Essential Calculus Early Transcendentals 2nd Edition Stewart Solutions Manual

COMPLETE SOLUTIONS MANUALfor

Stewart's

ESSENTIAL CALCULUS EARLY TRANSCENDENTALS

SECOND EDITION

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ABBREVIATIONS AND SYMBOLS

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CD	concave downward
CU	concave upward
D	the domain of f
FDT	First Derivative Test
HA	horizontal asymptote(s)
Ι	interval of convergence
IP	inflection point(s)
R	radius of convergence
VA	vertical asymptote(s)
$\stackrel{\text{CAS}}{=}$	indicates the use of a computer algebra system.
H	indicates the use of l'Hospital's Rule.
<u>j</u>	indicates the use of Formula j in the Table of Integrals in the back endpapers.
<u>s</u>	indicates the use of the substitution $\{u = \sin x, du = \cos x dx\}.$
<u> </u>	indicates the use of the substitution $\{u = \cos x, du = -\sin x dx\}$.

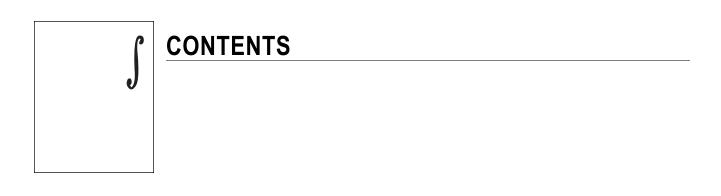
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DIAGNOSTIC TESTS

Test A Algebra

- 1. (a) $(-3)^4 = (-3)(-3)(-3)(-3) = 81$ (b) $-3^4 = -(3)(3)(3)(3) = -81$ (c) $3^{-4} = \frac{1}{3^4} = \frac{1}{81}$ (d) $\frac{5^{23}}{5^{21}} = 5^{23-21} = 5^2 = 25$ (e) $(\frac{2}{3})^{-2} = (\frac{3}{2})^2 = \frac{9}{4}$ (f) $16^{-3/4} = \frac{1}{16^{3/4}} = \frac{1}{(\sqrt[4]{16})^3} = \frac{1}{2^3} = \frac{1}{8}$
- 2. (a) Note that $\sqrt{200} = \sqrt{100 \cdot 2} = 10\sqrt{2}$ and $\sqrt{32} = \sqrt{16 \cdot 2} = 4\sqrt{2}$. Thus $\sqrt{200} \sqrt{32} = 10\sqrt{2} 4\sqrt{2} = 6\sqrt{2}$.

(b)
$$(3a^3b^3)(4ab^2)^2 = 3a^3b^316a^2b^4 = 48a^5b^7$$

(c)
$$\left(\frac{3x^{3/2}y^3}{x^2y^{-1/2}}\right)^{-2} = \left(\frac{x^2y^{-1/2}}{3x^{3/2}y^3}\right)^2 = \frac{(x^2y^{-1/2})^2}{(3x^{3/2}y^3)^2} = \frac{x^4y^{-1}}{9x^3y^6} = \frac{x^4}{9x^3y^6y} = \frac{x^4}{9y^7}$$

3. (a) 3(x+6) + 4(2x-5) = 3x + 18 + 8x - 20 = 11x - 2

- (b) $(x+3)(4x-5) = 4x^2 5x + 12x 15 = 4x^2 + 7x 15$
- (c) $\left(\sqrt{a} + \sqrt{b}\right)\left(\sqrt{a} \sqrt{b}\right) = \left(\sqrt{a}\right)^2 \sqrt{a}\sqrt{b} + \sqrt{a}\sqrt{b} \left(\sqrt{b}\right)^2 = a b$

Or: Use the formula for the difference of two squares to see that $\left(\sqrt{a} + \sqrt{b}\right)\left(\sqrt{a} - \sqrt{b}\right) = \left(\sqrt{a}\right)^2 - \left(\sqrt{b}\right)^2 = a - b$.

(d) $(2x+3)^2 = (2x+3)(2x+3) = 4x^2 + 6x + 6x + 9 = 4x^2 + 12x + 9.$

Note: A quicker way to expand this binomial is to use the formula $(a + b)^2 = a^2 + 2ab + b^2$ with a = 2x and b = 3: $(2x + 3)^2 = (2x)^2 + 2(2x)(3) + 3^2 = 4x^2 + 12x + 9$

- (e) See Reference Page 1 for the binomial formula $(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$. Using it, we get $(x + 2)^3 = x^3 + 3x^2(2) + 3x(2^2) + 2^3 = x^3 + 6x^2 + 12x + 8$.
- 4. (a) Using the difference of two squares formula, $a^2 b^2 = (a + b)(a b)$, we have $4x^2 - 25 = (2x)^2 - 5^2 = (2x + 5)(2x - 5).$
 - (b) Factoring by trial and error, we get $2x^2 + 5x 12 = (2x 3)(x + 4)$.
 - (c) Using factoring by grouping and the difference of two squares formula, we have

$$x^{3} - 3x^{2} - 4x + 12 = x^{2}(x - 3) - 4(x - 3) = (x^{2} - 4)(x - 3) = (x - 2)(x + 2)(x - 3).$$

(d) $x^4 + 27x = x(x^3 + 27) = x(x+3)(x^2 - 3x + 9)$

x

This last expression was obtained using the sum of two cubes formula, $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$ with a = x and b = 3. [See Reference Page 1 in the textbook.]

(e) The smallest exponent on x is $-\frac{1}{2}$, so we will factor out $x^{-1/2}$. $3x^{3/2} - 9x^{1/2} + 6x^{-1/2} = 3x^{-1/2}(x^2 - 3x + 2) = 3x^{-1/2}(x - 1)(x - 2)$

(f)
$$x^{3}y - 4xy = xy(x^{2} - 4) = xy(x - 2)(x + 2)$$

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2 🗆 DIAGNOSTIC TESTS

$$\begin{aligned} \mathbf{5.} & (a) \ \frac{x^2 + 3x + 2}{x^2 - x - 2} = \frac{(x + 1)(x + 2)}{(x + 1)(x - 2)} = \frac{x + 2}{x - 2} \\ & (b) \ \frac{x^2 - x - 1}{2x - 1} + \frac{x + 3}{2x + 1} = \frac{(2x + 1)(x - 1)}{(x - 3)(x + 3)} \cdot \frac{x + 3}{2x + 1} = \frac{x - 1}{x - 3} \\ & (c) \ \frac{x^2 - x - 1}{x^2 - 4} - \frac{x + 1}{x + 2} = \frac{x^2}{(x - 2)(x + 2)} - \frac{x + 1}{x + 2} = \frac{x^2}{(x - 2)(x + 2)} - \frac{x + 1}{x + 2} \cdot \frac{x - 2}{x - 2} = \frac{x^2 - (x + 1)(x - 2)}{(x - 2)(x + 2)} \\ & = \frac{x^2 - (x^2 - x^2 - 2)}{(x + 2)(x - 2)} = \frac{x + 2}{(x + 2)(x - 2)} - \frac{1}{x - 2} \end{aligned}$$

$$(d) \ \frac{y - x}{y} = \frac{y - y}{1 - \frac{x}{x}}, \ \frac{xy}{xy} = \frac{y^2 - x^2}{x - y} = \frac{(y - x)(y + x)}{(-(y - x))} = \frac{y + x}{-1} = -(x + y) \end{aligned}$$

$$\mathbf{6.} & (a) \ \frac{\sqrt{10}}{\sqrt{5 - 2}} = \frac{\sqrt{10}}{\sqrt{5 - 2}} \cdot \frac{\sqrt{5 + 2}}{\sqrt{5 + 2}} = \frac{\sqrt{50 + 2}\sqrt{10}}{(\sqrt{5})^2 - 2^2} = \frac{5\sqrt{2} + 2\sqrt{10}}{5 - 4} = 5\sqrt{2} + 2\sqrt{10} \end{aligned}$$

$$(b) \ \frac{\sqrt{4 + h} - 2}{h} = \frac{\sqrt{4 + h} - 2}{\sqrt{4 + h} + 2} = \frac{4 + h - 4}{h(\sqrt{4 + h} + 2)} = \frac{h}{h(\sqrt{4 + h} + 2)} = \frac{1}{\sqrt{4 + h} + 2} \end{aligned}$$

$$(c) \ x^2 + x + 1 = (x^2 + x + \frac{1}{4}) + 1 - \frac{1}{4} = (x + \frac{1}{2})^2 + \frac{3}{4} \end{aligned}$$

$$(b) \ 2x^2 - 12x + 11 = 2(x^2 - 6x) + 11 = 2(x^2 - 6x + 9 - 9) + 11 = 2(x^2 - 6x + 9) - 18 + 11 = 2(x - 3)^2 - 7 \end{aligned}$$

$$\mathbf{8.} (a) \ x + 5 = 14 - \frac{1}{2}x \ x + \frac{1}{2}x = 14 - 5 \ x = \frac{3}{2}x = 9 \ x = \frac{2}{3} \cdot 9 \ x = 6 \end{aligned}$$

$$(b) \ \frac{2x}{x + 1} = \frac{2x - 1}{x} \ \Rightarrow 2x^2 = (2x - 1)(x + 1) \ \Rightarrow 2x^2 = 2x^2 + x - 1 \ \Rightarrow x = 1 \end{aligned}$$

$$(c) \ x^2 - x - 12 - 0 \ \Leftrightarrow \ (x + 3)(x - 4) = 0 \ \Rightarrow x + 3 = 0 \ \text{or } x - 4 = 0 \ \Rightarrow x = -\frac{4}{2}\sqrt{2} = -1\frac{1}{2}\sqrt{2}.$$

$$(e) \ x^4 - 3x^2 + 2 = 0 \ \Leftrightarrow \ (x^2 - 1)(x^2 - 2) = 0 \ \Rightarrow x^2 - 1 = 0 \ \text{or } x^2 - 2 = 0 \ \Rightarrow x^2 = 1 \ \text{or } x^2 - 2 \ \Rightarrow x = \frac{1}{x} + 1 \ (x^2 - 4x)^2 = \frac{1}{2} \ (x^2 - 1)(x^2 - 2) = 0 \ \Rightarrow x^2 - 1 = 0 \ \text{or } x^2 - 2 = 0 \ \Rightarrow x^2 = 1 \ \text{or } x^2 = 2 \ \Rightarrow x = \frac{1}{x} + 1 \ \text{or } \pm \sqrt{2}$$

$$(f) \ 3|x - 4| = 10 \ \Rightarrow |x - 4| = \frac{10}{3} \ \Rightarrow x - 4 = -\frac{10}{3} \ \text{or } x - \frac{10}{3} \ \Rightarrow \frac{2}{3} \ \text{or } x = \frac{2}{3$$

single test value from each interval, we see that (-2, 4) is the only interval that satisfies the inequality.

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- (c) The inequality x(x − 1)(x + 2) > 0 has critical values of −2, 0, and 1. The corresponding possible intervals of solution are (-∞, -2), (-2, 0), (0, 1) and (1, ∞). By choosing a single test value from each interval, we see that both intervals (-2, 0) and (1, ∞) satisfy the inequality. Thus, the solution is the union of these two intervals: (-2, 0) ∪ (1, ∞).
- (d) $|x-4| < 3 \iff -3 < x 4 < 3 \iff 1 < x < 7$. In interval notation, the answer is (1,7).
- (e) $\frac{2x-3}{x+1} \le 1 \quad \Leftrightarrow \quad \frac{2x-3}{x+1} 1 \le 0 \quad \Leftrightarrow \quad \frac{2x-3}{x+1} \frac{x+1}{x+1} \le 0 \quad \Leftrightarrow \quad \frac{2x-3-x-1}{x+1} \le 0 \quad \Leftrightarrow \quad \frac{x-4}{x+1} \le 0.$ Now, the expression $\frac{x-4}{x+1}$ may change signs at the critical values x = -1 and x = 4, so the possible intervals of solution

are $(-\infty, -1)$, (-1, 4], and $[4, \infty)$. By choosing a single test value from each interval, we see that (-1, 4] is the only interval that satisfies the inequality.

- 10. (a) False. In order for the statement to be true, it must hold for all real numbers, so, to show that the statement is false, pick p = 1 and q = 2 and observe that $(1+2)^2 \neq 1^2 + 2^2$. In general, $(p+q)^2 = p^2 + 2pq + q^2$.
 - (b) True as long as a and b are nonnegative real numbers. To see this, think in terms of the laws of exponents:

$$\sqrt{ab} = (ab)^{1/2} = a^{1/2}b^{1/2} = \sqrt{a}\sqrt{b}.$$

- (c) False. To see this, let p = 1 and q = 2, then $\sqrt{1^2 + 2^2} \neq 1 + 2$.
- (d) False. To see this, let T = 1 and C = 2, then $\frac{1+1(2)}{2} \neq 1+1$.
- (e) False. To see this, let x = 2 and y = 3, then $\frac{1}{2-3} \neq \frac{1}{2} \frac{1}{3}$.
- (f) True since $\frac{1/x}{a/x b/x} \cdot \frac{x}{x} = \frac{1}{a b}$, as long as $x \neq 0$ and $a b \neq 0$.

Test B Analytic Geometry

- 1. (a) Using the point (2, -5) and m = -3 in the point-slope equation of a line, $y y_1 = m(x x_1)$, we get $y (-5) = -3(x 2) \Rightarrow y + 5 = -3x + 6 \Rightarrow y = -3x + 1$.
 - (b) A line parallel to the x-axis must be horizontal and thus have a slope of 0. Since the line passes through the point (2, -5), the y-coordinate of every point on the line is -5, so the equation is y = -5.
 - (c) A line parallel to the y-axis is vertical with undefined slope. So the x-coordinate of every point on the line is 2 and so the equation is x = 2.
 - (d) Note that 2x 4y = 3 ⇒ -4y = -2x + 3 ⇒ y = ¹/₂x ³/₄. Thus the slope of the given line is m = ¹/₂. Hence, the slope of the line we're looking for is also ¹/₂ (since the line we're looking for is required to be parallel to the given line). So the equation of the line is y (-5) = ¹/₂(x 2) ⇒ y + 5 = ¹/₂x 1 ⇒ y = ¹/₂x 6.
- 2. First we'll find the distance between the two given points in order to obtain the radius, r, of the circle: $r = \sqrt{[3 - (-1)]^2 + (-2 - 4)^2} = \sqrt{4^2 + (-6)^2} = \sqrt{52}$. Next use the standard equation of a circle, $(x - h)^2 + (y - k)^2 = r^2$, where (h, k) is the center, to get $(x + 1)^2 + (y - 4)^2 = 52$.

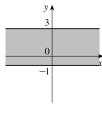
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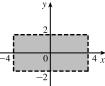
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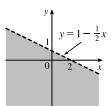
3. We must rewrite the equation in standard form in order to identify the center and radius. Note that

 $x^2 + y^2 - 6x + 10y + 9 = 0 \implies x^2 - 6x + 9 + y^2 + 10y = 0$. For the left-hand side of the latter equation, we factor the first three terms and complete the square on the last two terms as follows: $x^2 - 6x + 9 + y^2 + 10y = 0 \implies (x - 3)^2 + y^2 + 10y + 25 = 25 \implies (x - 3)^2 + (y + 5)^2 = 25$. Thus, the center of the circle is (3, -5) and the radius is 5.

- **4.** (a) A(-7,4) and $B(5,-12) \Rightarrow m_{AB} = \frac{-12-4}{5-(-7)} = \frac{-16}{12} = -\frac{4}{3}$
 - (b) $y-4 = -\frac{4}{3}[x-(-7)] \Rightarrow y-4 = -\frac{4}{3}x \frac{28}{3} \Rightarrow 3y-12 = -4x-28 \Rightarrow 4x+3y+16 = 0$. Putting y = 0, we get 4x + 16 = 0, so the x-intercept is -4, and substituting 0 for x results in a y-intercept of $-\frac{16}{3}$.
 - (c) The midpoint is obtained by averaging the corresponding coordinates of both points: $\left(\frac{-7+5}{2}, \frac{4+(-12)}{2}\right) = (-1, -4)$.
 - (d) $d = \sqrt{[5 (-7)]^2 + (-12 4)^2} = \sqrt{12^2 + (-16)^2} = \sqrt{144 + 256} = \sqrt{400} = 20$
 - (e) The perpendicular bisector is the line that intersects the line segment AB at a right angle through its midpoint. Thus the perpendicular bisector passes through (−1, −4) and has slope ³/₄ [the slope is obtained by taking the negative reciprocal of the answer from part (a)]. So the perpendicular bisector is given by y + 4 = ³/₄ [x (−1)] or 3x 4y = 13.
 - (f) The center of the required circle is the midpoint of \overline{AB} , and the radius is half the length of \overline{AB} , which is 10. Thus, the equation is $(x + 1)^2 + (y + 4)^2 = 100$.
- 5. (a) Graph the corresponding horizontal lines (given by the equations y = -1 and y = 3) as solid lines. The inequality y ≥ -1 describes the points (x, y) that lie on or *above* the line y = -1. The inequality y ≤ 3 describes the points (x, y) that lie on or *below* the line y = 3. So the pair of inequalities -1 ≤ y ≤ 3 describes the points that lie on or *between* the line y = -1 and y = 3.
 - (b) Note that the given inequalities can be written as -4 < x < 4 and -2 < y < 2, respectively. So the region lies between the vertical lines x = -4 and x = 4 and between the horizontal lines y = -2 and y = 2. As shown in the graph, the region common to both graphs is a rectangle (minus its edges) centered at the origin.
 - (c) We first graph $y = 1 \frac{1}{2}x$ as a dotted line. Since $y < 1 \frac{1}{2}x$, the points in the region lie *below* this line.







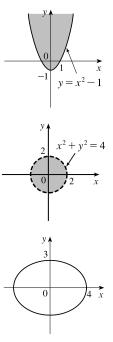
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TEST C FUNCTIONS D 5

- (d) We first graph the parabola $y = x^2 1$ using a solid curve. Since $y \ge x^2 1$, the points in the region lie on or *above* the parabola.
- (e) We graph the circle $x^2 + y^2 = 4$ using a dotted curve. Since $\sqrt{x^2 + y^2} < 2$, the region consists of points whose distance from the origin is less than 2, that is, the points that lie *inside* the circle.
- (f) The equation $9x^2 + 16y^2 = 144$ is an ellipse centered at (0, 0). We put it in standard form by dividing by 144 and get $\frac{x^2}{16} + \frac{y^2}{9} = 1$. The *x*-intercepts are located at a distance of $\sqrt{16} = 4$ from the center while the *y*-intercepts are a distance of $\sqrt{9} = 3$ from the center (see the graph).



Test C Functions

- 1. (a) Locate -1 on the x-axis and then go down to the point on the graph with an x-coordinate of -1. The corresponding y-coordinate is the value of the function at x = -1, which is -2. So, f(-1) = -2.
 - (b) Using the same technique as in part (a), we get $f(2) \approx 2.8$.
 - (c) Locate 2 on the y-axis and then go left and right to find all points on the graph with a y-coordinate of 2. The corresponding x-coordinates are the x-values we are searching for. So x = -3 and x = 1.
 - (d) Using the same technique as in part (c), we get $x \approx -2.5$ and $x \approx 0.3$.
 - (e) The domain is all the x-values for which the graph exists, and the range is all the y-values for which the graph exists. Thus, the domain is [-3, 3], and the range is [-2, 3].
- **2.** Note that $f(2+h) = (2+h)^3$ and $f(2) = 2^3 = 8$. So the difference quotient becomes

$$\frac{f(2+h) - f(2)}{h} = \frac{(2+h)^3 - 8}{h} = \frac{8 + 12h + 6h^2 + h^3 - 8}{h} = \frac{12h + 6h^2 + h^3}{h} = \frac{h(12+6h+h^2)}{h} = 12 + 6h + h^2.$$

3. (a) Set the denominator equal to 0 and solve to find restrictions on the domain: x² + x - 2 = 0 ⇒
(x - 1)(x + 2) = 0 ⇒ x = 1 or x = -2. Thus, the domain is all real numbers except 1 or -2 or, in interval notation, (-∞, -2) ∪ (-2, 1) ∪ (1, ∞).

- (b) Note that the denominator is always greater than or equal to 1, and the numerator is defined for all real numbers. Thus, the domain is (-∞, ∞).
- (c) Note that the function *h* is the sum of two root functions. So *h* is defined on the intersection of the domains of these two root functions. The domain of a square root function is found by setting its radicand greater than or equal to 0. Now,

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6 DIAGNOSTIC TESTS

 $4-x \ge 0 \Rightarrow x \le 4$ and $x^2-1 \ge 0 \Rightarrow (x-1)(x+1) \ge 0 \Rightarrow x \le -1$ or $x \ge 1$. Thus, the domain of h is $(-\infty, -1] \cup [1, 4]$.

4. (a) Reflect the graph of f about the x-axis.

(b) Stretch the graph of f vertically by a factor of 2, then shift 1 unit downward.

(c) Shift the graph of f right 3 units, then up 2 units.

5. (a) Make a table and then connect the points with a smooth curve:

x	-2	-1	0	1	2
y	-8	-1	0	1	8

(b) Shift the graph from part (a) left 1 unit.

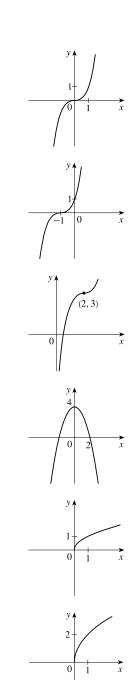
(c) Shift the graph from part (a) right 2 units and up 3 units.

(d) First plot y = x². Next, to get the graph of f(x) = 4 - x², reflect f about the x-axis and then shift it upward 4 units.

(e) Make a table and then connect the points with a smooth curve:

x	0	1	4	9
y	0	1	2	3

(f) Stretch the graph from part (e) vertically by a factor of two.



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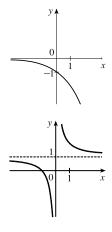
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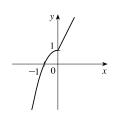
TEST D TRIGONOMETRY D 7

(g) First plot $y = 2^x$. Next, get the graph of $y = -2^x$ by reflecting the graph of $y = 2^x$ about the x-axis.

(h) Note that $y = 1 + x^{-1} = 1 + 1/x$. So first plot y = 1/x and then shift it upward 1 unit.



- **6.** (a) $f(-2) = 1 (-2)^2 = -3$ and f(1) = 2(1) + 1 = 3
 - (b) For x < 0 plot $f(x) = 1 x^2$ and, on the same plane, for x > 0 plot the graph of f(x) = 2x + 1.



7. (a) $(f \circ g)(x) = f(g(x)) = f(2x-3) = (2x-3)^2 + 2(2x-3) - 1 = 4x^2 - 12x + 9 + 4x - 6 - 1 = 4x^2 - 8x + 2$ (b) $(q \circ f)(x) = q(f(x)) = q(x^2 + 2x - 1) = 2(x^2 + 2x - 1) - 3 = 2x^2 + 4x - 2 - 3 = 2x^2 + 4x - 5$ (c) $(g \circ g \circ g)(x) = g(g(g(x))) = g(g(2x-3)) = g(2(2x-3)-3) = g(4x-9) = 2(4x-9) - 3$ = 8x - 18 - 3 = 8x - 21

Test D Trigonometry

- 1. (a) $300^{\circ} = 300^{\circ} \left(\frac{\pi}{180^{\circ}}\right) = \frac{300\pi}{180} = \frac{5\pi}{3}$ (b) $-18^{\circ} = -18^{\circ} \left(\frac{\pi}{180^{\circ}}\right) = -\frac{18\pi}{180} = -\frac{\pi}{10}$ **2.** (a) $\frac{5\pi}{6} = \frac{5\pi}{6} \left(\frac{180}{\pi}\right)^{\circ} = 150^{\circ}$ (b) $2 = 2\left(\frac{180}{\pi}\right)^{\circ} = \left(\frac{360}{\pi}\right)^{\circ} \approx 114.6^{\circ}$
- 3. We will use the arc length formula, $s = r\theta$, where s is arc length, r is the radius of the circle, and θ is the measure of the central angle in radians. First, note that $30^\circ = 30^\circ \left(\frac{\pi}{180^\circ}\right) = \frac{\pi}{6}$. So $s = (12) \left(\frac{\pi}{6}\right) = 2\pi$ cm.
- 4. (a) $\tan(\pi/3) = \sqrt{3}$ [You can read the value from a right triangle with sides 1, 2, and $\sqrt{3}$.]
 - (b) Note that $7\pi/6$ can be thought of as an angle in the third quadrant with reference angle $\pi/6$. Thus, $\sin(7\pi/6) = -\frac{1}{2}$, since the sine function is negative in the third quadrant.
 - (c) Note that $5\pi/3$ can be thought of as an angle in the fourth quadrant with reference angle $\pi/3$. Thus,

 $\sec(5\pi/3) = \frac{1}{\cos(5\pi/3)} = \frac{1}{1/2} = 2$, since the cosine function is positive in the fourth quadrant.

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