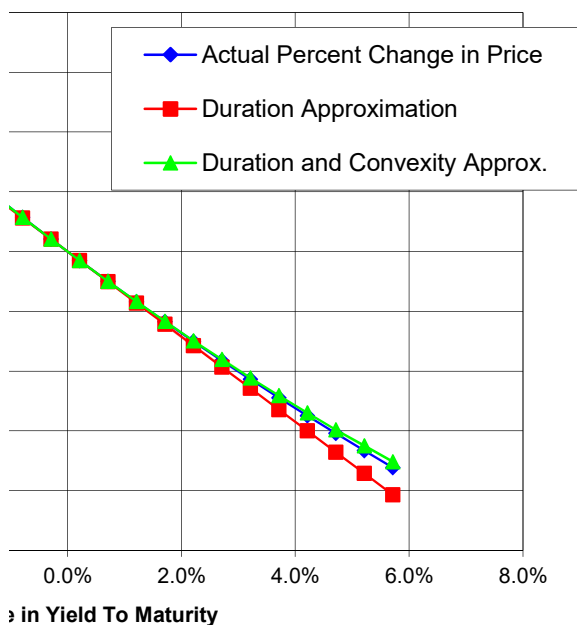
(b) The Convexity Formula is:

$$\frac{\left( CR \cdot (1+r)^{1+T} \cdot (r \cdot (NOP+1) + 2) - CR \cdot (r^2 \cdot (NOP+T+1) \cdot (T+1) + r \cdot (NOP+2 \cdot T+3) + 2) + r^3 \cdot NOP \cdot T \cdot (NOP+T) \right)}{r^2 \cdot NOP^2 \cdot \left( CR \cdot (1+r)^T - CR + r \cdot NOP \right)} \div \left( (1+r)^2 \right)$$

Enter =((B5\*((1+B12)^(1+B8))\*(B12\*(B7+1)+2)-B5\*(B12^2\*(B7+B8+1)\*(B8+B12\*(B7+2\*B8+3)+2)+B12^3\*B7\*B8\*(B7+B8)))/(B12^2\*B7^2\*(B5\*(1+B12)^B8-B5+B12\*B7)))/((1+B12)^2) and copy across

Currency: US Dollar      Exch Rate  
\$1.00 = \$1.00

### Sensitivity



Currency Number **4**  
(Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

3.00%	3.50%	4.00%	4.50%	5.00%	5.50%	6.00%	6.50%
1.5%	1.8%	2.0%	2.3%	2.5%	2.8%	3.0%	3.3%
-1.3%	-0.8%	-0.3%	0.2%	0.7%	1.2%	1.7%	2.2%
\$1,105	\$1,085	\$1,066	\$1,047	\$1,029	\$1,011	\$993	\$976
\$1,055	\$1,055	\$1,055	\$1,055	\$1,055	\$1,055	\$1,055	\$1,055
4.7%	2.9%	1.0%	-0.7%	-2.5%	-4.2%	-5.9%	-7.5%
3.56	3.56	3.56	3.56	3.56	3.56	3.56	3.56
4.6%	2.8%	1.0%	-0.7%	-2.5%	-4.3%	-6.1%	-7.9%
16.93	16.93	16.93	16.93	16.93	16.93	16.93	16.93
4.7%	2.9%	1.0%	-0.7%	-2.5%	-4.2%	-5.8%	-7.5%

(2) New YTM - Current YTM  
Enter =B21-\$B\$6 and copy across

PV(Absolute Discount Rate / Period,  
Number of Periods to Maturity,  
Coupon Payment, Face Value)  
Enter =-PV(B22,\$B\$8,\$B\$13,\$B\$9)  
and copy across

/(Current Discount Rate / Period,  
Number of Periods to Maturity,  
Coupon Payment, Face Value)  
Enter =-PV(\$B\$12,\$B\$8,\$B\$13,\$B\$9)  
and copy across

Modified Duration  
Change in YTM  
=B27\*B23  
copy across

$$+r)^2)$$

$$+1$$

7.00%	7.50%	8.00%	8.50%	9.00%	9.50%	10.00%
3.5%	3.8%	4.0%	4.3%	4.5%	4.8%	5.0%
2.7%	3.2%	3.7%	4.2%	4.7%	5.2%	5.7%
\$959	\$942	\$926	\$910	\$894	\$879	\$864
\$1,055	\$1,055	\$1,055	\$1,055	\$1,055	\$1,055	\$1,055
-9.1%	-10.7%	-12.2%	-13.7%	-15.2%	-16.7%	-18.1%
3.56	3.56	3.56	3.56	3.56	3.56	3.56
-9.7%	-11.4%	-13.2%	-15.0%	-16.8%	-18.6%	-20.3%
16.93	16.93	16.93	16.93	16.93	16.93	16.93
-9.0%	-10.6%	-12.1%	-13.5%	-14.9%	-16.3%	-17.6%



# BOND PRICING

# Immunization

## Inputs

Rate Convention

☐ EAR ☒ APR

2

Annual Percentage Rate

Yield to Maturity (Annualized)

3.17%

Number of Payments / Year

2

	Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
Bond 1	3.25%	4	\$1,000	2,838
Bond 2	4.25%	8	\$1,000	3,789
Bond 3	0.90%	2	\$1,000	0
Bond 4	1.50%	4	\$1,000	0
Bond 5	1.90%	6	\$1,000	0
Bond 6	2.30%	8	\$1,000	0
Bond 7	1.90%	6	\$1,000	0
Bond 8	2.30%	8	\$1,000	0

## Outputs

Discount Rate / Period (r)

1.6%

## Bond Present Value, Duration, and Convexity using a Timeline

Period	0	1	2	3
Time (Years)	0.0	0.5	1.0	1.5
Liabilities		\$0	\$0	\$0
Present Value of Liabilities		\$0	\$0	\$0
Total Present Value of Liabilities	\$6,642,711			
Weight		0.0%	0.0%	0.0%
Weight * Time		0.00	0.00	0.00
Duration of Liabilities	3.00			
Modified Duration of Liabilities	2.95			
Weight * (Time^2+Time)		0.00	0.00	0.00
Convexity of Liabilities	11.63			

## Assets

Bond 1	\$46,123	\$46,123	\$46,123
Bond 2	\$61,567	\$61,567	\$61,567
Bond 3	\$0	\$0	\$0
Bond 4	\$0	\$0	\$0
Bond 5	\$0	\$0	\$0
Bond 6	\$0	\$0	\$0
Bond 7	\$0	\$0	\$0
Bond 8	\$0	\$0	\$0
Total Assets	\$107,689	\$107,689	\$107,689
Present Value of Assets	\$106,309	\$104,355	\$102,727
Total Present Value of Assets	\$6,642,711		
Weight		1.6%	1.5%
Weight * Time		0.01	0.02
Duration of Assets	2.95		
Modified Duration of Assets	2.95		
Weight * (Time^2+Time)		0.03	0.06

## Differences

Total Assets - Liabilities

PV of Assets - PV of Liabilities

Duration of Assets - Duration of Liab

Convexity of Assets - Convexity of Liab

\$0  
0.00  
1.09

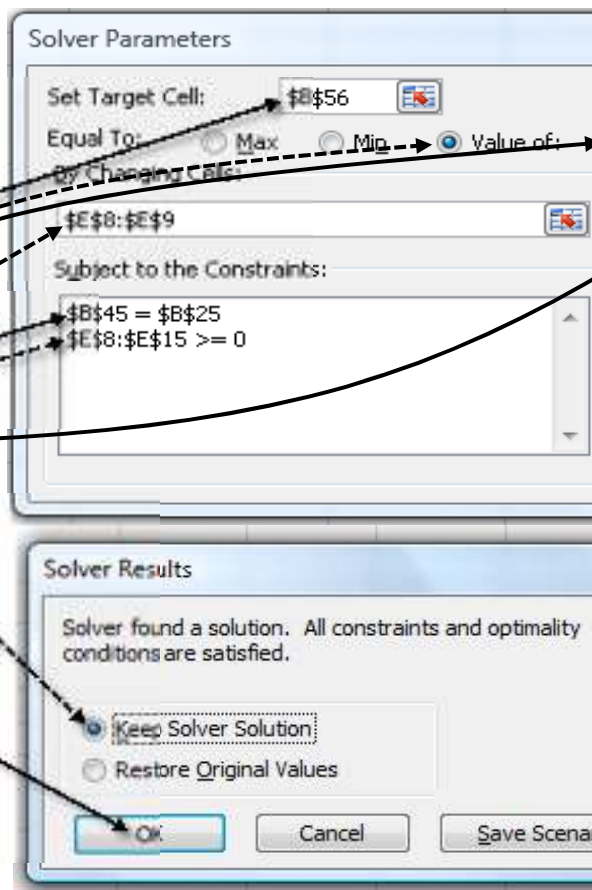
(6) Copy the Present Value,  
Copy the range B24:J31

(7) Total Assets - Liabilities  
Enter =C43-C23 and copy

(8) Compute the differences between Assets &  
Enter =B45-B25 in B55, =B48-B28 in B56,

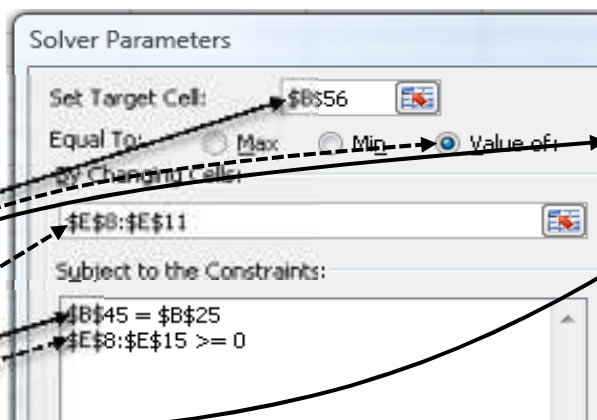
To solve the first problem  
when there is a single liability to immunize

- (9a) Use Solver to determine the number of both Treasury bonds.
- \* Click on **Data | Analysis | Solver**
  - \* enter B56 in Set Target Cell
  - \* click on the **Value Of** button
  - \* enter 0 in the adjacent box,
  - \* enter E8:E9 in By Changing Cells,
  - \* click on **Add** and enter B45 = B25,
  - \* click **Add** and enter E8:E15 >=0
  - \* and click on **Solve**
- When Solver finds a solution,
- \* click on the **Keep Solver Solution** button
  - \* and click on **OK**

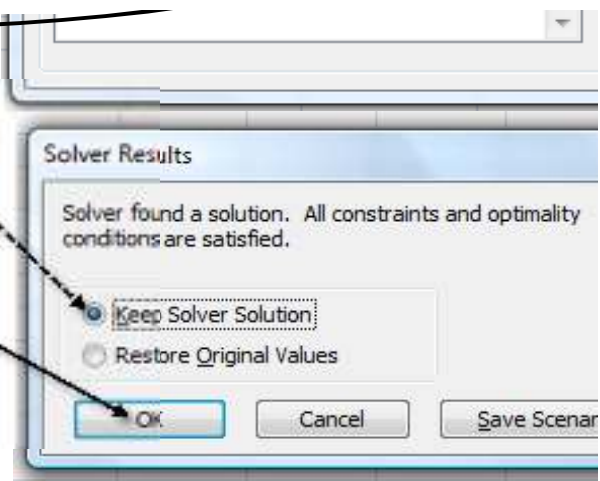


To solve the second problem  
when there is a series of liabilities to immunize

- (9b) Use Solver to determine the number of all four Treasury bonds.
- \* Click on **Data | Analysis | Solver**
  - \* enter B56 in Set Target Cell,
  - \* click on the **Value Of** button
  - \* enter 0 in the adjacent box,
  - \* enter E8:E11 in By Changing Cells,
  - \* click on **Add** and enter B45 = B25,
  - \* click **Add** and enter E8:E15 >=0

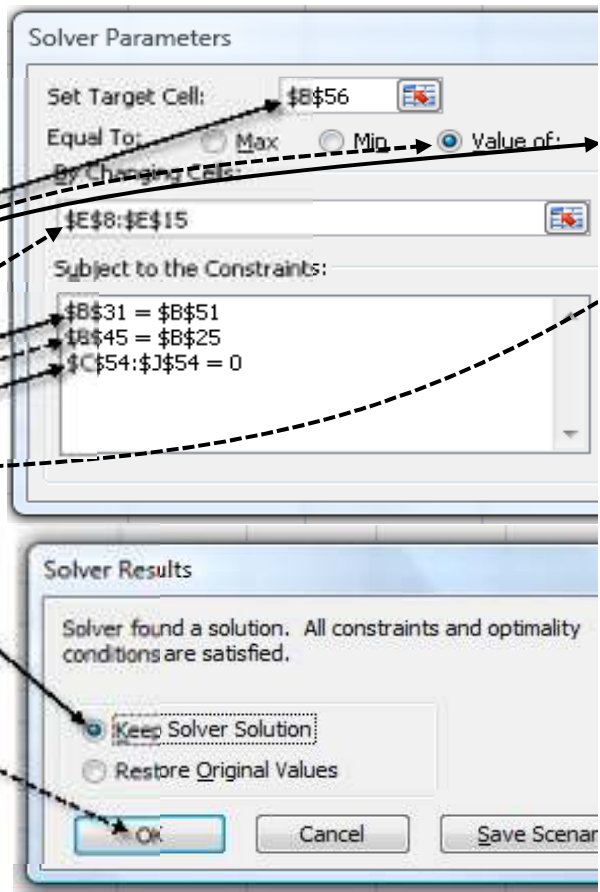


\* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



To solve the third problem  
 when there is a series of liabilities to immunize  
 with cash flow matching

(9c) Use Solver to determine the  
 number of all four Treasury bonds.  
 \* Click on **Data | Analysis | Solver**  
 \* enter **B56** in Set Target Cell,  
 \* click on the **Value Of** button  
 \* enter **0** in the adjacent box,  
 \* enter **E8:E15** in By Changing Cells,  
 \* click on **Add** and enter **B45 = B25**,  
 \* click **Add** and enter **E8:E15 >= 0**,  
 \* click **Add** and enter **C54:J54 = 0**  
 \* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



Currency: US Dollar

Exch Rate  
\$1.00 = \$1.00

Coupon  
Payment (PMT)

\$16  
\$21  
\$5  
\$8  
\$10  
\$12  
\$10  
\$12

(1) Coupon Rate \* Face Value / (Number of Payments / Year)  
Enter =B8\*D8/\$B\$6 and copy down

(2) If Rate Convention = EAR,  
Then  $(1 + \text{Yield To Maturity})^{(1 / (\text{Number of Payments / Year}))} - 1$   
Else  $(\text{Yield To Maturity}) / \text{Number of Payment / Year}$   
Enter =IF(C4=1,((1+B5)^(1/B6))-1,B5/B6)

on formulas from the Duration and Convexity sheet  
Duration and Convexity sheet to B24

4	5	6	7	8
2.0	2.5	3.0	3.5	4.0
\$0	\$0	\$7,300,000	\$0	\$0
\$0	\$0	\$6,642,711	\$0	\$0
0.0%	0.0%	100.0%	0.0%	0.0%
0.00	0.00	3.00	0.00	0.00

0.00 0.00 12.00 0.00 0.00

(4) Weight \* (Time^2 + Time)  
Enter =C26\*(C22^2+C22) and copy across

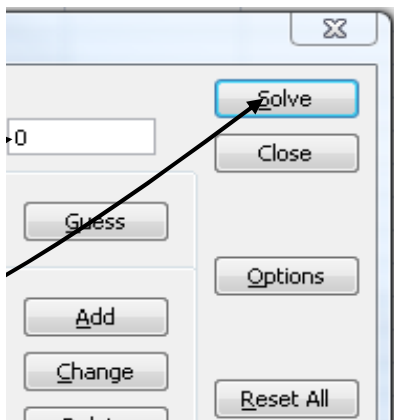
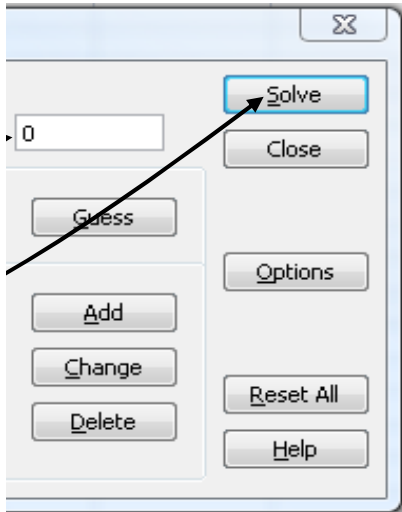
\$2,884,451	\$0	\$0	\$0	\$0
\$61,567	\$61,567	\$61,567	\$61,567	\$3,850,280
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$2,946,017	\$61,567	\$61,567	\$61,567	\$3,850,280
\$2,766,413	\$56,911	\$56,023	\$55,149	\$3,395,124
41.6%	0.9%	0.8%	0.8%	51.1%
0.83	0.02	0.03	0.03	2.04
2.50	0.07	0.10	0.13	10.22

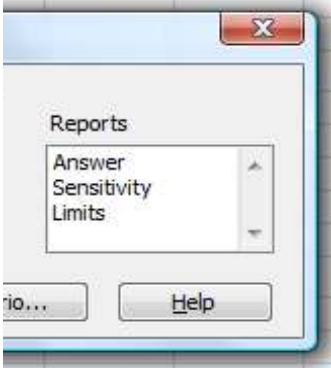
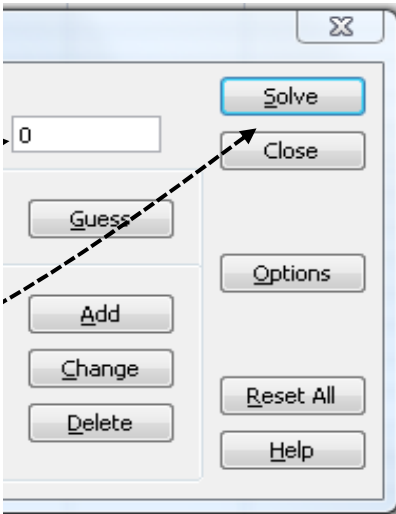
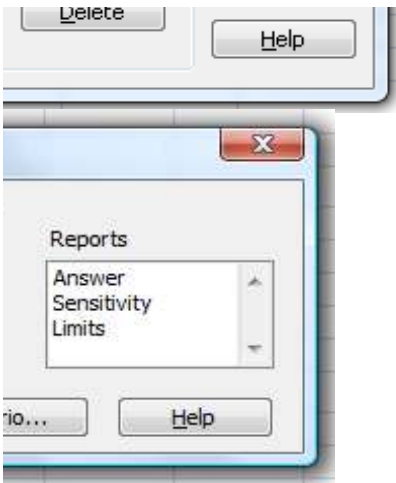
Duration, and Convexity formulas from above  
to B44

\$2,946,017	\$61,567	(\$7,238,433)	\$61,567	\$3,850,280
-------------	----------	---------------	----------	-------------

by across

and Liabilities in Present Value, Duration, and Convexity  
and =B51-B31 in B57





Currency Number 4  
 (Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
3.25%	4	\$1,000	1,783
4.25%	8	\$1,000	2,042
0.90%	2	\$1,000	6,038
1.50%	4	\$1,000	5,937
1.90%	6	\$1,000	7,017
2.30%	8	\$1,000	8,068

0	1	2	3
0.0	0.5	1.0	1.5
	\$0	\$0	\$0
	\$2,000,000	\$2,200,000	\$2,500,000





Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
0.00%	1	\$1,000	2,000
0.00%	2	\$1,000	2,200
0.00%	3	\$1,000	2,500
0.00%	4	\$1,000	3,200
0.00%	5	\$1,000	3,700
0.00%	6	\$1,000	4,300
0.00%	7	\$1,000	4,700
0.00%	8	\$1,000	5,100

4 2.0	5 2.5	6 3.0	7 3.5	8 4.0
\$0	\$0	\$4,000,000	\$0	\$0
\$3,200,000	\$3,700,000	\$4,300,000	\$4,700,000	\$5,100,000





# BOND PRICING

# Immunization

## Inputs

Rate Convention

☐ EAR ☒ APR

2

Annual Percentage Rate

Yield to Maturity (Annualized)

3.17%

Number of Payments / Year

2

	Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
Bond 1	1.50%	2	\$1,000	0
Bond 2	2.70%	4	\$1,000	34,996
Bond 3	2.90%	6	\$1,000	5,073
Bond 4	3.20%	8	\$1,000	10,046
Bond 5	1.90%	6	\$1,000	0
Bond 6	2.30%	8	\$1,000	0
Bond 7	1.90%	6	\$1,000	0
Bond 8	2.30%	8	\$1,000	0

## Outputs

Discount Rate / Period (r)

1.6%

## Bond Present Value, Duration, and Convexity using a Timeline

Period	0	1	2	3
Time (Years)	0.0	0.5	1.0	1.5
Liabilities		\$4,500,000	\$5,100,000	\$5,600,000
Present Value of Liabilities		\$4,429,788	\$4,942,094	\$5,341,943
Total Present Value of Liabilities	\$48,127,151			
Weight		9.2%	10.3%	11.1%
Weight * Time		0.05	0.10	0.17
Duration of Liabilities	2.44			
Modified Duration of Liabilities	2.40			
Weight * (Time^2+Time)		0.07	0.21	0.42
Convexity of Liabilities	9.37			

## Assets

Bond 1	\$0	\$0	\$0
Bond 2	\$262,469	\$262,469	\$262,469
Bond 3	\$38,044	\$38,044	\$38,044
Bond 4	\$75,346	\$75,346	\$75,346
Bond 5	\$0	\$0	\$0
Bond 6	\$0	\$0	\$0
Bond 7	\$0	\$0	\$0
Bond 8	\$0	\$0	\$0
Total Assets	\$375,859	\$375,859	\$375,859
Present Value of Assets	\$364,222	\$364,222	\$358,539
Total Present Value of Assets	\$48,124,385		
Weight		0.8%	0.7%
Weight * Time		0.01	0.01
Duration of Assets	2.43		
Modified Duration of Assets	2.41		
Weight * (Time^2+Time)		0.02	0.03

## Convexity of Assets

8.83

### Differences

Total Assets - Liabilities

PV of Assets - PV of Liabilities

Duration of Assets - Duration of Liab

Convexity of Assets - Convexity of Liab

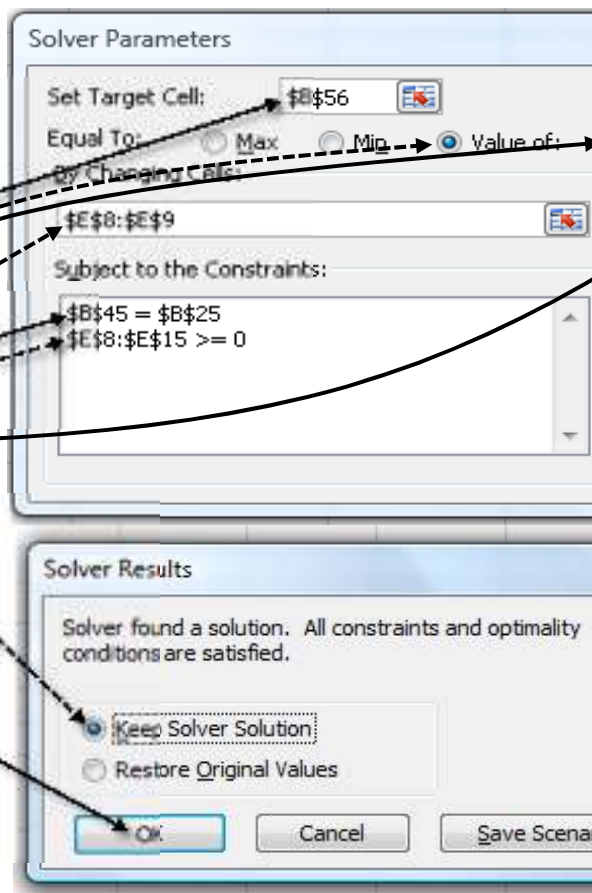
(6) Copy the Present Value, Copy the range B24:J31

(7) Total Assets - Liabilities  
Enter =C43-C23 and copy

(8) Compute the differences between Assets and Liabilities  
Enter =B45-B25 in B55, =B48-B28 in B56,

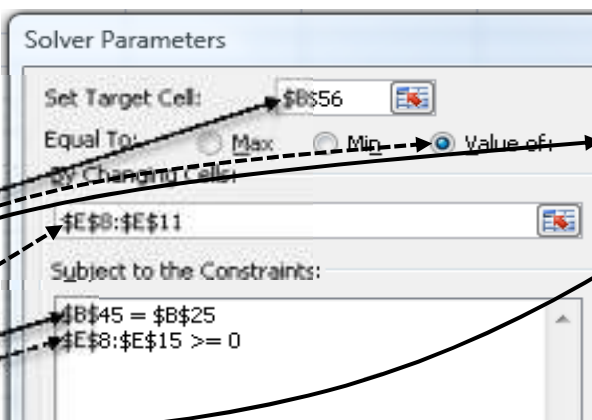
To solve the first problem  
when there is a single liability to immunize

- (9a) Use Solver to determine the number of both Treasury bonds.
- \* Click on **Data | Analysis | Solver**
  - \* enter B56 in Set Target Cell
  - \* click on the **Value Of** button
  - \* enter 0 in the adjacent box,
  - \* enter E8:E9 in By Changing Cells,
  - \* click on **Add** and enter B45 = B25,
  - \* click **Add** and enter E8:E15 >=0
  - \* and click on **Solve**
- When Solver finds a solution,
- \* click on the **Keep Solver Solution** button
  - \* and click on **OK**

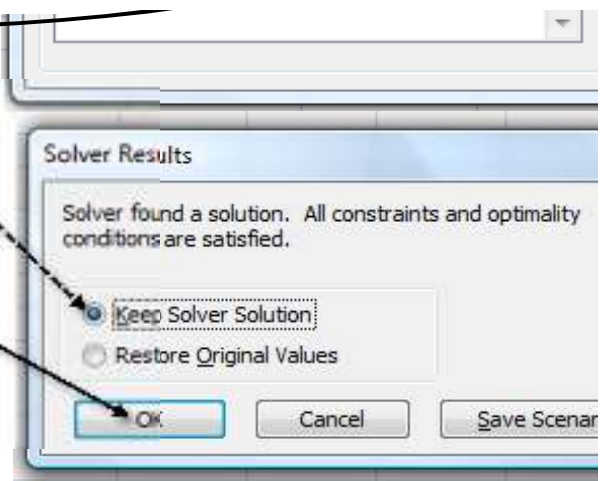


To solve the second problem  
when there is a series of liabilities to immunize

- (9b) Use Solver to determine the number of all four Treasury bonds.
- \* Click on **Data | Analysis | Solver**
  - \* enter B56 in Set Target Cell,
  - \* click on the **Value Of** button
  - \* enter 0 in the adjacent box,
  - \* enter E8:E11 in By Changing Cells,
  - \* click on **Add** and enter B45 = B25,
  - \* click **Add** and enter E8:E15 >=0

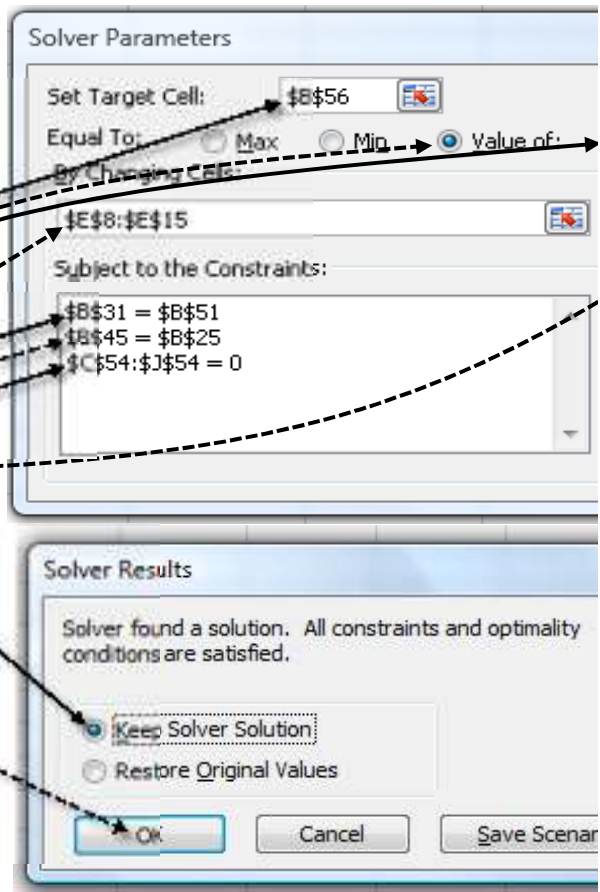


\* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



To solve the third problem  
 when there is a series of liabilities to immunize  
 with cash flow matching

(9c) Use Solver to determine the  
 number of all four Treasury bonds.  
 \* Click on **Data | Analysis | Solver**  
 \* enter **B56** in Set Target Cell,  
 \* click on the **Value Of** button  
 \* enter **0** in the adjacent box,  
 \* enter **E8:E15** in By Changing Cells,  
 \* click on **Add** and enter **B45 = B25**,  
 \* click **Add** and enter **E8:E15 >= 0**,  
 \* click **Add** and enter **C54:J54 = 0**  
 \* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



Currency: US Dollar

Exch Rate  
\$1.00 = \$1.00

Coupon  
Payment (PMT)

\$8  
\$14  
\$15  
\$16  
\$10  
\$12  
\$10  
\$12

(1) Coupon Rate \* Face Value / (Number of Payments / Year)  
Enter =B8\*D8/\$B\$6 and copy down

(2) If Rate Convention = EAR,  
Then  $(1 + \text{Yield To Maturity})^{(1 / (\text{Number of Payments / Year}))} - 1$   
Else  $(\text{Yield To Maturity}) / \text{Number of Payment / Year}$   
Enter =IF(C4=1,((1+B5)^(1/B6))-1,B5/B6)

on formulas from the Duration and Convexity sheet  
Duration and Convexity sheet to B24

4	5	6	7	8
2.0	2.5	3.0	3.5	4.0
\$6,300,000	\$6,800,000	\$7,200,000	\$7,900,000	\$8,600,000
\$5,915,919	\$6,285,806	\$6,551,715	\$7,076,524	\$7,583,362
12.3%	13.1%	13.6%	14.7%	15.8%
0.25	0.33	0.41	0.51	0.63

0.74 1.14 1.63 2.32 3.15

(4) Weight \* (Time^2 + Time)  
Enter =C26\*(C22^2+C22) and copy across

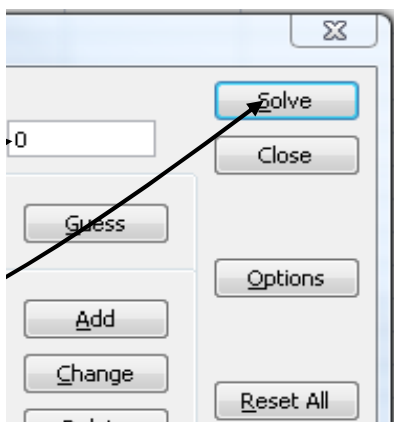
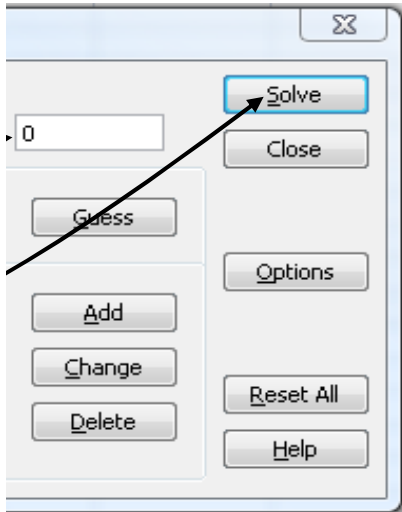
\$0	\$0	\$0	\$0	\$0
\$35,258,310	\$0	\$0	\$0	\$0
\$38,044	\$38,044	\$5,110,580	\$0	\$0
\$75,346	\$75,346	\$75,346	\$75,346	\$10,121,479
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$35,371,700	\$113,390	\$5,185,926	\$75,346	\$10,121,479
\$33,215,255	\$104,816	\$4,718,987	\$67,492	\$8,924,981
69.0%	0.2%	9.8%	0.1%	18.5%
1.38	0.01	0.29	0.00	0.74
4.14	0.02	1.18	0.02	3.71

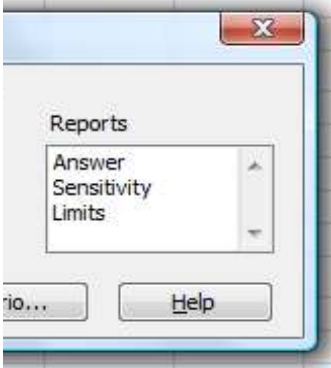
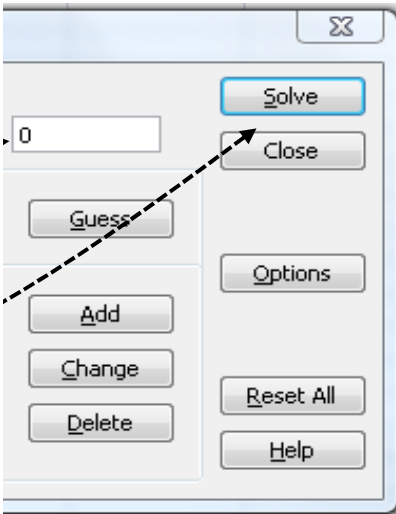
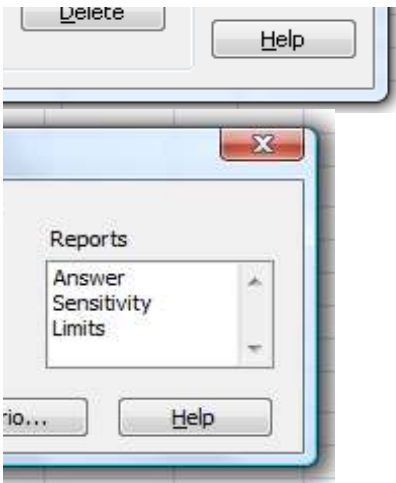
Duration, and Convexity formulas from above  
to B44

\$29,071,700	(\$6,686,610)	(\$2,014,074)	(\$7,824,654)	\$1,521,479
--------------	---------------	---------------	---------------	-------------

by across

and Liabilities in Present Value, Duration, and Convexity  
and =B51-B31 in B57





Currency Number 4  
 (Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
1.50%	4	\$1,000	1,783
2.00%	8	\$1,000	2,042
0.90%	2	\$1,000	6,038
1.50%	4	\$1,000	5,937
1.90%	6	\$1,000	7,017
2.30%	8	\$1,000	8,068

0	1	2	3
0.0	0.5	1.0	1.5
	\$0	\$0	\$0
	\$2,000,000	\$2,200,000	\$2,500,000





Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
0.00%	1	\$1,000	2,000
0.00%	2	\$1,000	2,200
0.00%	3	\$1,000	2,500
0.00%	4	\$1,000	3,200
0.00%	5	\$1,000	3,700
0.00%	6	\$1,000	4,300
0.00%	7	\$1,000	4,700
0.00%	8	\$1,000	5,100

4 2.0	5 2.5	6 3.0	7 3.5	8 4.0
\$0	\$0	\$4,000,000	\$0	\$0
\$3,200,000	\$3,700,000	\$4,300,000	\$4,700,000	\$5,100,000





# BOND PRICING

# Immunization

## Inputs

Rate Convention

☐ EAR ☒ APR

2

Annual Percentage Rate

Yield to Maturity (Annualized)

3.17%

Number of Payments / Year

2

	Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
Bond 1	0.00%	1	\$1,000	4,500
Bond 2	0.00%	2	\$1,000	5,100
Bond 3	0.00%	3	\$1,000	5,600
Bond 4	0.00%	4	\$1,000	6,300
Bond 5	0.00%	5	\$1,000	6,800
Bond 6	0.00%	6	\$1,000	7,200
Bond 7	0.00%	7	\$1,000	7,900
Bond 8	0.00%	8	\$1,000	8,600

## Outputs

Discount Rate / Period (r)

1.6%

## Bond Present Value, Duration, and Convexity using a Timeline

Period	0	1	2	3
Time (Years)	0.0	0.5	1.0	1.5
Liabilities		\$4,500,000	\$5,100,000	\$5,600,000
Present Value of Liabilities		\$4,429,788	\$4,942,094	\$5,341,943
Total Present Value of Liabilities	\$48,127,151			
Weight		9.2%	10.3%	11.1%
Weight * Time		0.05	0.10	0.17
Duration of Liabilities	2.44			
Modified Duration of Liabilities	2.40			
Weight * (Time^2+Time)			0.07	0.21
Convexity of Liabilities	9.37			0.42

## Assets

Bond 1		\$4,500,000	\$0	\$0
Bond 2		\$0	\$5,100,000	\$0
Bond 3		\$0	\$0	\$5,600,000
Bond 4		\$0	\$0	\$0
Bond 5		\$0	\$0	\$0
Bond 6		\$0	\$0	\$0
Bond 7		\$0	\$0	\$0
Bond 8		\$0	\$0	\$0
<hr/>				
Total Assets		\$4,500,000	\$5,100,000	\$5,600,000
Present Value of Assets		\$4,429,788	\$4,942,094	\$5,341,943
Total Present Value of Assets	\$48,127,151			
Weight		9.75%	10.3%	11.1%
Weight * Time		0.02	0.10	0.17
Duration of Assets	3.41			
Modified Duration of Assets	2.48			
Weight * (Time^2+Time)		0.21	0.21	0.42

(3) Copy the Present Value & Duration  
Copy the range B19:J24 from the

(5) (Sum of Weight \* (Time ^ 2 + Time))  
/ ((1 + Yield to Maturity / Number of Payments)  
Enter =SUM(C30:J30)/((1+B18)^2)

## Differences

Total Assets - Liabilities

PV of Assets - PV of Liabilities

Duration of Assets - Duration of Liab

Convexity of Assets - Convexity of Liab

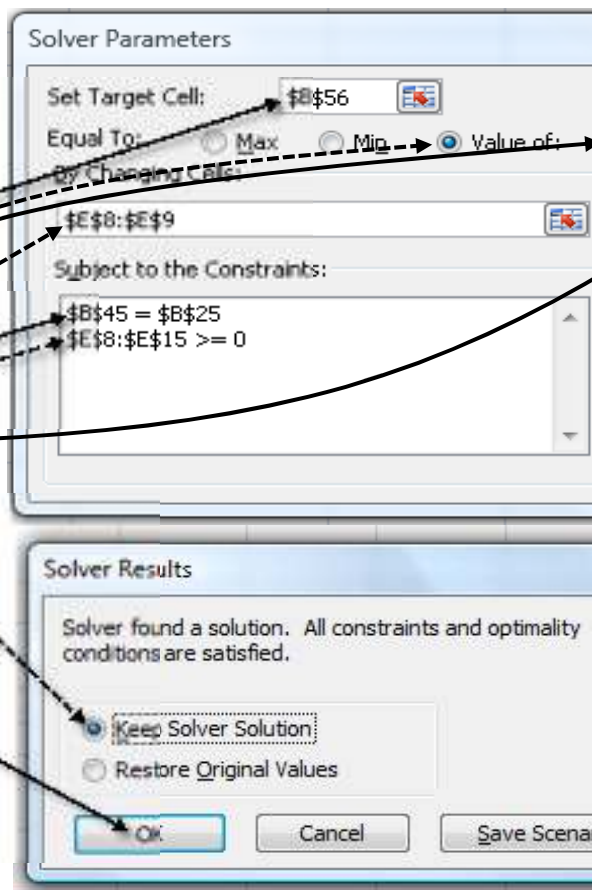
(6) Copy the Present Value,  
Copy the range B24:J31

(7) Total Assets - Liabilities  
Enter =C43-C23 and copy

(8) Compute the differences between Assets &  
Enter =B45-B25 in B55, =B48-B28 in B56,

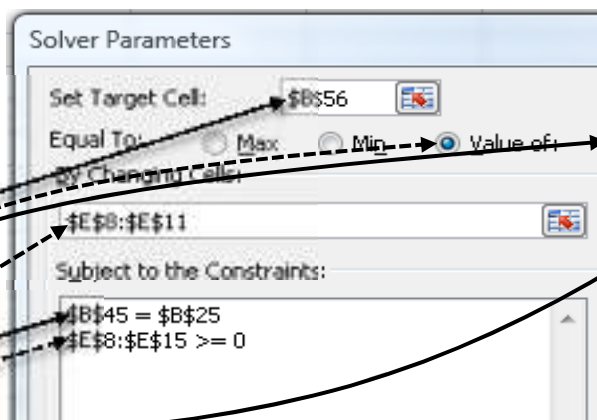
To solve the first problem  
when there is a single liability to immunize

- (9a) Use Solver to determine the number of both Treasury bonds.
- \* Click on **Data | Analysis | Solver**
  - \* enter B56 in Set Target Cell
  - \* click on the **Value Of** button
  - \* enter 0 in the adjacent box,
  - \* enter E8:E9 in By Changing Cells,
  - \* click on **Add** and enter B45 = B25,
  - \* click **Add** and enter E8:E15 >=0
  - \* and click on **Solve**
- When Solver finds a solution,
- \* click on the **Keep Solver Solution** button
  - \* and click on **OK**

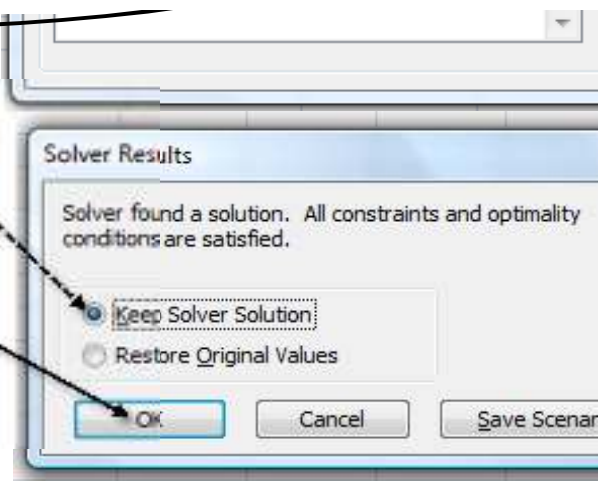


To solve the second problem  
when there is a series of liabilities to immunize

- (9b) Use Solver to determine the number of all four Treasury bonds.
- \* Click on **Data | Analysis | Solver**
  - \* enter B56 in Set Target Cell,
  - \* click on the **Value Of** button
  - \* enter 0 in the adjacent box,
  - \* enter E8:E11 in By Changing Cells,
  - \* click on **Add** and enter B45 = B25,
  - \* click **Add** and enter E8:E15 >=0

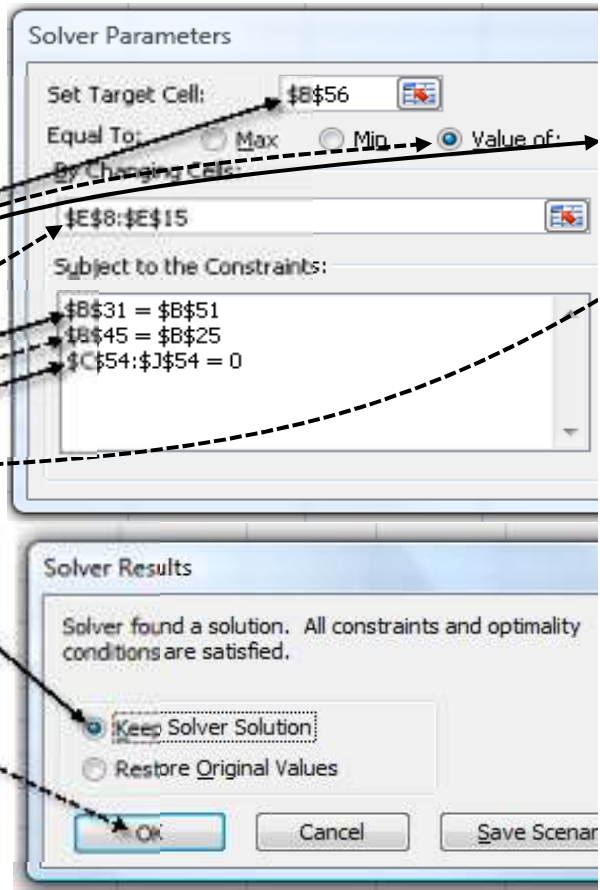


\* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



To solve the third problem  
 when there is a series of liabilities to immunize  
 with cash flow matching

(9c) Use Solver to determine the  
 number of all four Treasury bonds.  
 \* Click on **Data | Analysis | Solver**  
 \* enter **B56** in Set Target Cell,  
 \* click on the **Value Of** button  
 \* enter **0** in the adjacent box,  
 \* enter **E8:E15** in By Changing Cells,  
 \* click on **Add** and enter **B45 = B25**,  
 \* click **Add** and enter **E8:E15 >= 0**,  
 \* click **Add** and enter **C54:J54 = 0**  
 \* and click on **Solve**.  
 When Solver finds a solution,  
 \* click on the **Keep Solver Solution**  
 button  
 \* and click on **OK**



Currency: US Dollar

Exch Rate  
\$1.00 = \$1.00

Coupon  
Payment (PMT)

\$0  
\$0  
\$0  
\$0  
\$0  
\$0  
\$0  
\$0

(1) Coupon Rate \* Face Value / (Number of Payments / Year)  
Enter =B8\*D8/\$B\$6 and copy down

(2) If Rate Convention = EAR,  
Then  $(1 + \text{Yield To Maturity})^{(1 / (\text{Number of Payments / Year}))} - 1$   
Else  $(\text{Yield To Maturity}) / \text{Number of Payment / Year}$   
Enter =IF(C4=1,((1+B5)^(1/B6))-1,B5/B6)

on formulas from the Duration and Convexity sheet  
Duration and Convexity sheet to B24

4	5	6	7	8
2.0	2.5	3.0	3.5	4.0
\$6,300,000	\$6,800,000	\$7,200,000	\$7,900,000	\$8,600,000
\$5,915,919	\$6,285,806	\$6,551,715	\$7,076,524	\$7,583,362
12.3%	13.1%	13.6%	14.7%	15.8%
0.25	0.33	0.41	0.51	0.63

0.74      1.14      1.63      2.32      3.15

(4) Weight \* (Time^2 + Time)  
Enter =C26\*(C22^2+C22) and copy across

\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$0	\$0	\$0	\$0	\$0
\$6,300,000	\$0	\$0	\$0	\$0
\$0	\$6,800,000	\$0	\$0	\$0
\$0	\$0	\$7,200,000	\$0	\$0
\$0	\$0	\$0	\$7,900,000	\$0
\$0	\$0	\$0	\$0	\$8,600,000
\$6,300,000	\$6,800,000	\$7,200,000	\$7,900,000	\$8,600,000
\$5,915,919	\$6,285,806	\$6,551,715	\$7,076,524	\$7,583,362

12.3%      13.1%      13.6%      14.7%      15.8%  
0.25      0.33      0.41      0.51      0.63

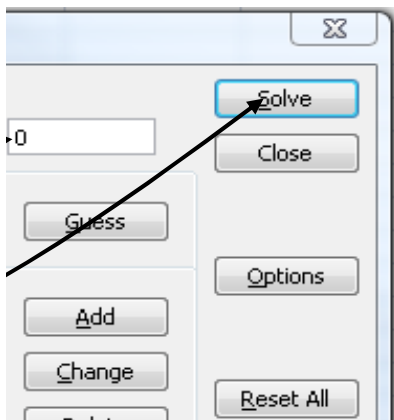
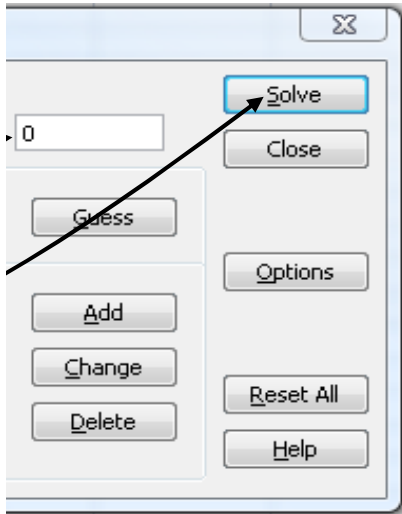
0.74      1.14      1.63      2.32      3.15

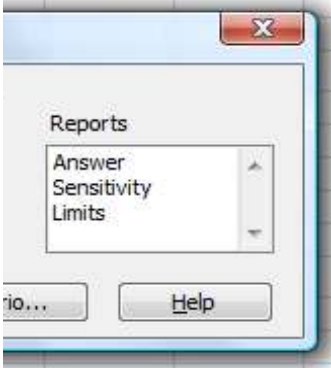
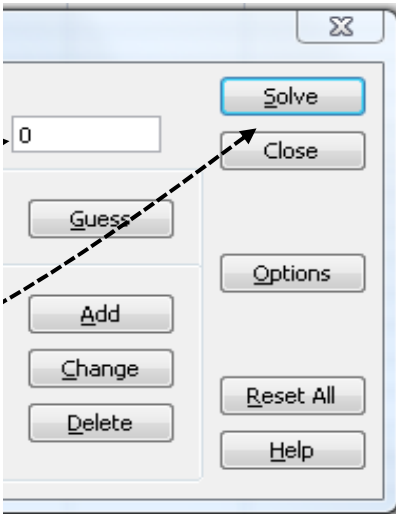
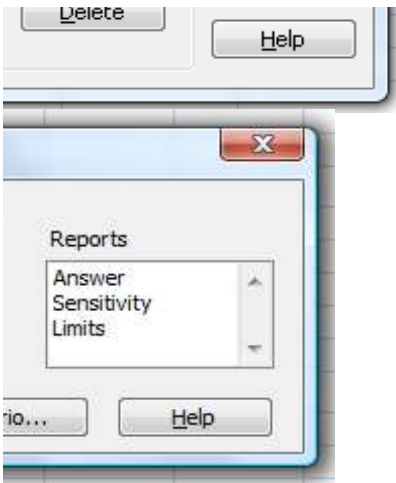
Duration, and Convexity formulas from above  
to B44

\$0                      \$0                      \$0                      \$0                      \$0

by across

and Liabilities in Present Value, Duration, and Convexity  
and =B51-B31 in B57





Currency Number 4  
 (Select from below)

- 1 = Chinese Yuan      ¥ 7.3790
- 2 = European Euro      € 0.6805
- 3 = Indian Rupee      IDR 39.30
- 4 = US Dollar      \$1.00

Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
1.50%	4	\$1,000	1,783
2.00%	8	\$1,000	2,042
0.90%	2	\$1,000	6,038
1.50%	4	\$1,000	5,937
1.90%	6	\$1,000	7,017
2.30%	8	\$1,000	8,068

0	1	2	3
0.0	0.5	1.0	1.5
	\$0	\$0	\$0
	\$2,000,000	\$2,200,000	\$2,500,000





Annual Coupon Rate	Number of Periods to Maturity (T)	Face Value (PAR)	Number of Bonds
0.00%	1	\$1,000	2,000
0.00%	2	\$1,000	2,200
0.00%	3	\$1,000	2,500
0.00%	4	\$1,000	3,200
0.00%	5	\$1,000	3,700
0.00%	6	\$1,000	4,300
0.00%	7	\$1,000	4,700
0.00%	8	\$1,000	5,100

4 2.0	5 2.5	6 3.0	7 3.5	8 4.0
\$0	\$0	\$4,000,000	\$0	\$0
\$3,200,000	\$3,700,000	\$4,300,000	\$4,700,000	\$5,100,000





	A	B	C	D	E	F	G	H	I	J
1	<b>BOND PRICING</b>	<b>System of Five Bond Variables</b>					Currency: US Dollar	Exch Rate \$1.00 =	\$1.00	
2										
3	<b>Inputs</b>	<b>Annual Percentage Rate</b>								
4	Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2							
5	Annual Coupon Rate	8.00%								
6	Yield to Maturity (Annualized)	6.54%								
7	Number of Payments / Year	2								
8	(1) Number of Periods to Maturity (T)	10								
9	(2) Face Value (PAR)	\$1,000								
10	(3) Discount Rate / Period (r)	3.27%								
11	(4) Coupon Payment (PMT)	\$40.00								
12	(5) Bond Price (P)	\$1,061.42								
13										
14	(1) Number of Periods to Maturity (T) from the other four variables									
15	Number of Periods to Maturity using NPER Function	10								
16										
17	(2) Face Value (PAR) from the other four variables									
18	Face Value using the FV Function	\$1,000.00								
19	Face Value using the Formula	\$1,000.00								
20										
21	(3) Discount Rate / Period (r) from the other four variables									
22	Discount Rate / Period using the RATE Function	3.27%								
23										
24	(4) Coupon Payment (PMT) from the other four variables									
25	Coupon Payment using the PMT Function	\$40.00								
26	Coupon Payment using the Formula	\$40.00								
27										
28	(5) Bond Price (P) from the other four variables									
29	Bond Price using the PV Function	\$1,061.42								
30	Bond Price using the Formula	\$1,061.42								
31										
32										
33										
34	(5) The Bond Price Formula is									
35	$P = \frac{PMT \cdot \left(1 - \frac{1}{(1+r)^T}\right)}{r} + \frac{PAR}{(1+r)^T}$									
36	Enter =B11*(1-(1/(1+(B10/2)^B8)))/(B10/2)+B10/(1+(B10/2)^B8)									
37										
38										
39										
40										
41										
42										

(1) NPER(Discount Rate / Period, Coupon Payment, -Bond Price, Face Value)  
Enter =NPER(B10,B11,B12,B9)

(2) FV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price)  
Enter =FV(B10,B11,B11,B12)

(3) The Face Value Formula is  
$$PAR = P \cdot (1+r)^T - \frac{PMT \cdot \left(\left((1+r)^T\right) - 1\right)}{r}$$
  
Enter =B12\*(1+B10/2)^B11-(B11/2)\*(1+B10/2)^B11

(4) RATE(Number of Periods to Maturity, Coupon Payment, -Bond Price, Face Value)  
Enter =RATE(B10,B11,B12,B9)

(5) PMT(Discount Rate / Period, Number of Periods to Maturity, Bond Price, Face Value)  
Enter =PMT(B10,B8,B12,B9)

(6) The Coupon Payment Formula is  
$$PMT = \frac{P - PAR / (1+r)^T}{\left(1 - \frac{1}{(1+r)^T}\right) / r}$$
  
Enter =B12-B9/(1+B10/2)^B11-(1+B10/2)^B11

(7) PV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, Face Value)  
Enter =PV(B10,B11,B11,B9)

	A	B	C	D	E	F	G	H	I	J
	<b>BOND PRICING</b>	<b>System of Five Bond Variables</b>					Currency: US Dollar	Exch Rate \$1.00 =	\$1.00	
1										
2										
3	<b>Inputs</b>	<b>Annual Percentage Rate</b>								
4	Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2							
5	Annual Coupon Rate	5.44%								
6	Yield to Maturity (Annualized)	9.08%								
7	Number of Payments / Year	2								
8	(1) Number of Periods to Maturity (T)	11								
9	(2) Face Value (PAR)	\$1,000								
10	(3) Discount Rate / Period (r)	4.54%								
11	(4) Coupon Payment (PMT)	\$27.10								
12	(5) Bond Price (P)	\$880.00								
13										
14	(1) Number of Periods to Maturity (T) from the other four variables									
15	Number of Periods to Maturity using NPER Function	11								
16										
17	(2) Face Value (PAR) from the other four variables									
18	Face Value using the FV Function	\$1,000.00								
19	Face Value using the Formula	\$1,000.00								
20										
21	(3) Discount Rate / Period (r) from the other four variables									
22	Discount Rate / Period using the RATE Function	4.54%								
23										
24	(4) Coupon Payment (PMT) from the other four variables									
25	Coupon Payment using the PMT Function	\$27.10								
26	Coupon Payment using the Formula	\$27.10								
27										
28	(5) Bond Price (P) from the other four variables									
29	Bond Price using the PV Function	\$880.00								
30	Bond Price using the Formula	\$880.00								
31										
32										
33										
34	(5) The Bond Price Formula is									
35	$P = \frac{PMT \cdot \left(1 - (1+r)^{-T}\right)}{r} + \frac{PAR}{(1+r)^T}$									
36	Enter =B11*(1-(1+B10^(-B8)))/B10 + B10/(1+B10^B8)									
37										
38										
39										
40										
41										
42										

(1) NPER(Discount Rate / Period, Coupon Payment, -Bond Price, Face Value)  
Enter =NPER(B10,B11,B12,B9)

(2) FV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price)  
Enter =FV(B10,B11,B11,B12)

(3) The Face Value Formula is  
$$PAR = P \cdot (1+r)^T - \frac{PMT \cdot \left( \left( (1+r)^T \right) - 1 \right)}{r}$$
  
Enter =B12\*(1+B10^B11)-B11\*(1+B10^B11)/B10

(4) RATE(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price, Face Value)  
Enter =RATE(B10,B11,B12,B9)

(5) PMT(Discount Rate / Period, Number of Periods to Maturity, Bond Price, Face Value)  
Enter =PMT(B10,B8,B12,B9)

(6) The Coupon Payment Formula is  
$$PMT = \frac{P - PAR / (1+r)^T}{\left( 1 - (1+r)^{-T} \right) / r}$$
  
Enter =B12-B9/(1+B10^B11)/(1-(1+B10^(-B11))/B10)

(7) PV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, Face Value)  
Enter =PV(B10,B11,B11,B9)

	A	B	C	D	E	F	G	H	I	J
1	<b>BOND PRICING</b>	<b>System of Five Bond Variables</b>					Currency: US Dollar	Exch Rate \$1.00 =	\$1.00	
2										
3	<b>Inputs</b>	<b>Annual Percentage Rate</b>								
4	Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2							
5	Annual Coupon Rate	6.00%								
6	Yield to Maturity (Annualized)	11.44%								
7	Number of Payments / Year	2								
8	(1) Number of Periods to Maturity (T)	8								
9	(2) Face Value (PAR)	\$1,000								
10	(3) Discount Rate / Period (r)	5.72%								
11	(4) Coupon Payment (PMT)	\$30.00								
12	(5) Bond Price (P)	\$865.00								
13										
14	(1) Number of Periods to Maturity (T) from the other four variables									
15	Number of Periods to Maturity using NPER Function	8								
16										
17	(2) Face Value (PAR) from the other four variables									
18	Face Value using the FV Function	\$1,000.00								
19	Face Value using the Formula	\$1,000.00								
20										
21	(3) Discount Rate / Period (r) from the other four variables									
22	Discount Rate / Period using the RATE Function	5.72%								
23										
24	(4) Coupon Payment (PMT) from the other four variables									
25	Coupon Payment using the PMT Function	\$30.00								
26	Coupon Payment using the Formula	\$30.00								
27										
28	(5) Bond Price (P) from the other four variables									
29	Bond Price using the PV Function	\$865.00								
30	Bond Price using the Formula	\$865.00								
31										
32										
33										
34	(5) The Bond Price Formula is									
35	$P = \frac{PMT \cdot \left(1 - \frac{1}{(1+r)^T}\right)}{r} + \frac{PAR}{(1+r)^T}$									
36	Enter =B11*(1-(1/(1+(B10/2)^B8)))/(B10/2)+B10/(1+(B10/2)^B8)									
37										
38										
39										
40										
41										
42										

(1) NPER(Discount Rate / Period, Coupon Payment, -Bond Price, Face Value)  
Enter =NPER(B10,B11,B12,B9)

(2) FV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price)  
Enter =FV(B10,B11,B11,B12)

(3) The Face Value Formula is  
$$PAR = P \cdot (1+r)^T - \frac{PMT \cdot \left(\left((1+r)^T\right) - 1\right)}{r}$$
  
Enter =B12\*(1+B10/2)^B8-(B11\*(1+B10/2)^B8-1)/B10

(4) RATE(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price, Face Value)  
Enter =RATE(B10,B11,B12,B9)

(5) PMT(Discount Rate / Period, Number of Periods to Maturity, Bond Price, Face Value)  
Enter =PMT(B10,B8,B12,B9)

(6) The Coupon Payment Formula is  
$$PMT = \frac{P - PAR / (1+r)^T}{\left(1 - \frac{1}{(1+r)^T}\right) / r}$$
  
Enter =(B12-B9)/(1+(B10/2)^B8-1)/(1+(B10/2)^B8-1)/B10

(7) PV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, Face Value)  
Enter =PV(B10,B8,B11,B9)

	A	B	C	D	E	F	G	H	I	J
1	<b>BOND PRICING</b>	<b>System of Five Bond Variables</b>					Currency: US Dollar	Exch Rate \$1.00 =	\$1.00	
2										
3	<b>Inputs</b>	<b>Annual Percentage Rate</b>								
4	Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2							
5	Annual Coupon Rate	11.78%								
6	Yield to Maturity (Annualized)	7.62%								
7	Number of Payments / Year	2								
8	(1) Number of Periods to Maturity (T)	11								
9	(2) Face Value (PAR)	\$764.22								
10	(3) Discount Rate / Period (r)	3.81%								
11	(4) Coupon Payment (PMT)	\$45.00								
12	(5) Bond Price (P)	\$872.00								
13										
14	(1) Number of Periods to Maturity (T) from the other four variables									
15	Number of Periods to Maturity using NPER Function	11								
16										
17	(2) Face Value (PAR) from the other four variables									
18	Face Value using the FV Function	\$764.22								
19	Face Value using the Formula	\$764.22								
20										
21	(3) Discount Rate / Period (r) from the other four variables									
22	Discount Rate / Period using the RATE Function	3.81%								
23										
24	(4) Coupon Payment (PMT) from the other four variables									
25	Coupon Payment using the PMT Function	\$45.00								
26	Coupon Payment using the Formula	\$45.00								
27										
28	(5) Bond Price (P) from the other four variables									
29	Bond Price using the PV Function	\$872.00								
30	Bond Price using the Formula	\$872.00								
31										
32										
33										
34	(5) The Bond Price Formula is									
35	$P = \frac{PMT \cdot \left(1 - \frac{1}{(1+r)^T}\right)}{r} + \frac{PAR}{(1+r)^T}$									
36	Enter =B11*(1-(1/(1+B10^B11)))/B10 + B12/(1+B10^B11)									
37										
38										
39										
40										
41										
42										

(1) NPER(Discount Rate / Period, Coupon Payment, -Bond Price, Face Value)  
Enter =NPER(B10,B11,B12,B9)

(2) FV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price)  
Enter =FV(B10,B11,B11,B12)

(3) The Face Value Formula is  
$$PAR = P \cdot (1+r)^T - \frac{PMT \cdot \left(\left((1+r)^T\right) - 1\right)}{r}$$
  
Enter =B12\*(1+B10^B11) - B11\*(1+B10^B11 - 1)/B10

(4) RATE(Number of Periods to Maturity, Coupon Payment, -Bond Price, Face Value)  
Enter =RATE(B11,B11,B12,B9)

(5) PMT(Discount Rate / Period, Number of Periods to Maturity, Bond Price, Face Value)  
Enter =PMT(B10,B11,B12,B9)

(6) The Coupon Payment Formula is  
$$PMT = \frac{P - PAR / (1+r)^T}{\left(1 - \frac{1}{(1+r)^T}\right) / r}$$
  
Enter =B12/B10 - (B12/B10)/(1+B10^B11 - 1)/B10

(7) PV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, Face Value)  
Enter =PV(B10,B11,B11,B9)

	A	B	C	D	E	F	G	H	I	J
	<b>BOND PRICING</b>	<b>System of Five Bond Variables</b>					Currency: US Dollar	Exch Rate \$1.00 =	\$1.00	
1										
2										
3	<b>Inputs</b>	<b>Annual Percentage Rate</b>								
4	Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR	2							
5	Annual Coupon Rate	7.40%								
6	Yield to Maturity (Annualized)	8.70%								
7	Number of Payments / Year	2								
8	(1) Number of Periods to Maturity (T)	30								
9	(2) Face Value (PAR)	\$1,000								
10	(3) Discount Rate / Period (r)	4.35%								
11	(4) Coupon Payment (PMT)	\$37.00								
12	(5) Bond Price (P)	\$887.00								
13										
14	(1) Number of Periods to Maturity (T) from the other four variables									
15	Number of Periods to Maturity using NPER Function	30								
16										
17	(2) Face Value (PAR) from the other four variables									
18	Face Value using the FV Function	\$1,000.00								
19	Face Value using the Formula	\$1,000.00								
20										
21	(3) Discount Rate / Period (r) from the other four variables									
22	Discount Rate / Period using the RATE Function	4.35%								
23										
24	(4) Coupon Payment (PMT) from the other four variables									
25	Coupon Payment using the PMT Function	\$37.00								
26	Coupon Payment using the Formula	\$37.00								
27										
28	(5) Bond Price (P) from the other four variables									
29	Bond Price using the PV Function	\$887.00								
30	Bond Price using the Formula	\$887.00								
31										
32										
33										
34	(5) The Bond Price Formula is									
35	$P = \frac{PMT \cdot \left(1 - (1+r)^{-T}\right)}{r} + \frac{PAR}{(1+r)^T}$									
36	Enter =B11*(1-(1+(B10)/(B8))^(-B12))/(B10/(B8))+(B11/(1+(B10)/(B8)))									
37										
38										
39										
40										
41										
42										

(1) NPER(Discount Rate / Period, Coupon Payment, -Bond Price, Face Value)  
Enter =NPER(D10,D11,D12,D8)

(2) FV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price)  
Enter =FV(D10,D11,D11,D12)

(3) The Face Value Formula is  
$$PAR = P \cdot (1+r)^T - \frac{PMT \cdot \left( \left( (1+r)^T \right) - 1 \right)}{r}$$
  
Enter =D12\*(1+D10/D11)^D11-(D11\*(1+D10/D11)^D11)/D10

(4) RATE(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, -Bond Price, Face Value)  
Enter =RATE(D10,D11,D12,D8)

(5) PMT(Discount Rate / Period, Number of Periods to Maturity, Bond Price, Face Value)  
Enter =PMT(B10,B8,-B12,B3)

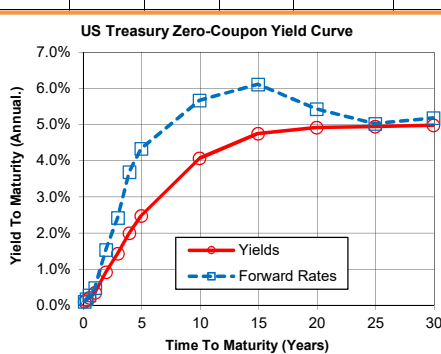
(6) The Coupon Payment Formula is  
$$PMT = \frac{P - PAR / (1+r)^T}{\left( 1 - (1+r)^{-T} \right) / r}$$
  
Enter =(D12-D9)/(1+D10/D11)^D11-(1+D10/D11)^D11/D10

(7) PV(Discount Rate / Period, Number of Periods to Maturity, Coupon Payment, Face Value)  
Enter =PV(D10,D11,D11,D9)

# THE YIELD CURVE

## Obtaining and Using It

Yield Curve Inputs	Maturity Date	Time To Maturity	Yield To Maturity	Forward Rates
Today's Date	3/11/2010			
One Month Treasury Bill	4/15/2010	0.09	0.101%	0.101%
Three Month Treasury Bill	6/10/2010	0.25	0.147%	0.175%
Six Month Treasury Bill	9/9/2010	0.49	0.211%	0.275%
One Year Treasury Strip	3/10/2011	1.00	0.349%	0.485%
Two Year Treasury Strip	2/15/2012	1.93	0.920%	1.336%
Three Year Treasury Strip	2/15/2013	2.93	1.430%	2.420%
Four Year Treasury Strip	2/15/2014	3.93	2.000%	3.687%
Five Year Treasury Strip	2/15/2015	4.93	2.470%	4.337%
Ten Year Treasury Strip	2/15/2020	9.93	4.070%	5.671%
Fifteen Year Treasury Bond	2/15/2025	14.93	4.750%	6.113%
Twenty Year Treasury Bond	2/15/2030	19.93	4.920%	5.429%
Twenty Five Year Treasury Bond	2/15/2035	24.93	4.940%	5.020%
Thirty Year Treasury Bond	2/15/2040	29.93	4.980%	5.80%



Notation:

$t$  = an earlier date

$T$  = a later date

$y_t$  = date  $t$  yield

$y_T$  = date  $T$  yield

$f_{t,T}$  = forward rate from date  $t$  to date  $T$

(1) Maturity Date = Today's Date  
Enter =YL48-4VCISUS4,US and copy down

(2) Forward Rate from date  $t$  to date  $T$

$$f_{T-t} = \left( \frac{1 + y_T}{1 + y_t} \right)^{T-t} - 1$$

Enter =((1+Y5/360)/(1+Y4/360)^(3/360))-1 and copy down

### Bond Inputs

	Effective Annual Rate
Rate Convention	<input checked="" type="radio"/> EAR <input type="radio"/> APR
Annual Coupon Rate	3.5%
Number of Payments / Year	2
Number of Periods to Maturity	8
Face Value	\$1,000

(3) Coupon Rate = Face Value / (Number of Payments/Year)  
Enter =B27/B30/B38

(4) Periods 1 - 7 = Coupon Payment

Enter =B33 and copy across

(5) Period 8 = Coupon Payment + Face Value

Enter =B33+B30

### Outputs

Coupon Payment	\$10
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(6) Corresponding yield on the yield curve

Enter =D7 in C39, =D8 in B35, =D9 in B39, =D10 in B35, =D11 in B39  
Enter =D19+19/2 in L19, =D19+19/2 in G35, =D19+19/2 in G39

### Bond Price and Yield To Maturity using a Timeline

Period	0	1	2	3	4	5	6	7	8
Time (Years)	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
Cash Flows		\$17.50	\$17.50	\$17.50	\$17.50	\$17.50	\$17.50	\$17.50	\$1,017.50
Yield to Maturity (Annualized)		0.21%	0.35%	0.63%	0.92%	1.18%	1.43%	1.72%	2.00%
Discount Rate / Period		0.11%	0.17%	0.32%	0.46%	0.59%	0.71%	0.85%	1.00%
Present Value of Cash Flow		\$17.48	\$17.44	\$17.33	\$17.18	\$17.00	\$16.77	\$16.49	\$940.01
Coupon Bond Price									\$1,059.71
Coupon Bond Discount Rate / Period									0.97%
Coupon Bond Yield to Maturity									1.95%

(7) If Rate Convention = EAR,  
Then (Yield To Maturity) \* (1 + (Number of Payments / Year)) - 1  
Else (Yield to Maturity) / (Number of Payments / Year)  
Enter =1+(B35-1)\*(1+(C39/360)/360) or (C39/360)  
and copy across

(8) Cash Flow / (1 + Discount Rate / Period) ^ Period

Enter =C39/(1+D40/360) and copy across

(9) Sum of all the Present Value of Cash Flows

Enter =SUM(C41:J41)

(10) RATE (Number of Periods to Maturity, Coupon Bond, -Bond Price, Par Value)

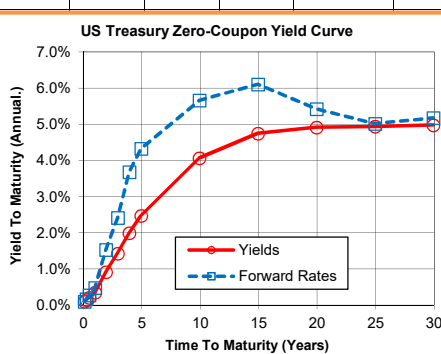
Enter =RATE(J29,D33,D42,D30)

(11) If Rate Convention = EAR  
Then (1 + Discount Rate / Period) ^ (Number of Payments / Year) - 1  
Else (Discount Rate / Period) ^ (Number of Payments / Year)  
Enter =F(\$C\$26-1)^(1+(B43/360)/360) or B43/360

# THE YIELD CURVE

## Obtaining and Using It

Yield Curve Inputs	Maturity Date	Time To Maturity	Yield To Maturity	Forward Rates
Today's Date	3/11/2010			
One Month Treasury Bill	4/15/2010	0.09	0.101%	0.101%
Three Month Treasury Bill	6/10/2010	0.25	0.147%	0.175%
Six Month Treasury Bill	9/9/2010	0.49	0.211%	0.275%
One Year Treasury Strip	3/10/2011	1.00	0.349%	0.485%
Two Year Treasury Strip	2/15/2012	1.93	0.920%	1.36%
Three Year Treasury Strip	2/15/2013	2.93	1.430%	2.420%
Four Year Treasury Strip	2/15/2014	3.93	2.000%	3.687%
Five Year Treasury Strip	2/15/2015	4.93	2.470%	4.337%
Ten Year Treasury Strip	2/15/2020	9.93	4.070%	5.671%
Fifteen Year Treasury Bond	2/15/2025	14.93	4.750%	6.113%
Twenty Year Treasury Bond	2/15/2030	19.93	4.920%	6.429%
Twenty Five Year Treasury Bond	2/15/2035	24.93	4.940%	6.520%
Thirty Year Treasury Bond	2/15/2040	29.93	4.980%	6.80%



### Notation:

$t$  = an earlier date

$T$  = a later date

$y_t$  = date  $t$  yield

$y_T$  = date  $T$  yield

$f_{t,T}$  = forward rate from date  $t$  to date  $T$

(1) Maturity Date = Today's Date  
Enter =YL40-4VCISUS4,US and copy down

(2) Forward Rate from date  $t$  to date  $T$

$$f_{T-t} = \left( \frac{(1 + y_T)^T}{(1 + y_t)^t} \right)^{1/(T-t)} - 1$$

Enter =((1+Y5)^25)/((1+Y4)^10)-1 and copy down

### Bond Inputs

	Effective Annual Rate
Rate Convention	<input checked="" type="radio"/> EAR <input type="radio"/> APR
Annual Coupon Rate	4.2%
Number of Payments / Year	2
Number of Periods to Maturity	8
Face Value	\$2,000

(3) Coupon Rate = Face Value / (Number of Payments/Year)  
Enter =B27/B30/B28

(4) Periods 1 - 7 = Coupon Payment

Enter =B33 and copy across

(5) Period 8 = Coupon Payment + Face Value

Enter =B33+B30

### Outputs

Coupon Payment	\$42
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(6) Corresponding yield on the yield curve

Enter =D7 in C39, =D8 in B35, =D9 in B38, =D10 in B35, =D11 in B38  
Enter =D19+19/2 in L19, =D19+19/2 in G35, =D19+19/2 in G38

### Bond Price and Yield To Maturity using a Timeline

Period	0	1	2	3	4	5	6	7	8
Time (Years)	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
Cash Flows		\$42.00	\$42.00	\$42.00	\$42.00	\$42.00	\$42.00	\$42.00	\$2,042.00
Yield to Maturity (Annualized)		0.21%	0.35%	0.63%	0.92%	1.18%	1.43%	1.72%	2.00%
Discount Rate / Period		0.11%	0.17%	0.32%	0.46%	0.59%	0.71%	0.85%	1.00%
Present Value of Cash Flow		\$41.96	\$41.65	\$41.60	\$41.24	\$40.79	\$40.25	\$39.57	\$1,886.49
Coupon Bond Price									\$2,173.79
Coupon Bond Discount Rate / Period									0.97%
Coupon Bond Yield to Maturity									1.94%

(7) If Rate Convention = EAR,  
Then (Yield To Maturity) \* (1 + (Number of Payments / Year)) - 1  
Else (Yield to Maturity) / (Number of Payments / Year)  
Enter =1+(B35-1)\*(1+(C39/(B35/2))) / (C39/(B35/2))  
and copy across

(8) Cash Flow / (1 + Discount Rate / Period) ^ Period  
Enter =C39/((1+C40/C35)^C36) and copy across

(9) Sum of all the Present Value of Cash Flows  
Enter =SUM(C41:C49)

(10) RATE (Number of Periods to Maturity, Coupon Bond, -Bond Price, Par Value)  
Enter =RATE(D29,D30,-D42,D30)

(11) If Rate Convention = EAR  
Then (1 + Discount Rate \* Period) / (Number of Payments / Year) - 1  
Else (Discount Rate \* Period) / (Number of Payments / Year)  
Enter =F((B35-1)\*(1+(C39/(B35/2))) / (C39/(B35/2)))

## THE YIELD CURVE

### Obtaining and Using It

Yield Curve Inputs	Maturity Date	Time To Maturity	Yield To Maturity	Forward Rates
Today's Date	3/11/2010			
One Month Treasury Bill	4/15/2010	0.09	0.101%	0.101%
Three Month Treasury Bill	6/10/2010	0.25	0.147%	0.175%
Six Month Treasury Bill	9/9/2010	0.49	0.211%	0.275%
One Year Treasury Strip	3/10/2011	1.00	0.349%	0.485%
Two Year Treasury Strip	2/15/2012	1.93	0.920%	1.36%
Three Year Treasury Strip	2/15/2013	2.93	1.430%	2.420%
Four Year Treasury Strip	2/15/2014	3.93	2.000%	3.687%
Five Year Treasury Strip	2/15/2015	4.93	2.470%	4.337%
Ten Year Treasury Strip	2/15/2020	9.93	4.070%	5.671%
Fifteen Year Treasury Bond	2/15/2025	14.93	4.750%	6.113%
Twenty Year Treasury Bond	2/15/2030	19.93	4.920%	6.429%
Twenty Five Year Treasury Bond	2/15/2035	24.93	4.940%	6.620%
Thirty Year Treasury Bond	2/15/2040	29.93	4.980%	6.80%

**Notation:**  
 $t$  = an earlier date  
 $T$  = a later date  
 $y_t$  = date  $t$  yield  
 $y_T$  = date  $T$  yield  
 $f_{t,T}$  = forward rate from date  $t$  to date  $T$

(1) **Maturity Date = Today's Date**  
 Enter =YIELD(A4,B4,C4,D4,E4) and copy down

(2) **Forward Rate from date  $t$  to date  $T$**   

$$f_{t,T} = \left( \frac{(1 + y_T)^T}{(1 + y_t)^t} \right)^{1/(T-t)} - 1$$
 Enter =((1+B5^25)/(1+B4^10)^2.5)^0.4-1 and copy down

### Bond Inputs

	Annual Percentage Rate
Rate Convention	<input type="radio"/> EAR <input checked="" type="radio"/> APR
Annual Coupon Rate	4.2%
Number of Payments / Year	2
Number of Periods to Maturity	8
Face Value	\$2,000

(3) **Coupon Rate = Face Value / (Number of Payments/Year)**  
 Enter =B27\*B30/B28

(4) **Periods 1 - 7 = Coupon Payment**  
 Enter =B28 and copy across

(5) **Period 8 = Coupon Payment + Face Value**  
 Enter =B28+B30

### Outputs

Coupon Payment	\$42
----------------	------

(6) **Corresponding yield on the yield curve**  
 Enter =D7 in C39, =D8 in D39, =D9 in E39, =D10 in F39, =D11 in G39  
 Enter =D19+19D2 in L19, =D19+19D2 in G39, =D19+19D2 in G39

### Bond Price and Yield To Maturity using a Timeline

Period	0	1	2	3	4	5	6	7	8
Time (Years)	0.0	0.5	1.0	1.5	2.0	2.5	3.0	3.5	4.0
Cash Flows	\$42.00	\$42.00	\$42.00	\$42.00	\$42.00	\$42.00	\$42.00	\$42.00	\$2,042.00
Yield to Maturity (Annualized)		0.21%	0.35%	0.63%	0.92%	1.18%	1.43%	1.72%	2.00%
Discount Rate / Period		0.11%	0.17%	0.32%	0.46%	0.59%	0.72%	0.86%	1.00%
Present Value of Cash Flow		\$41.96	\$41.65	\$41.60	\$41.24	\$40.79	\$40.24	\$39.56	\$1,885.75
Coupon Bond Price									\$2,112.89
Coupon Bond Discount Rate / Period									0.97%
Coupon Bond Yield to Maturity									1.94%

(7) If Rate Convention = EAR,  
 Then (Yield To Maturity) \* (Number of Payments / Year) - 1  
 Else (Yield to Maturity) / (Number of Payments / Year)  
 Enter =1+(B32-1)\*(1+(C39)/(B30/2)) (C39/B30/2) and copy across

(8) **Cash Flow / (1 + Discount Rate / Period) ^ Period**  
 Enter =C39/(1+D40^D36) and copy across

(9) **Sum of all the Present Value of Cash Flows**  
 Enter =SUM(D41:D49)

(10) **RATLN( Number of Periods to Maturity, Coupon Bond, Bond Price, Face Value)**  
 Enter =RATLN(D29,D30,D42,D30)

(11) If Rate Convention = EAR,  
 Then (1 + Discount Rate \* Period) / (Number of Payments / Year) - 1  
 Else (Discount Rate \* Period) / (Number of Payments / Year)  
 Enter =F(\$C\$26-1)/(1+(B43)/(B28))-1 (B43/B28)